



**EARTHQUAKE PLANNING AND  
PROTECTION ORGANIZATION  
(E.P.P.O.)**

**COUNCIL OF EUROPE  
EUROPEAN CENTRE ON PREVENTION  
AND FORECASTING OF EARTHQUAKES  
(E.C.P.F.E.)**



# **TRAINING COURSE ON SEISMIC RISK ASSESSMENT IN SPECIFIC AREAS WITH MONUMENTAL STRUCTURES**

**Athens - December 6-10, 2010**

## **Mechanical models for the seismic performance based assessment of monuments and the design of interventions**

***Sergio Lagomarsino***

**Dept. of Civil, Environmental and Architectural Engineering, University of Genoa, Italy**

**[sergio.lagomarsino@unige.it](mailto:sergio.lagomarsino@unige.it)**

# Performance Based Assessment

Earthquake is a rare environmental action, that must be defined through a probabilistic approach (**hazard scenario**)

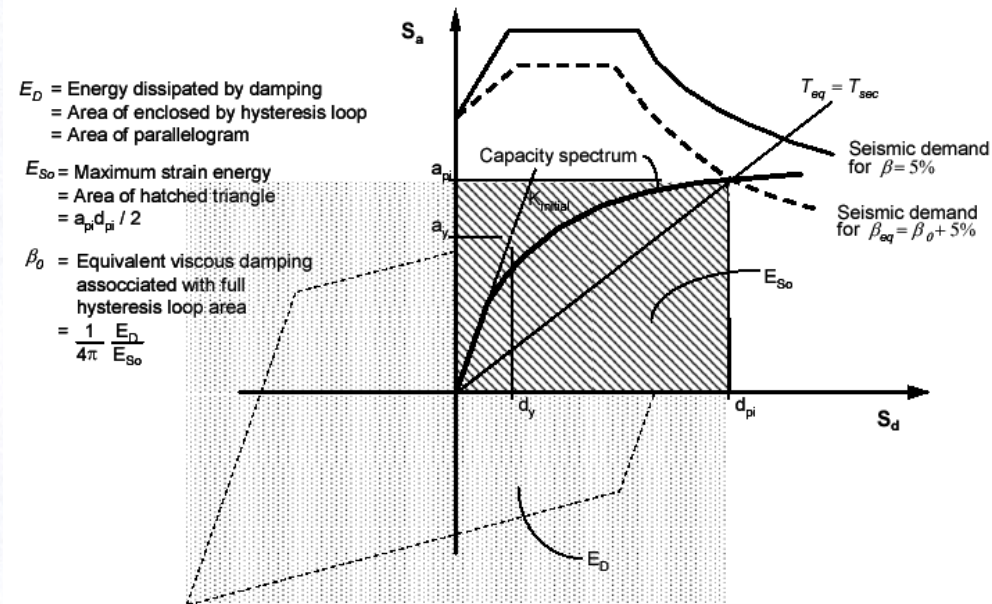
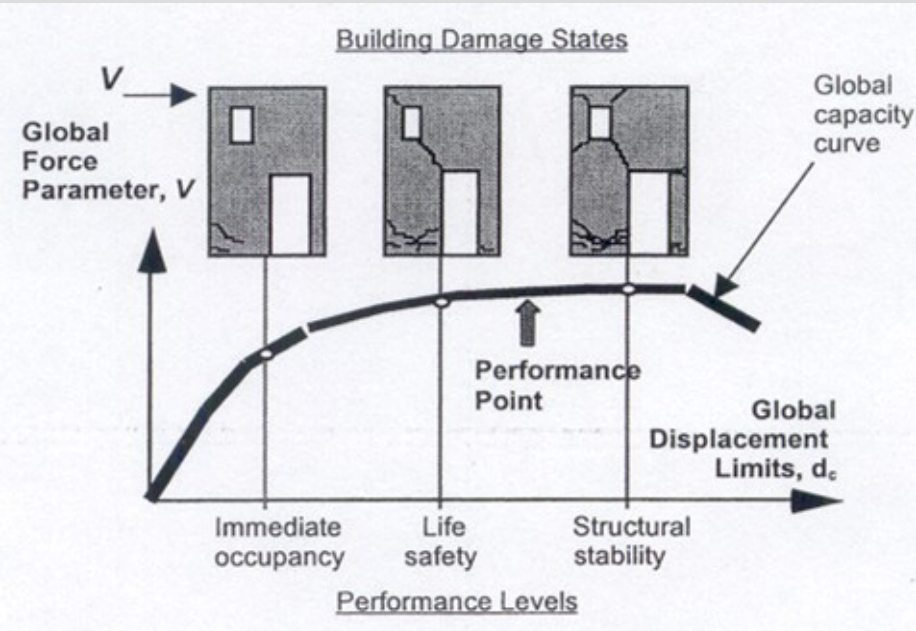
It is impossible to require that an ancient masonry construction withstand without any damage to strong ground motions. Usually we ask that buildings survive to a strong earthquake and suffer few damage for a low intensity earthquake (**performance levels**)



## PERFORMANCE BASED ASSESSMENT AND DESIGN

- FEMA 356 (U.S. Federal Emergency Management Agency), Nov. 2000 – Prestandard and commentary for the seismic rehabilitation of buildings
- Eurocode 8: Design of structures for earthquake resistance - Part 3: Assessment and retrofitting of buildings (June 2005)
- Italian Technical Code for the design of constructions (January 2008)

# Performance Based Assessment



- Earthquake induces horizontal actions on structures.
- Pushover analysis evaluates the behaviour till to collapse. Increasing the displacement: the stiffness decreases, the maximum strength occurs, some constructions may profit by ductility.
- **Performance levels** (or limit states) can be defined on the pushover curve.
- Once the **earthquake hazard level** is defined, displacement demand may be evaluated by CSM (**capacity spectrum method**), using an acceleration-displacement response spectrum, reduced by considering hysteretic damping.

# Performance Based Assessment

## REHABILITATION OBJECTIVES

### Building performance level

### Earthquake hazard levels

#### FEMA 356

LS1	Operational performance		$p=50\%$ in 50 years ( $T_R=72$ years)
LS2	Immediate occupancy		$p=20\%$ in 50 years ( $T_R=225$ years)
LS3	Life safety	→	$p=10\%$ in 50 years ( $T_R=475$ years)
LS4	Collapse prevention	→	$p=2\%$ in 50 years ( $T_R=2475$ years)

#### Eurocode 8 – Part 3

LS-DL	Damage limitation		$p=20\%$ in 50 years ( $T_R=225$ years)
LS-SD	Significant damage		$p=10\%$ in 50 years ( $T_R=475$ years)
LS-NC	Near collapse		$p=2\%$ in 50 years ( $T_R=2475$ years)

#### Eurocode 8 – Part 1

LS-DL	Damage limitation		$p=10\%$ in 10 years ( $T_R=95$ years)
LS-NC	No-collapse		$p=10\%$ in 50 years ( $T_R=475$ years)

#### NTC 2008 (Italian Technical Code)

LS-O	Operational performance		$p=81\%$ in $V_R$ years	
LS-D	Damage limitation	→	$p=63\%$ in $V_R$ years	$V_R$
LS-V	Life safety	→	$p=10\%$ in $V_R$ years	reference life
LS-C	Collapse prevention		$p=5\%$ in $V_R$ years	



# Performance Based Assessment

## REHABILITATION OBJECTIVES

### Building performance level

### Earthquake hazard levels

#### FEMA 356

LS1	Operational performance		$p=50\%$ in 50 years ( $T_R=72$ years)
LS2	Immediate occupancy		$p=20\%$ in 50 years ( $T_R=225$ years)
LS3	Life safety	—————→	$p=10\%$ in 50 years ( $T_R=475$ years)
LS4	Collapse prevention	—————→	$p=2\%$ in 50 years ( $T_R=2475$ years)

#### Eurocode 8 – Part 3

LS-DL	Damage limitation		$p=20\%$ in 50 years ( $T_R=225$ years)
LS-SD	Significant damage		$p=10\%$ in 50 years ( $T_R=475$ years)
LS-NC	Near collapse		$p=2\%$ in 50 years ( $T_R=2475$ years)

#### Eurocode 8 – Part 1

LS-DL	Damage limitation		$p=10\%$ in 10 years ( $T_R=95$ years)
LS-NC	No-collapse		$p=10\%$ in 50 years ( $T_R=475$ years)

#### NTC 2008 (Italian Technical Code)

LS-O	Operational performance		$p=81\%$ in 50 years ( $T_R=30$ years)
LS-D	Damage limitation	—————→	$p=63\%$ in 50 years ( $T_R=50$ years)
LS-V	Life safety	—————→	$p=10\%$ in 50 years ( $T_R=475$ years)
LS-C	Collapse prevention		$p=5\%$ in 50 years ( $T_R=975$ years)

# Italian Guidelines for Cultural Heritage

## Italian Guidelines for evaluation and mitigation of seismic risk to cultural heritage

Ministry of Cultural Heritage – Civil Protection Department – Ministry of Public Works  
(NTC 2008 - Italian Technical Code)

### Building performance level

LS-DL Damage limitation

LS-V Life safety

LS-A Artistic assets

### Earthquake hazard levels

$p=63\%$  in  $V_R$  years

$p=10\%$  in  $V_R$  years

$p=63\%$  in  $V_R$  years

**REFERENCE LIFE** -  $V_R = V_N C_U$

**NOMINAL LIFE** - Is the time in which the building can be considered safe (serviceable period), only assuring structural health monitoring and proper maintenance ( $V_N \leq 50$  years)

**USE COEFFICIENT**  $C_U$  - a) occasional 0.7; b) frequent 1.0;  
c) frequent with crowding 1.5

# Probability of exceedance and return periods

**Tabella 3.2.I** – Probabilità di superamento  $P_{V_R}$  al variare dello stato limite considerato

Stati Limite		$P_{V_R}$ : Probabilità di superamento nel periodo di riferimento $V_R$
Stati limite di esercizio	SLO	81%
	SLD	63%
Stati limite ultimi	SLV	10%
	SLC	5%

$$T_R = \frac{1}{1 - e^{\frac{\ln(1-P_{V_R})}{V_R}}} \cong -\frac{V_R}{\ln(1 - P_{V_R})}$$

$$P_{V_R} = 1 - e^{-V_R / T_R}$$

$$P_{\text{annuale}} = 1 - e^{-1/T_R}$$

	$P_{V_r}$				
SLD	63%	35	50	75	101

	$C_U$	0.7	1	1.5	2
$V_N = 50$	$V_R$	35	50	75	100
	$P_{V_r}$	Annual probability of exceedance			
SLD	63%	2.8%	2%	1.3%	1%
SLV	10%				



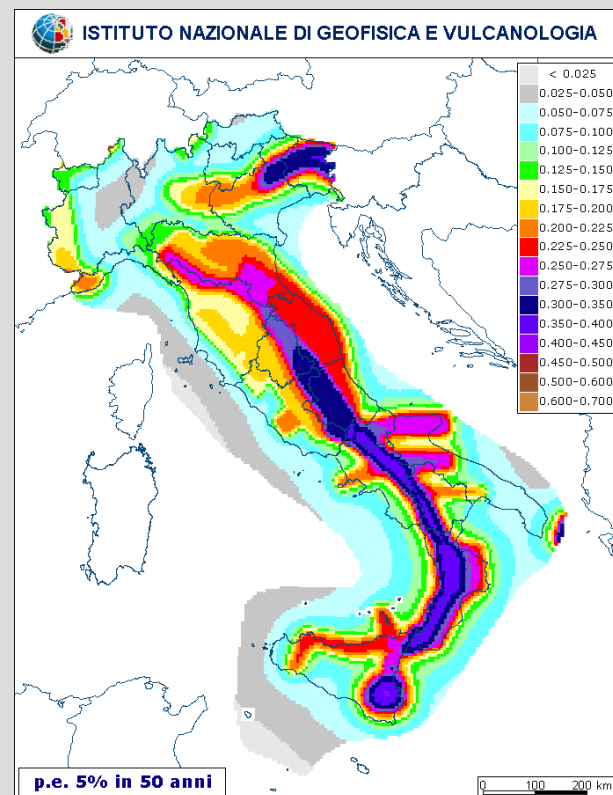
## INGV-DPC Framework project 2004-2006

### S1 Project

## Seismic Hazard in Italy: PGA for different occurrence probabilities in 50 years

*C. Meletti, V. Montaldo*

Occurrence probability in 50 years	Return period	Annual rate of exceedance	File (download)
<b>81%</b>	30	0.0332	(file zip - 631 kb)
<b>63%</b>	50	0.0199	(file zip - 642 kb)
<b>50%</b>	72	0.0139	(file zip - 651 kb)
<b>39%</b>	101	0.0099	(file zip - 657 kb)
<b>30%</b>	140	0.0071	(file zip - 650 kb)
<b>22%</b>	201	0.0050	(file zip - 666 kb)
<b>10%</b>	475	0.0021	<b>MPS04</b>
<b>5%</b>	975	0.0010	(file zip - 682 kb)
<b>2%</b>	2475	0.0004	(file zip - 686 kb)

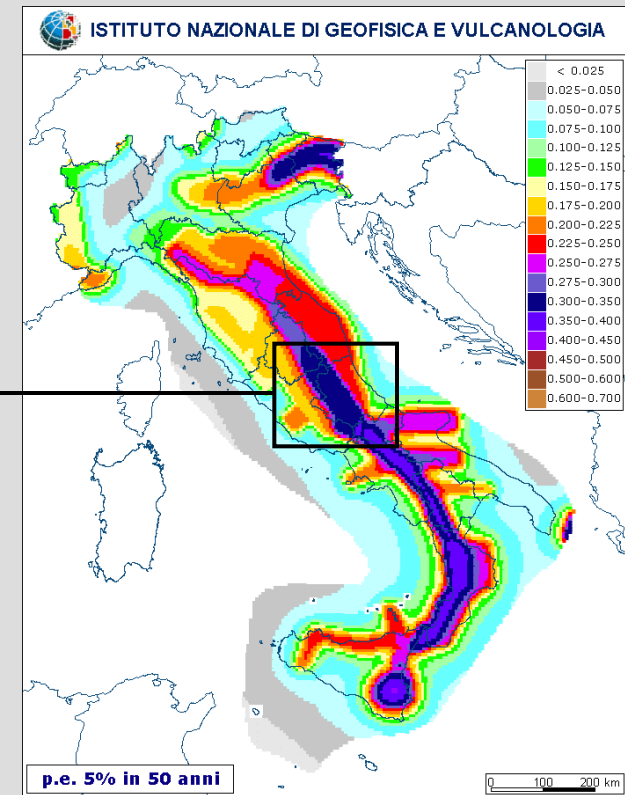
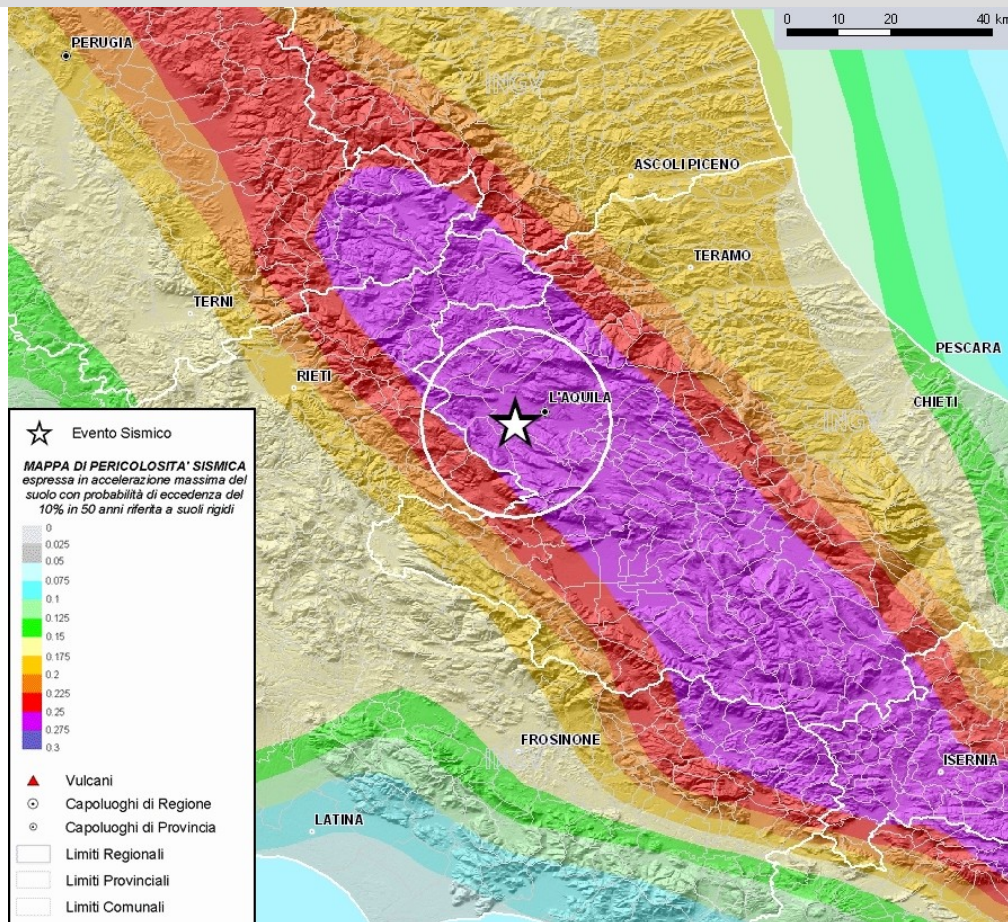




**INGV-DPC Framework project 2004-2006**  
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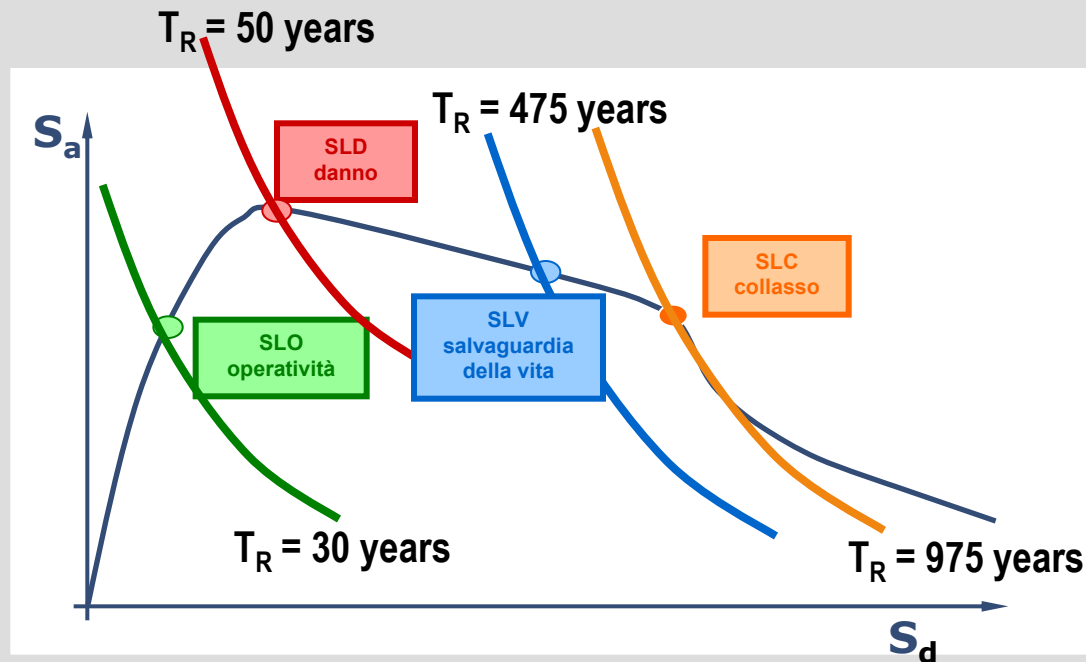
*C. Meletti, V. Montaldo*



# Performance based assessment

**Tabella 3.2.I** – Probabilità di superamento  $P_{V_R}$  al variare dello stato limite considerato

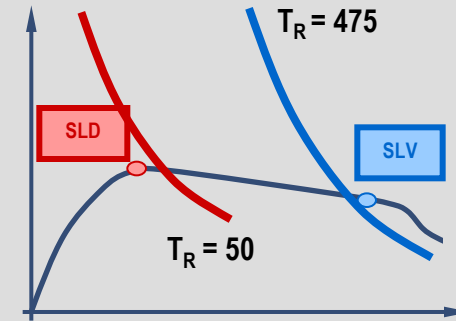
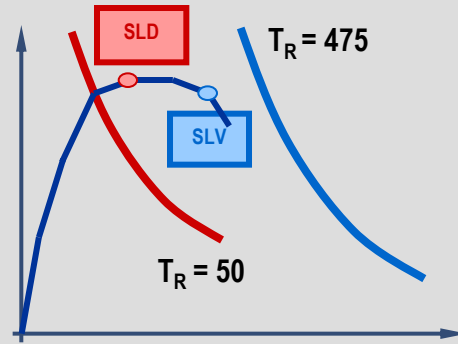
Stati Limite		$P_{V_R}$ : Probabilità di superamento nel periodo di riferimento $V_R$
Stati limite di esercizio	SLO	81%
	SLD	63%
Stati limite ultimi	SLV	10%
	SLC	5%





# Why it is necessary to consider different limit state?

## STRENGTH and DUCTILITY



## SEISMIC HAZARD

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Sono state approvate e registrate le nuove Circolari recanti i criteri per il rilascio delle autorizzazioni ai laboratori per l'esecuzione e la certificazione delle prove sui materiali da costruzione tradizionali, sul legno, sulle terre e sulle rocce, nonché per le indagini geognostiche, il prelievo dei campioni e le prove in...

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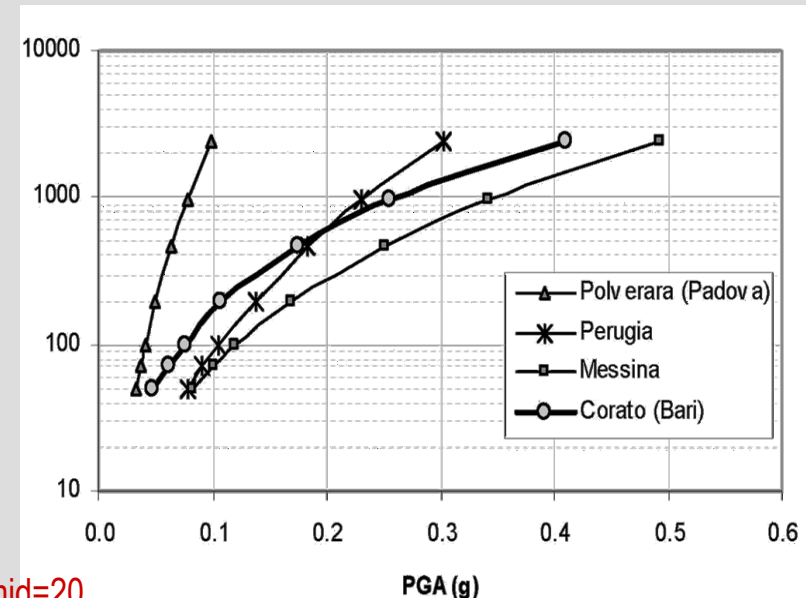
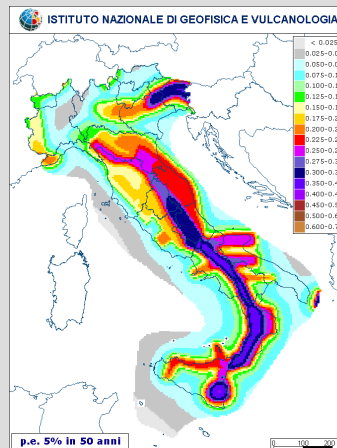
È in linea ed è possibile scaricare la NUOVA VERSIONE 1.03 del programma sperimentale "Spettri di risposta" che fornisce gli spettri di risposta rappresentativi delle componenti (orizzontali e verticale) delle azioni sismiche di progetto per il generico sito del territorio nazionale.

L'utente potrà visualizzare e stampare i risultati delle elaborazioni - in forma sia grafica che numerica - nonché i relativi elementi alle nuove Norme Tecniche per le Costruzioni di cui al D.M. 14.01.2008 pubblicato nella G.U. n.29 del 04.02.2008 Suppl. Ordinario n.30 e scaricabile dal sito [www.cslp.it](http://www.cslp.it)

La verifica dell'adempimento del programma, l'utilizzo dei risultati da esso ottenuti sono a cura e responsabilità esclusiva dell'utente.

Il Consiglio Superiore dei Lavori Pubblici non potrà essere ritenuto responsabile degli eventuali danni conseguenti all'utilizzo del stesso.

Download - Spettri 2008 ver. 1.03



Sito da dove scaricare il programma "Spettri di risposta"

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# Guidelines for Cultural Heritage

**NOMINAL LIFE**  $V_N$  - Is the time in which the building can be considered safe (serviceable period), only assuring structural health monitoring and proper maintenance ( $V_N \leq 50$  years)

## What does it means?

If I made a safety check for a monumental building considering  $V_N=50$  years, does it mean that the monument will stand only for 50 years?

Is the age of the monument important in this evaluation?

What can I do after 50 years from this evaluation?

## Some short and preliminary answers:

The age of the monument is not important, as I diagnose the actual state of the building after proper investigations.

50 years from now I will evaluate again the seismic safety, considering an updated hazard scenario (possibly obtained by time-dependent models).



# THE USE OF NOMINAL LIFE

**Nominale life:** Is the time in which the building can be considered safe, only assuring structural health monitoring and proper maintenance .

It is not the **residual life (LCA – life cycle assessment)**, evaluated considering the decay of materials, but only the period in which the building can be considered safe (from a probabilistic point of view).

The nominal life of a monument should be very long, because we would like to preserve the building forever; to this end we should consider the earthquake action related to a long return period (i.e. the maximum possible earthquake in the site).

However, this would lead to the design of invasive interventions, not compatible with the conservation. So the interventions can refer to a reduced value of the nominal life.

Further interventions will be eventually adopted in the future, at the end of the nominal life assumed today. At that time further information will be available on:

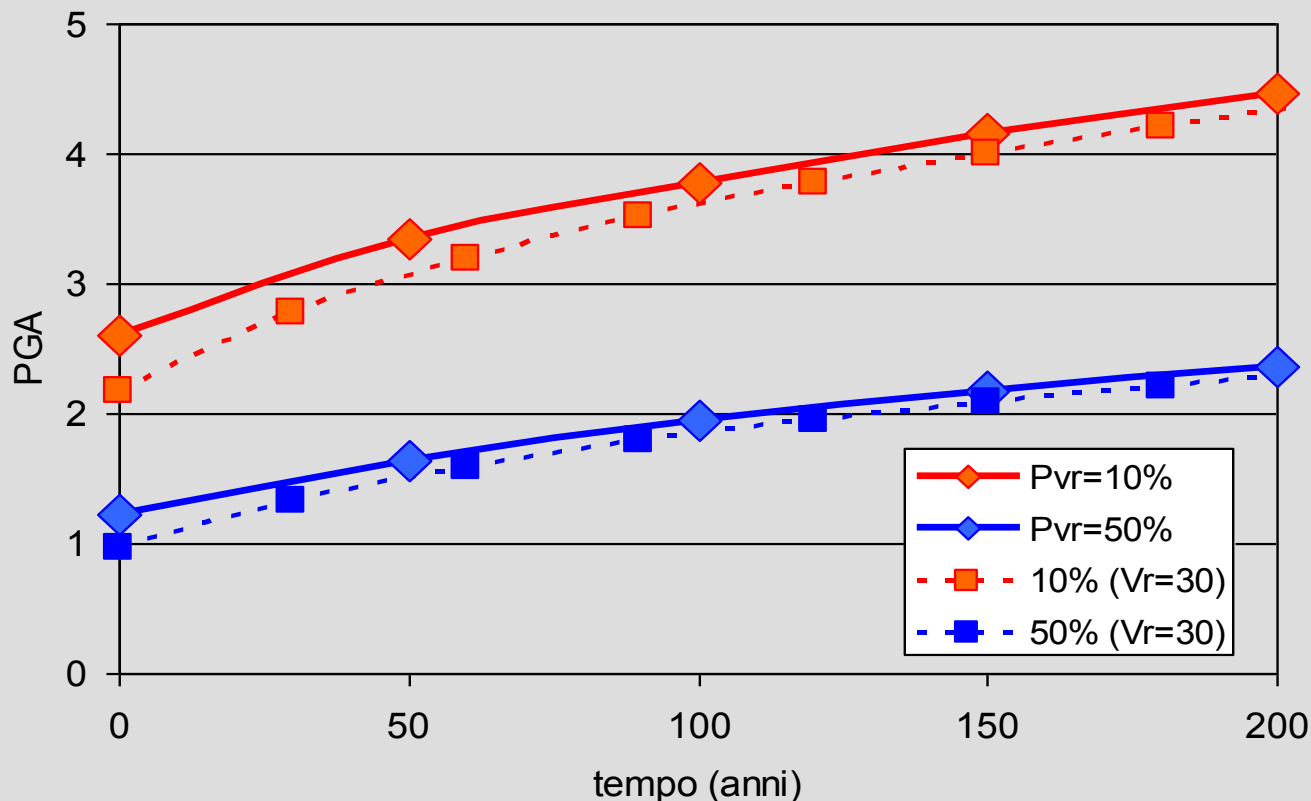
- 1) **seismic hazard**; 2) **building capacity** (new more detailed mechanical models);
- 3) **strengthening interventions** (more effective and less invasive).

When we design a restoration intervention, we decide which are the effective strengthening solutions that reduce vulnerability and are compatible with the conservation criteria. Then, we evaluate  $V_N$ , the time of validity of this check.

# What will be necessary at the end of the nominal life?

The seismic hazard to be used for the next check will have to consider the time that has gone by (time-dependent hazard maps).

If the available hazard will still be time-independent (Poisson model), the reference period to be considered for the next check will must take into account the time that has passed.



## PERformance-based aPproach to EArthquake proTection of cUlturAl heriTage in European and mediterranean countries

- Development of European Guidelines for the evaluation and mitigation of seismic risk to cultural heritage assets.
- Both architectonic assets (historic buildings; macroelements) and artistic assets (frescos, stucco-works, statues, pinnacles, battlements, banisters, balconies ...) will be considered. Only masonry structures will be considered.
- Two different scales will be considered:
  - a) assessment at the territorial scale including simplified vulnerability and risk analysis and policy issues for seismic risk mitigation
  - b) assessment of a single cultural heritage asset and design of interventions

# PERformance-based aPproach to EArthquake proTection of cUlturAl heriTage in European and mediterranean countries

**PERPETUATE** means “to preserve from extinction”

In the case of cultural heritage assets this means to extend their survival towards **infinity**.

The symbol of infinity is used as a conceptual key for the logo, together with the propagation of seismic waves.





**Time is the keyword for the conservation of cultural heritage.**

**Periodic maintenance protects against material decay, ensuring endless life to buildings.**

**Structural health monitoring controls the occurrence of damage or instability due to anthropic or environmental transformations.**

**Preventive actions must be adopted in order to PERPETUATE the life of monuments in seismic areas, in due time, before an earthquake interrupts their life forever.**

*Sergio Lagomarsino*

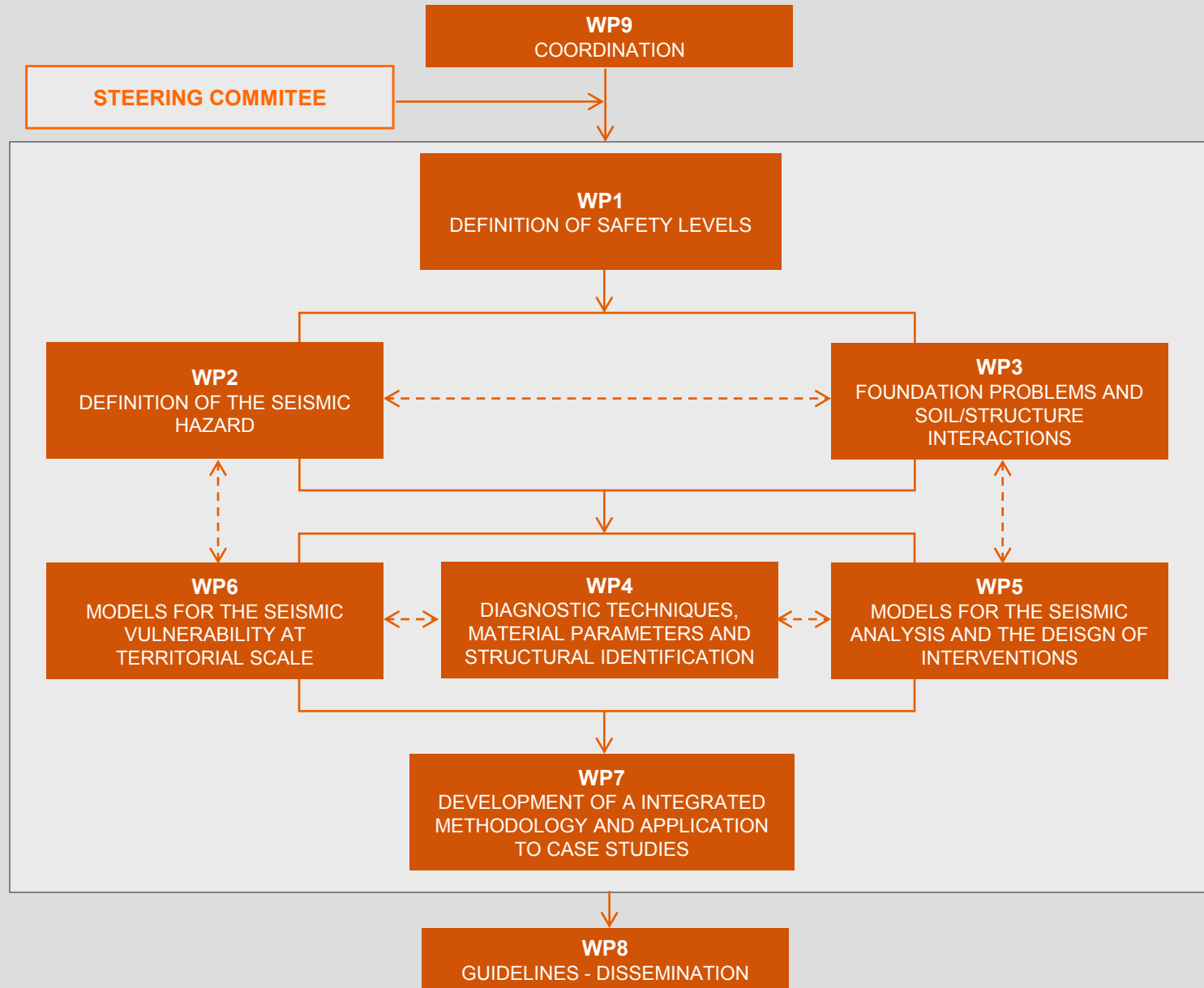
Coordinator of PERPETUATE Project

The Consortium consists of:

- **6 Universities** (Genoa, Thessaloniki, Athens, Ljubljana, Bath, Algiers)
- **2 Public/Research Institutions** (ENEA, Italy; BRGM, France)
- **3 SMEs** from Slovenia (ZMRK) and Italy (CENACOLO, PHASE).







## TASK 8.2: Application to the Citadel and the Great Mosque of Algiers (Algeria)



## TASK 8.3: Application to the historical centre of Rhodes (Greece)





# WP7 – APPLICATION TO CASE STUDIES

## TASK 8.4: Application to the case studies selected in the Abruzzo region (Italy)



## TASK 8.5: Application to the St. Pardo Cathedral in Larino (Molise Region, Italy)



## TASK 8.6: Application to the Cathedral St. Nicholas in Ljubljana

# SHAKING TABLE TESTS AT ENEA, ROME



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progetto Reluis Linea 1



A photograph showing a physical model of a building structure undergoing a shaking table test. The model is a two-story structure with a gabled roof, constructed from white blocks. It is mounted on a large, dark, rectangular base. The model shows significant damage, with many blocks missing and the structure appearing to be in a state of collapse. The background is a plain, light-colored wall.





PERFORMANCE-BASED APPROACH TO EARTHQUAKE PROTECTION OF  
CULTURAL HERITAGE IN EUROPEAN AND MEDITERRANEAN COUNTRIES

European Research Project funded by FP7



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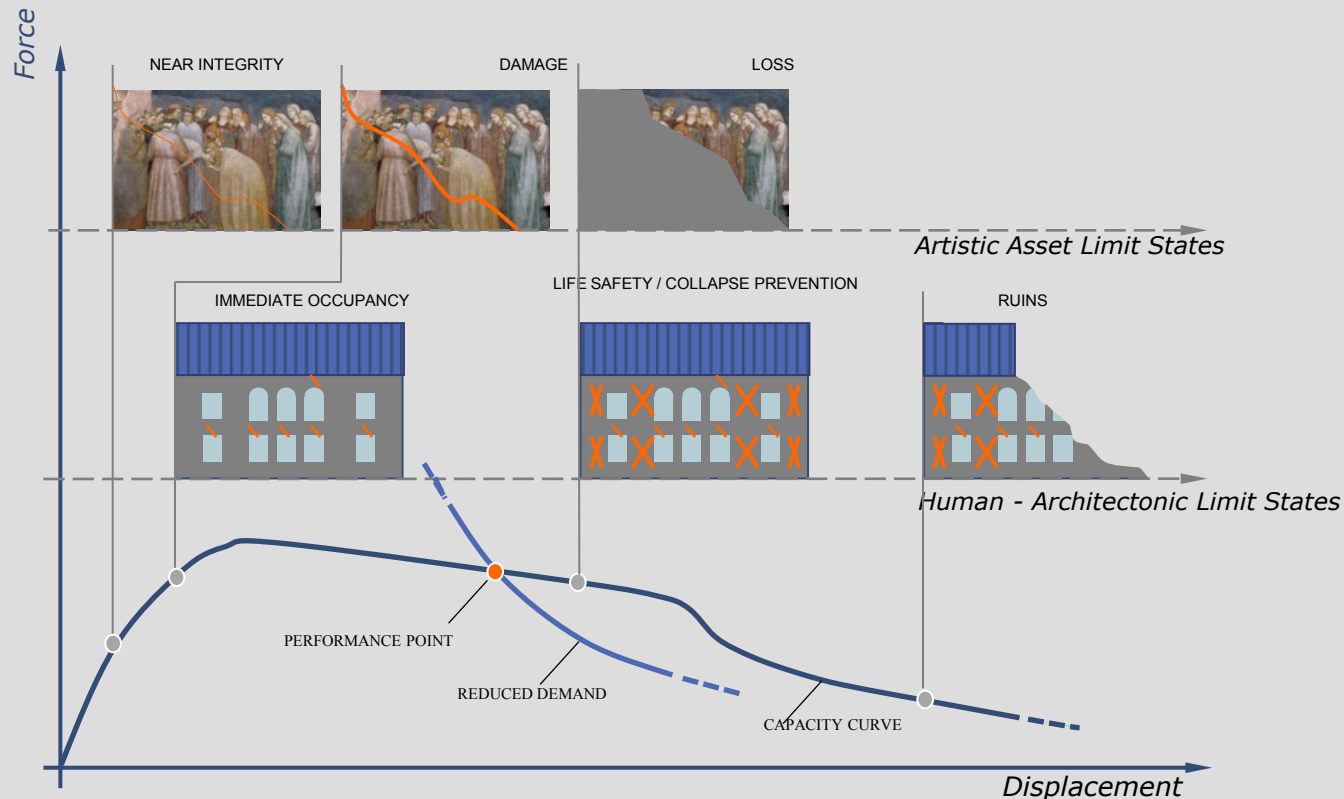
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Reference websites and partners

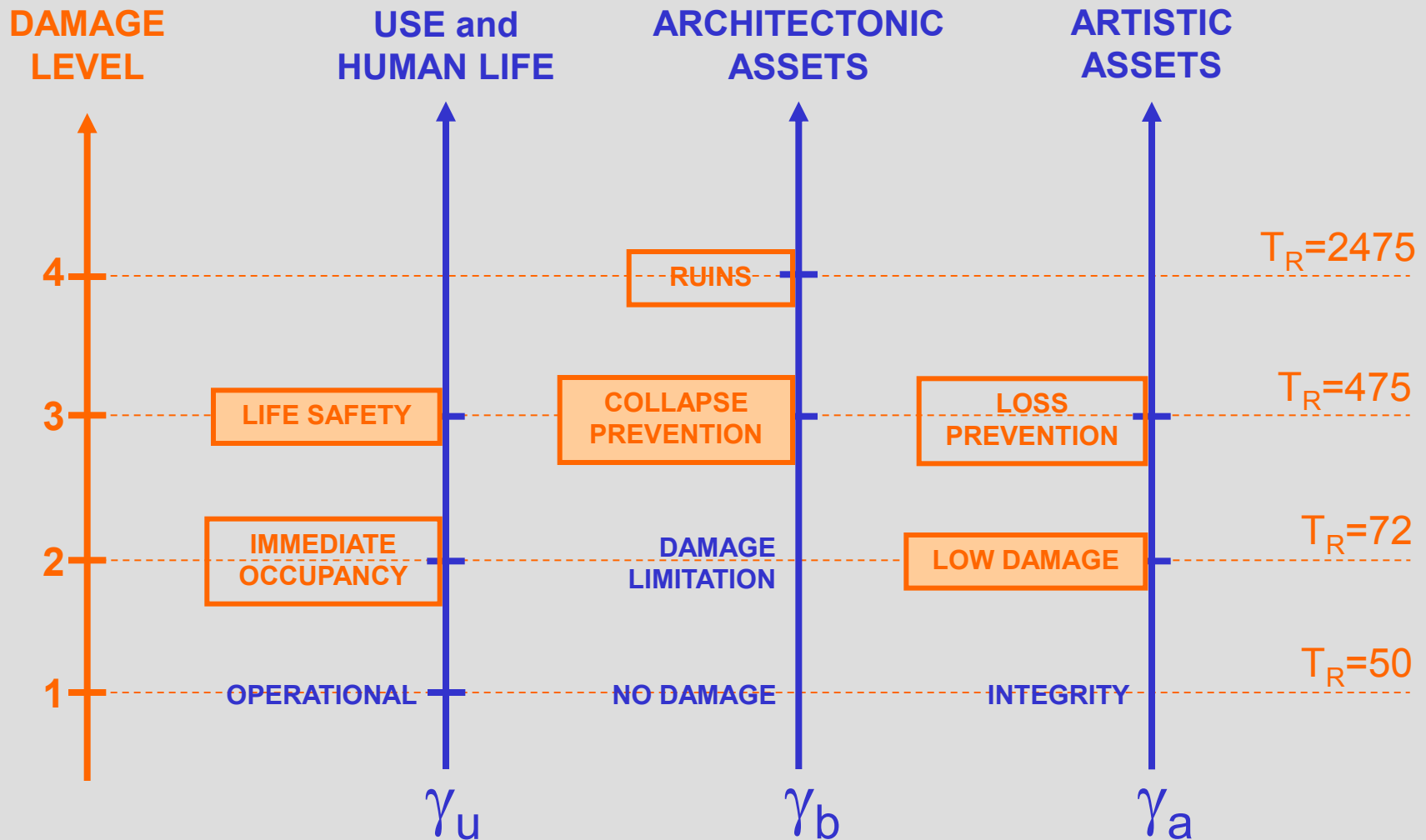
[www.perpetuate.eu](http://www.perpetuate.eu)

Displacement-based approach for the seismic assessment of architectural and artistic assets and for the design of strengthening interventions:

- 1) evaluation of the capacity curve by a non linear static analysis;
- 2) identification of performance limit states;
- 3) evaluation of the performance point by capacity spectrum method



## Main and secondary limit states





## Introduction of coefficients modifying the reference return period

### 1. USE AND HUMAN LIFE

#### USE ( $\gamma_u$ )

FUNCTION OF: BUILDING USE; CROWDING LEVEL.

$\gamma_u < 1$  WHETHER THE BUILDING IS RARELY USED. IF  $\gamma_u < 1$ , THE ASSESSMENT OF PERFORMANCE LEVEL "IO" IS NOT REQUIRED.

### 2. ARCHITECTONIC ASSETS

#### ARCHITECTONIC RELEVANCE ( $\gamma_b$ )

FUNCTION OF: CULTURAL VALUE OF THE BUILDING ITSELF.

$\gamma_b > 1$  WHETHER THE BUILDING HAS A PARTICULAR CULTURAL RELEVANCE.  $\gamma_b > 1$ , THE ASSESSMENT OF PERFORMANCE LEVEL "RU" IS REQUIRED

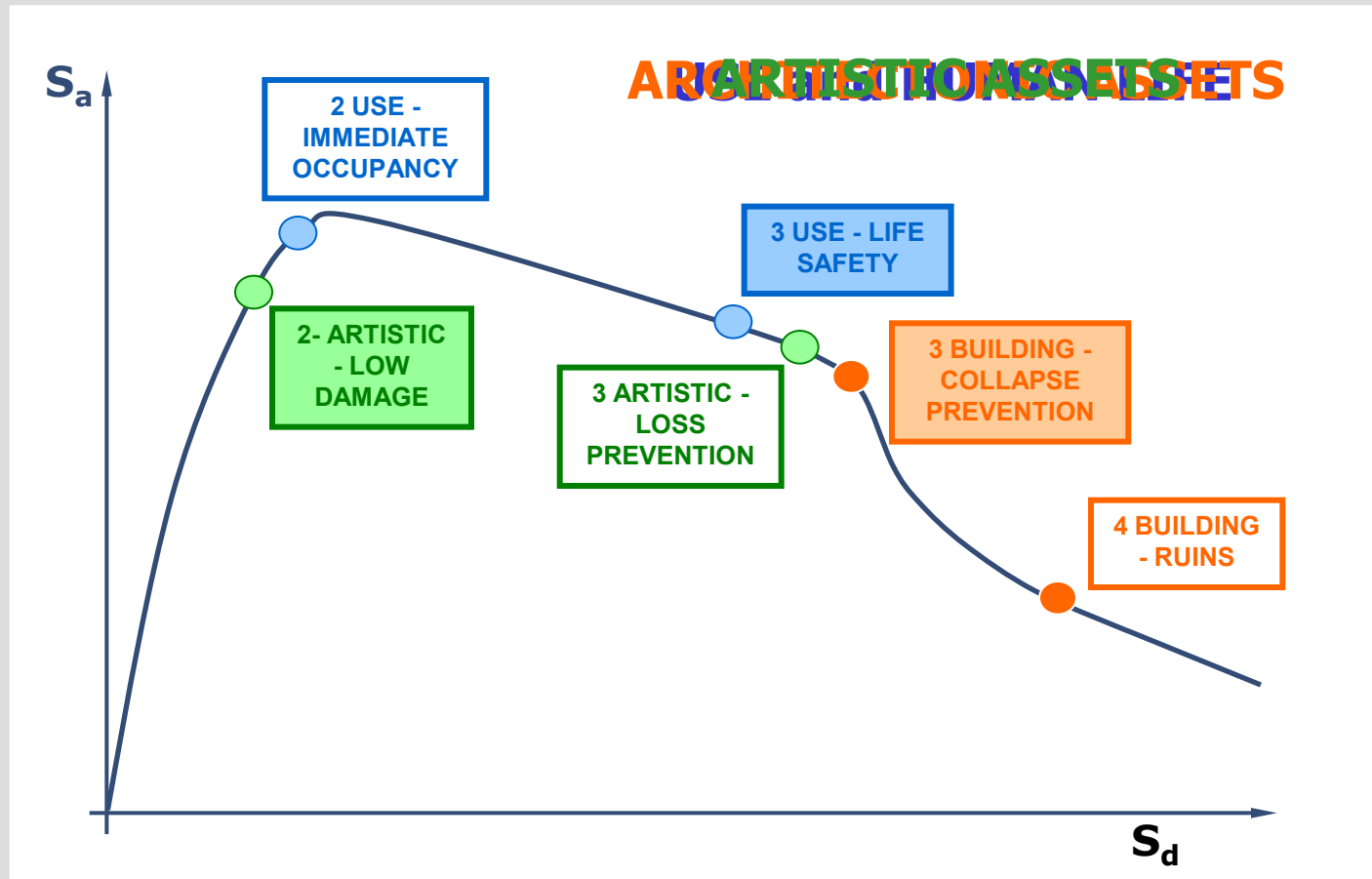
### 3. ARTISTIC ASSETS

#### ARTISTIC RELEVANCE ( $\gamma_a$ )

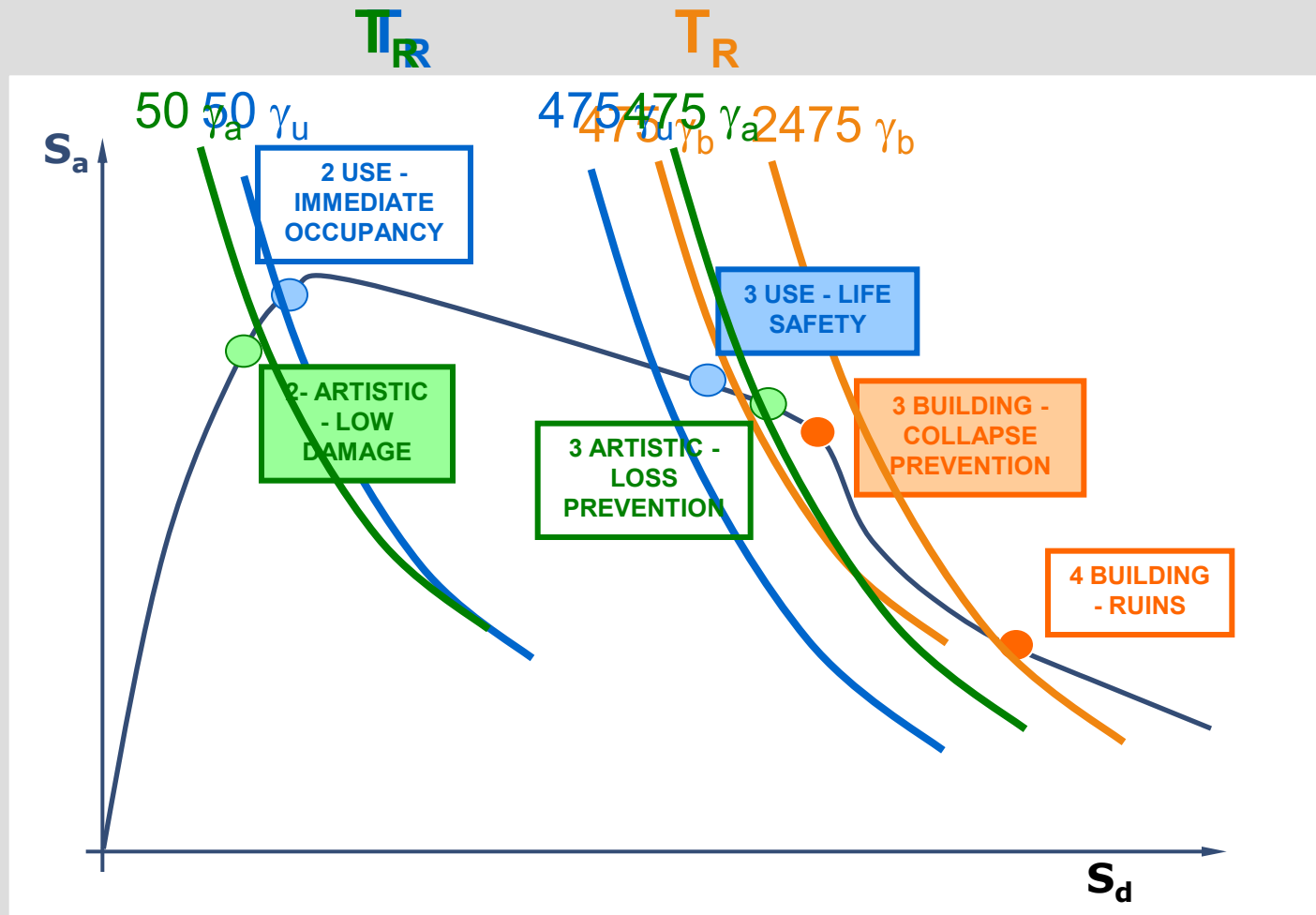
FUNCTION OF: CULTURAL VALUE OF THE ARTISTIC ASSETS PRESENT IN THE BUILDING.

$\gamma_a > 1$  WHETHER THE ASSETS HAVE A PARTICULAR CULTURAL RELEVANCE.  $\gamma_a > 1$ , THE ASSESSMENT OF PERFORMANCE LEVEL "LP" IS REQUIRED

Multicriteria probabilistic approach for the definition of performance limit states: 1) global behaviour; 2) macroelement; 3) local damage



# PERFORMANCE-BASED ASSESSMENT



# CLASSIFICATION OF ARCHITECTONIC ASSETS



It is functional to model main seismic behaviour of buildings

Classes	Description	List of assets
A	This class collects architectonic assets with two main bearing structural elements: <b>vertical walls</b> and <b>horizontal floors</b> . If they are properly connected, mutual cooperation between the structural elements allows the building to <b>behave as a box</b> .	A1 <i>palaces</i> , A2 <i>castles</i> , A3 <i>religious houses</i> , A4 <i>caravansaries</i> , A5 <i>madrasas</i>
B	This class collects architectonic assets which are characterized by <b>wide spaces without intermediate floors</b> and few inner walls. Independent damage mechanisms occurs in the different parts of the building, and it is often possible to recognize <b>specific structural macroelements</b> (façade, triumphal arch, apse, dome, transept,...).	B1 <i>churches</i> , B2 <i>mosques</i> , B3 <i>temples</i> , B4 <i>baptisteries</i> , B5 <i>mausoleum</i> , B6 <i>hammam</i> B7 <i>theatres</i>
C	This class collects architectonic assets in which the <b>vertical dimension prevails</b> on the other ones. Since usually, these buildings are characterized by significant slenderness, their seismic response may be assumed as a <b>global flexural behavior</b> .	C1 <i>towers</i> , C2 <i>bell towers</i> , C3 <i>minarets</i> , C4 <i>lighthouses</i> , C5 <i>chimneys</i>
D	This class collects architectonic assets in which the main structural element is an <b>arch</b> or a <b>vault</b> . Both single arches or much more complex constructions based on this basic structural element are included.	D1 <i>triumphal arches</i> , D2 <i>aqueducts</i> , D3 <i>bridges</i> , D4 <i>cloisters</i>
E	This class collects <b>massive constructions</b> in which the wide thickness of walls, if compared to other dimensions, doesn't allow the idealization as plane structural element. <b>Local failure occurs</b> as, for example, the detachment of external leaf.	E1 <i>fortresses</i> , E2 <i>defensive city walls</i>
F	This class collects <b>single isolated architectonic assets</b> , which does not delimit an interior space.	F1 <i>columns</i> , F2 <i>trilithes</i> , F3 <i>obelisks</i> , F4 <i>archaeological ruins</i>
G	This class refers to <b>historical centers</b> , made of ordinary buildings' aggregates, which assume the relevance of cultural heritage asset as whole in the urban context. The seismic response must consider the interaction among adjacent buildings.	

## BOX-TYPE STRUCTURES (vertical walls and horizontal floors)

Classes	Description	List of assets
A	This class collects architectonic assets with two main bearing structural elements: <u>vertical walls</u> and <u>horizontal floors</u> . If they are properly connected, mutual cooperation between the structural elements allows the building <u>to behave as a box</u> .	A1 palaces, A2 castles, A3 religious houses, A4 caravansaries, A5 madrasas

### A1 Palaces



### A2 Castles



### A3 Religious houses



### A4 Caravansaries





## WIDE HALLS WITHOUT INTERMEDIATE FLOORS (macroelements)

Classes	Description	List of assets
B	This class collects architectonic assets which are characterized by <u>wide spaces without intermediate floors</u> and few inner walls. Independent damage mechanisms occurs in the different parts of the building, and it is often possible to recognize <u>specific structural macroelements</u> (façade, triumphal arch, apse, dome, transept,...).	B1 churches, B2 mosques, B3 temples, B4 baptisteries, B5 mausoleum, B6 hammam B7 theatres

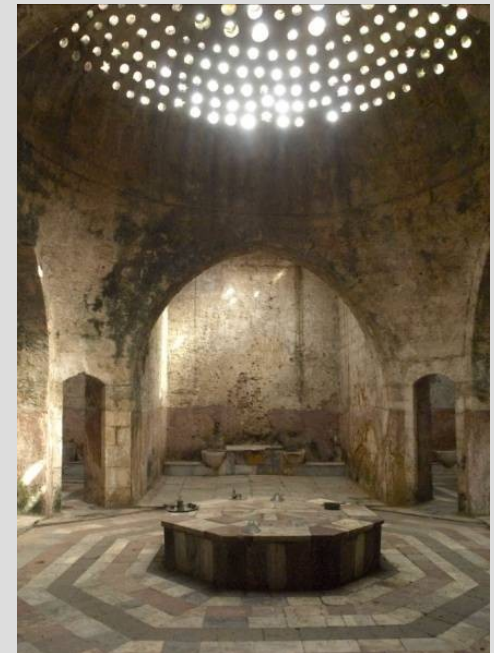
B1 Churches



B2 Mosques



B6 Hammam



## SLENDER MASONRY STRUCTURES

Classes	Description	List of assets
C	This class collects architectonic assets in which the <u>vertical dimension prevails</u> on the other ones. Since usually, these buildings are characterized by significant slenderness, their seismic response may be assumed as a <u>global flexural behavior</u> .	C1 towers, C2 bell towers, C3 minarets, C4 lighthouses, C5 chimneys

*C1 Towers*



*C2 Bell Towers*



*C3 Minarets*



*C4 Lighthouses*





## ARCHED AND VAULTED STRUCTURES

Classes	Description	List of assets
D	This class collects architectonic assets in which the main structural element is an <b>arch</b> or a <b>vault</b> . Both single arches or much more complex constructions based on this basic structural element are included.	D1 <i>triumphal arches</i> , D2 <i>aqueducts</i> , D3 <i>bridges</i> , D4 <i>cloisters</i>

### D1 Triumphal arches



### D4 Cloisters



### D2 Acqueducts



## MASSIVE MASONRY CONSTRUCTIONS

Classes	Description	List of assets
E	This class collects <u>massive constructions</u> in which the wide thickness of walls, if compared to other dimensions, doesn't allow the idealization as plane structural element. <u>Local failure occurs</u> as, for example, the detachment of external leaf.	E1 fortresses, E2 defensive city walls

*E1 Fortress*



*E2 Defensive city walls*



## DRY BLOCKS SIMPLE STRUCTURES

Classes	Description	List of assets
F	This class collects <u>single isolated architectonic assets</u> , which does not delimit an interior space.	F1 <i>columns</i> , F2 <i>trilithes</i> , F3 <i>obelisks</i> , F4 <i>archaeological ruins</i>

F1 Columns



F2 Trilithes



F3 Obelisks





## AGGREGATED BUILDINGS IN HISTORICAL CENTRES

Classes	Description	List of assets
G	This class refers to <u>historical centers</u> , made of ordinary buildings' aggregates, which assume the relevance of cultural heritage asset as whole in the urban context. The seismic response must consider the interaction among adjacent buildings.	

*Navelli, L'Aquila, Italy*



*Skofja Loka, Slovenia*



# CLASSIFICATION OF ARTISTIC ASSETS



Class	Description	Sub-class	Examples
P	<b>Artistic assets which are structural elements themselves</b>	P1 – carved or shaped vertical structural assets	Caryatid, carved stone columns, walls with carved blocks or shaped bricks, ...
		P2 – carved or decorated horizontal structural assets	Carved stone or wooden lintels, decorated wooden beams, ...
		P3 – carved structural arched assets	Carved stone arches, vaults and domes, etc.
		P4 – carved or decorated wooden roof	Decorated wooden roof, etc.
Q	<b>Artistic assets which are strictly connected to structural elements</b>	Q1 – assets connected to vertical structural elements	Carved stone plates, frescos, mosaics, stuccoes, ...
		Q2 – assets connected to the intrados of horizontal and arched structural elements	<b>Frescos, mosaics</b> , stuccoes, wooden or plaster false ceiling, light thin plaster vaults, ...
		Q3 – assets connected to the extrados of horizontal structural elements	Floor with mosaics, decorated tiles, parquets, ...
R	<b>Artistic assets which has their own seismic response</b>	R1 – assets leant on horizontal structural elements	<b>Pinnacles</b> , altars, sculptures, pulpits, ...
		R2 – assets jutting out from vertical structural elements	Balconies, shelves, gargoyles, ...
		R3 – assets hanging on horizontal structural elements	Lamps, bells, crosses, ...

It is functional to model the seismic behaviour



## Q - Artistic assets connected to structural elements

- ROSE WINDOWS



- PORTALS





## Q -Artistic assets connected to structural elements

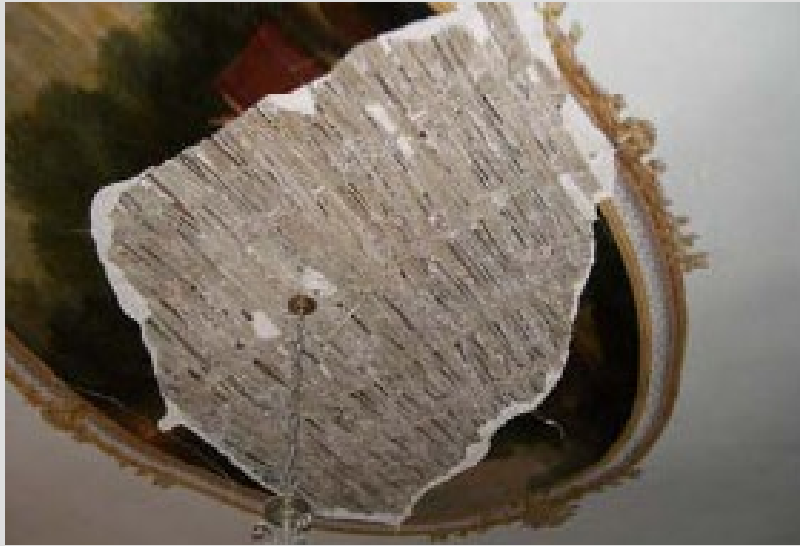
- San Bernardino, L'Aquila





## Q - Artistic assets connected to structural elements

- LATHWORK VAULTS



- FRESCOES



# R - Artistic assets with their own seismic response

- PINNACLES, STATUES



- CORBELS, GARGOYLES



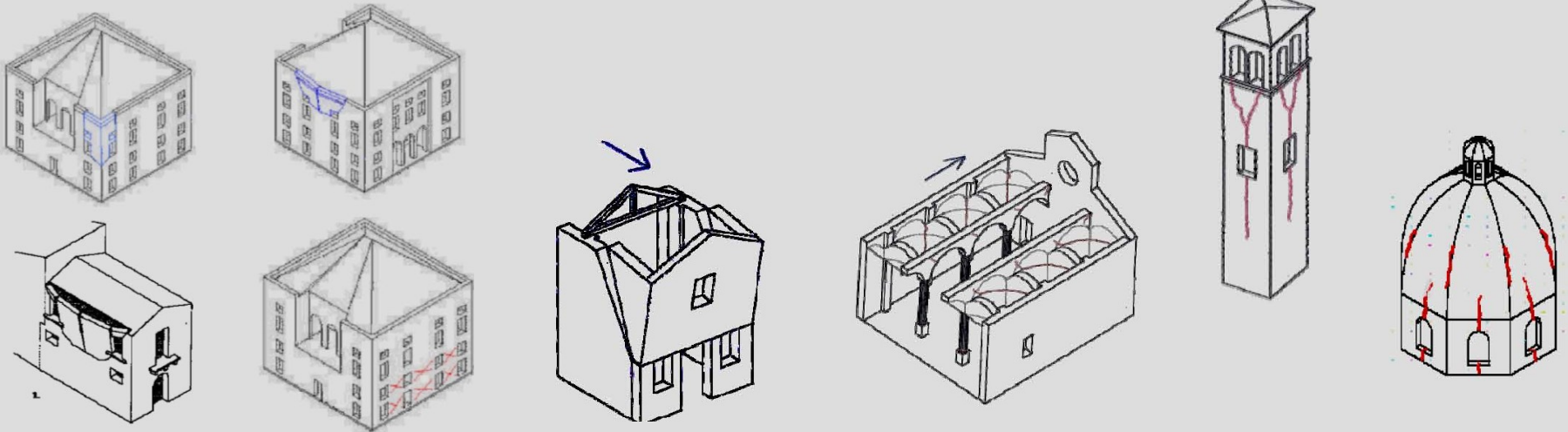


It is possible to identify different **seismic damage modes** for cultural heritage assets, related to the different classes previously defined.

## ***ARCHITECTONIC AND ARTISTIC ASSETS CLASSIFICATION***



## ***DAMAGE CLASSIFICATION***





## Correlation between type of building and damage classification

	A	B	C	D	E	F	G
1 – in plane							
2 – out of plane				D2			
3 – flexural/crushing							
4 – arches			C2				
5 – local masonry failure							
6 – blocks							
7 – floors / roofs					E1		
8 – vaults							
9 – domes							

- Prevailing behaviour
- Possible behaviour
- Occasional behaviour

The table above is only qualitative and based most on the presence of macroelements than on frequency of damage.

# SEISMIC BEHAVIOUR OF MASONRY BUILDINGS

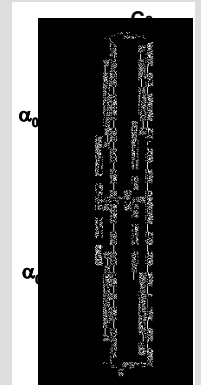
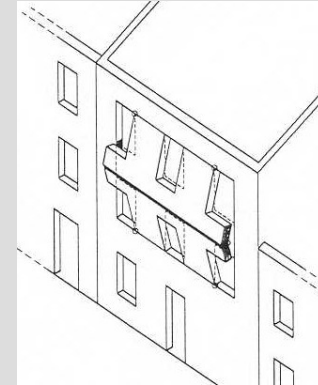
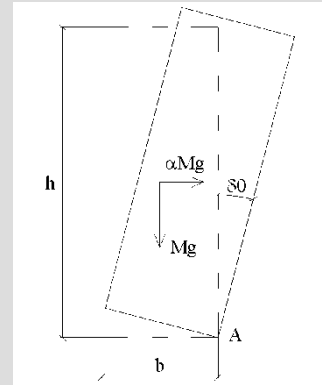
**L'AQUILA, ITALY – 2009**



- TASK 5.1 – Modelling of local mechanisms of buildings



OUT-OF-PLANE MECHANISMS  
(1° failure mode)



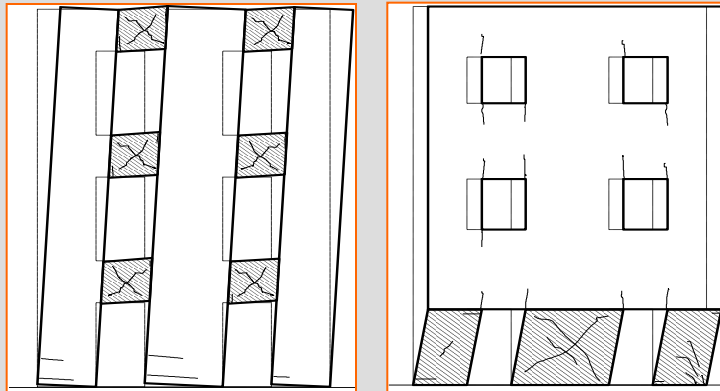
- LIMIT ANALYSIS – KINEMATIC APPROACH

- PUSH-OVER CURVE THROUGH NON LINEAR KINEMATIC ANALYSIS

$$\lambda = a_{\max} / g$$

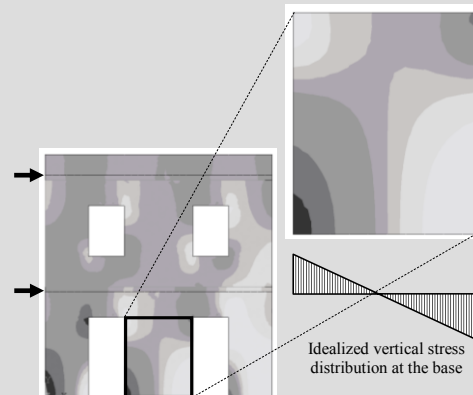
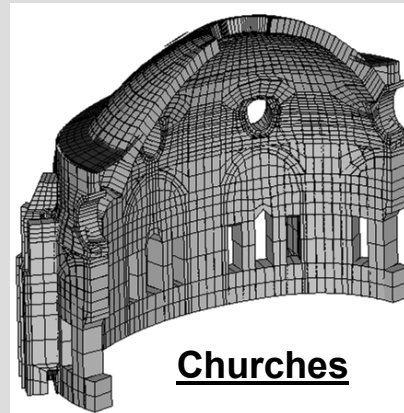


- TASK 5.2 – Modelling of global response of buildings

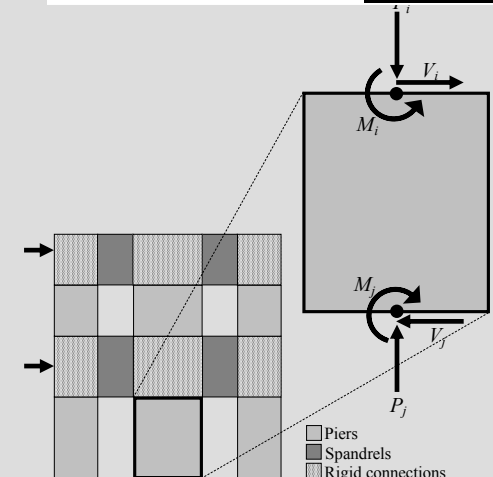
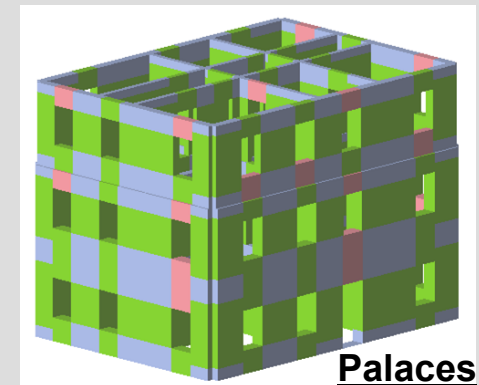


IN-PLANE MECHANISMS  
(2° failure mode)

## Finite element approach



## Structural element approach



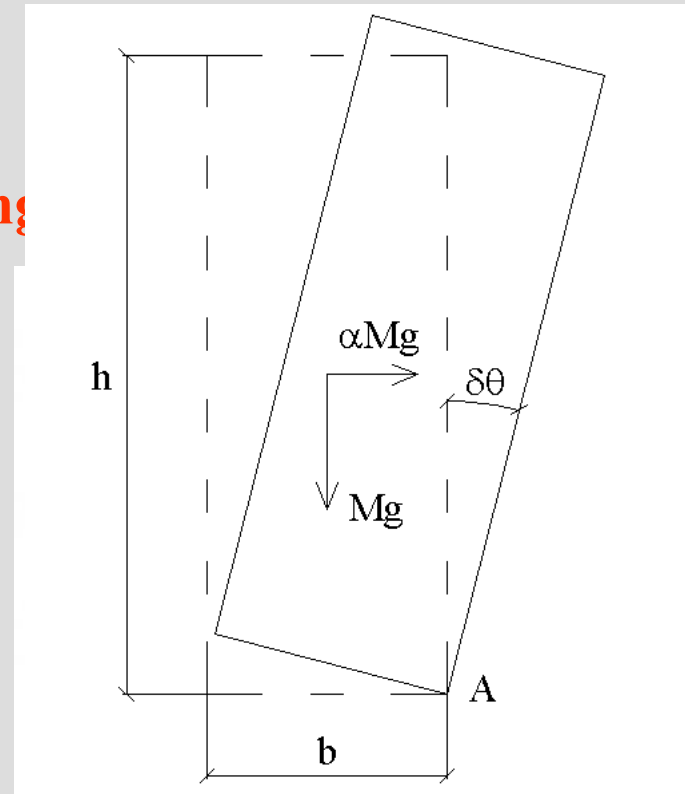
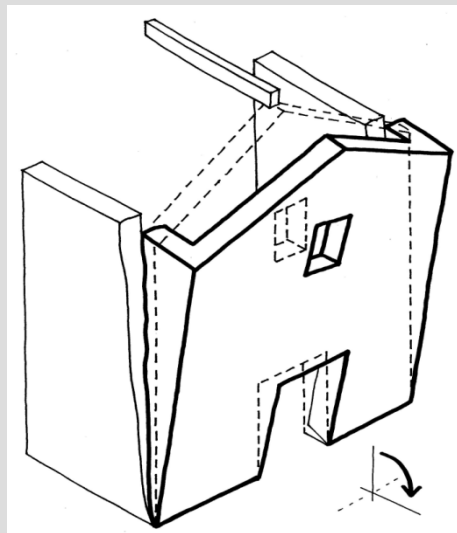
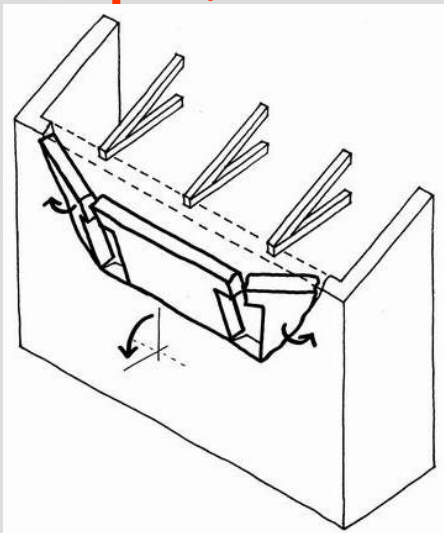
# SEISMIC LIMIT ANALYSIS

For the seismic evaluation by collapse limit analysis the following actions have to be considered:

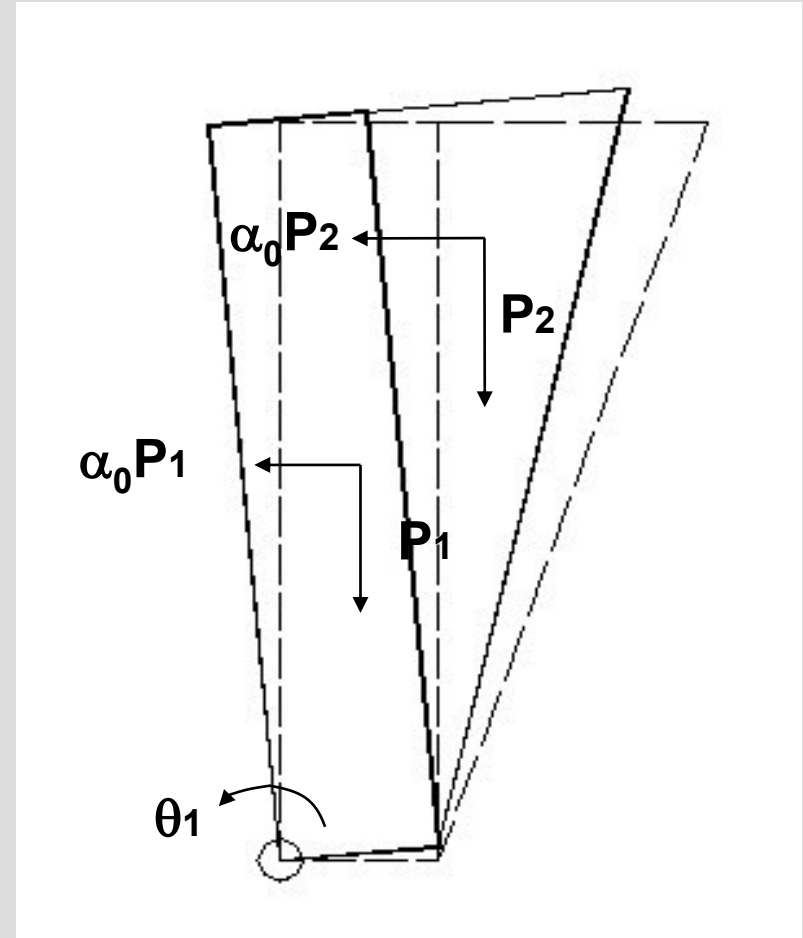
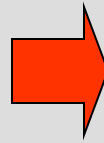
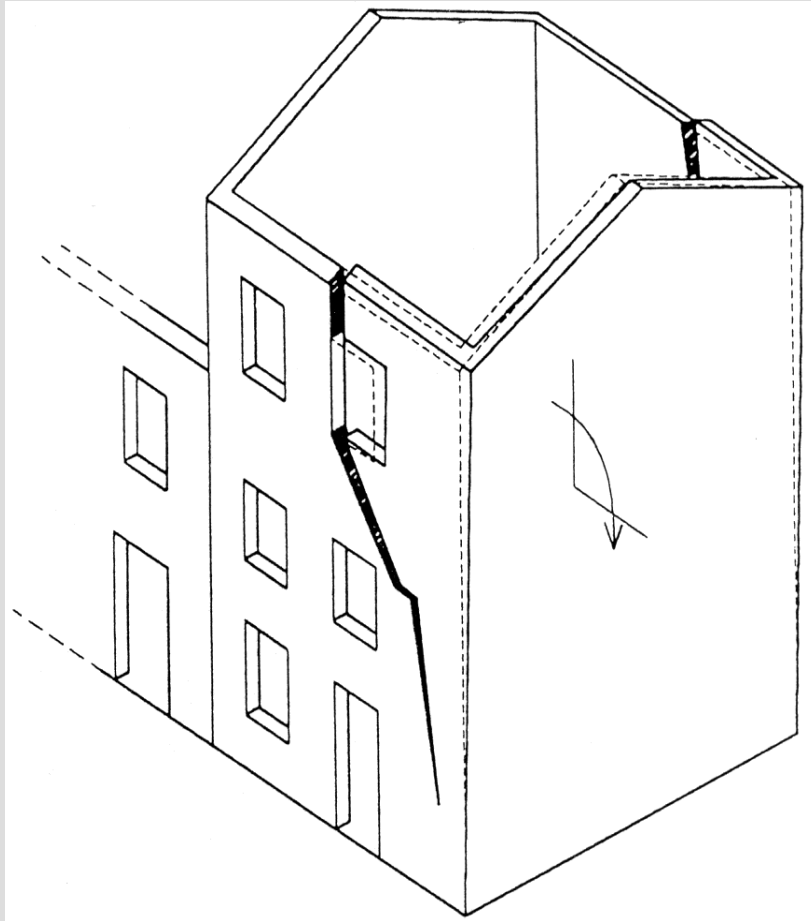
- dead loads
- applied external actions (tie rods, clamping with other structures)
- horizontal actions proportional to dead loads through the multiplier  $\lambda$ , representative of seismic actions

$$\lambda = a_{\max} / g$$

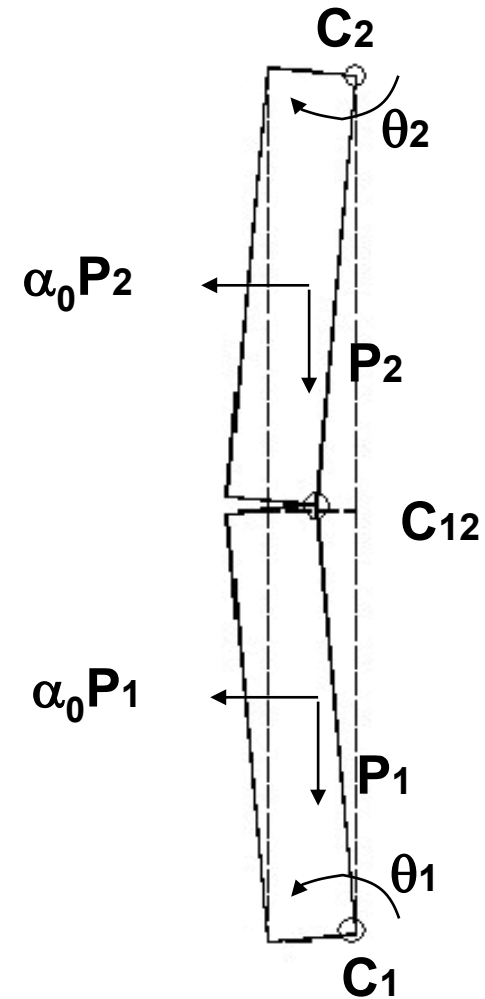
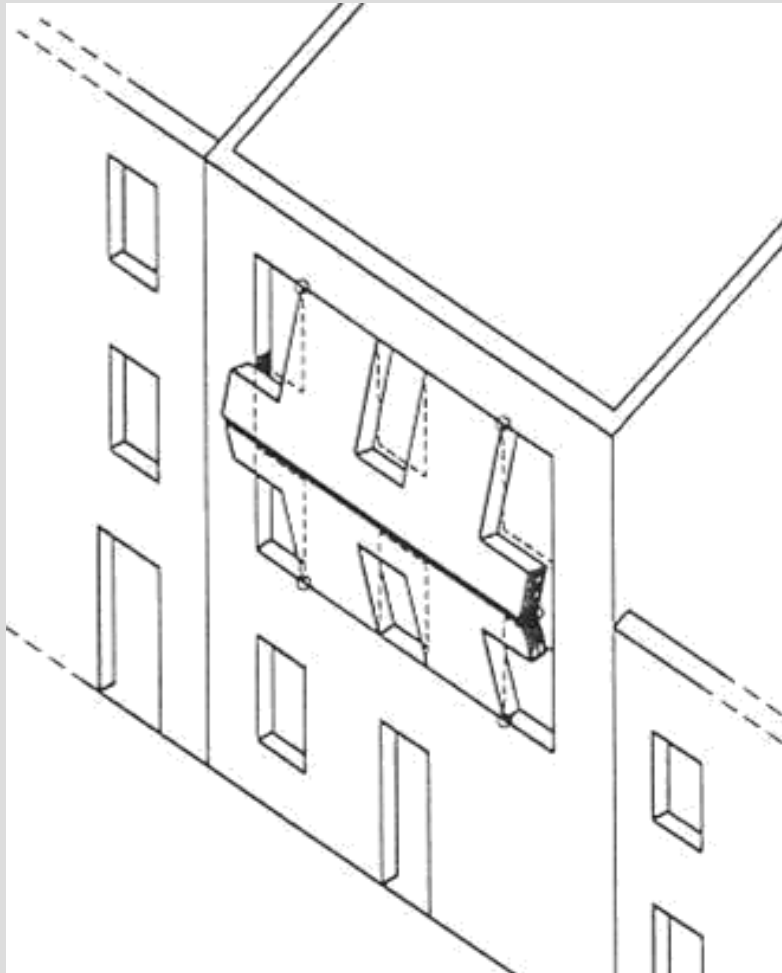
With the unsafe theorem, it is necessary to sing



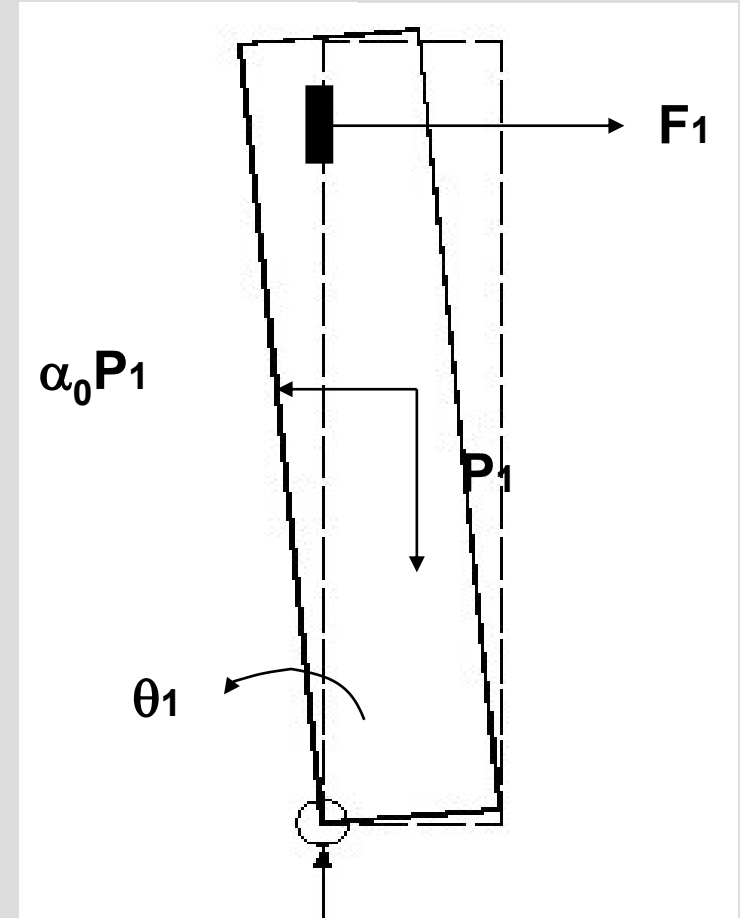
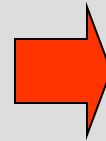
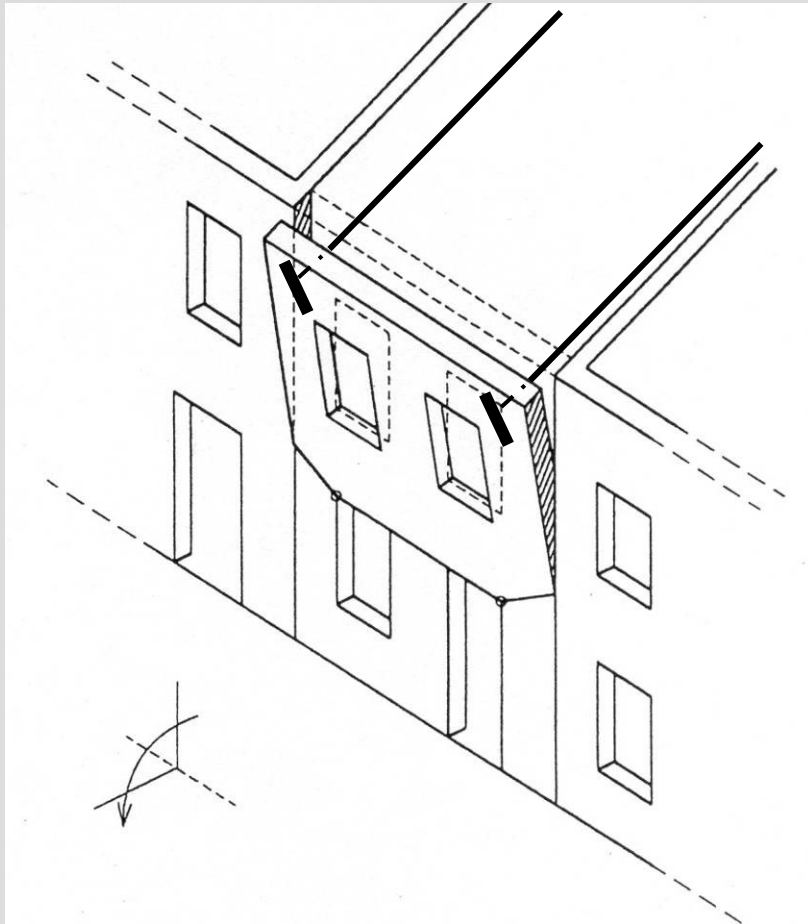




Overturning of a façade with good clamping to orthogonal walls



Local collapse mechanism in the case of stiff and heavy r.c. slab



Seismic strengthening by tie rods

$$\theta_2 = \theta_1 \frac{(y_B - y_A)(x_C - x_D) + (y_C - y_D)(x_A - x_B)}{(y_B - y_C)(x_C - x_D) + (y_C - y_D)(x_C - x_B)}$$

$$\theta_3 = \theta_1 \frac{(y_B - y_A)(x_C - x_B) + (y_C - y_B)(x_A - x_B)}{(y_D - y_C)(x_B - x_C) + (y_B - y_C)(x_C - x_D)}$$

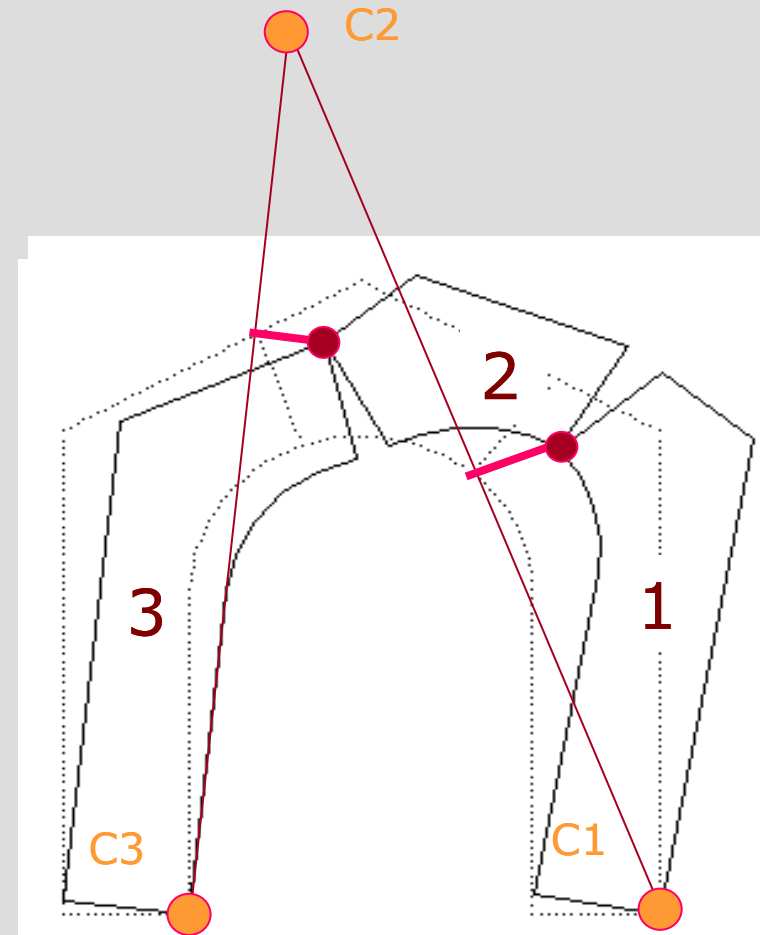
$$\Delta x_1 = \theta_1(y_A - y_1) \quad \Delta y_1 = \theta_1(x_1 - x_A)$$

$$\Delta x_2 = \theta_1(y_A - y_B) + \theta_2(y_B - y_2) \quad \Delta y_2 = \theta_1(x_B - x_A) + \theta_2(x_2 - x_B)$$

$$\Delta x_3 = \theta_3(y_D - y_3) \quad \Delta y_3 = \theta_3(x_3 - x_D)$$

$$\Delta l = \theta_3(y_A - y_3) - \theta_1(y_A - y_1)$$

$$\sum_{i=1}^3 P_i \Delta y_i - \alpha \sum_{i=1}^3 P_i \Delta x_i = T \Delta l$$





# The Basilica of St. Francesco d'Assisi – September 26<sup>th</sup>, 1997

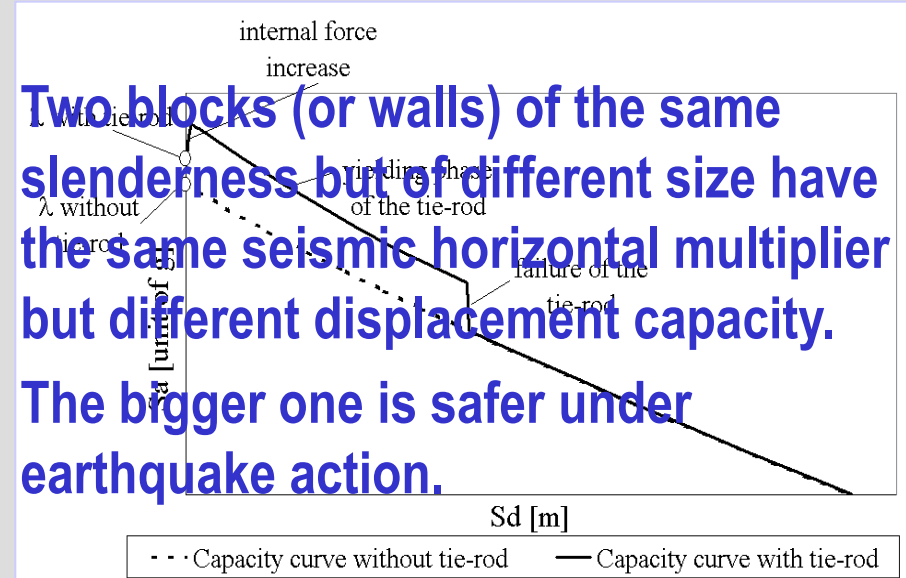
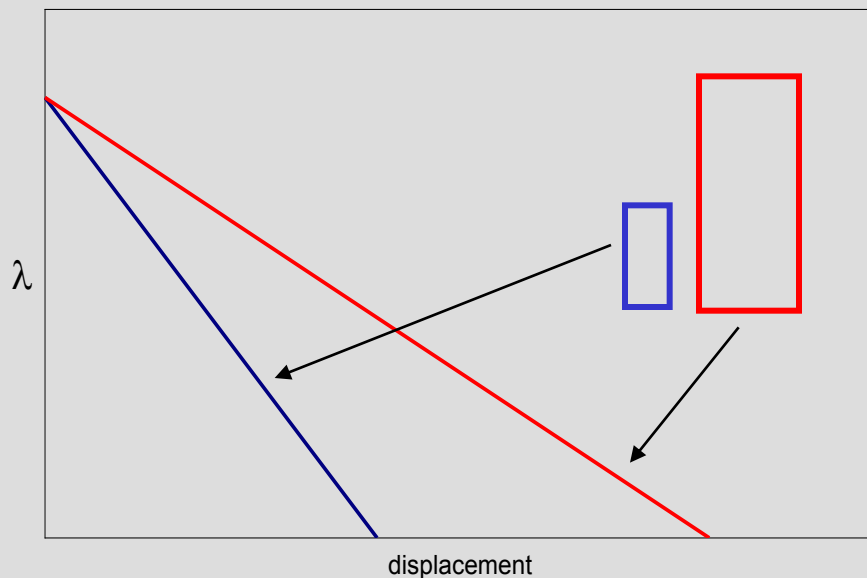
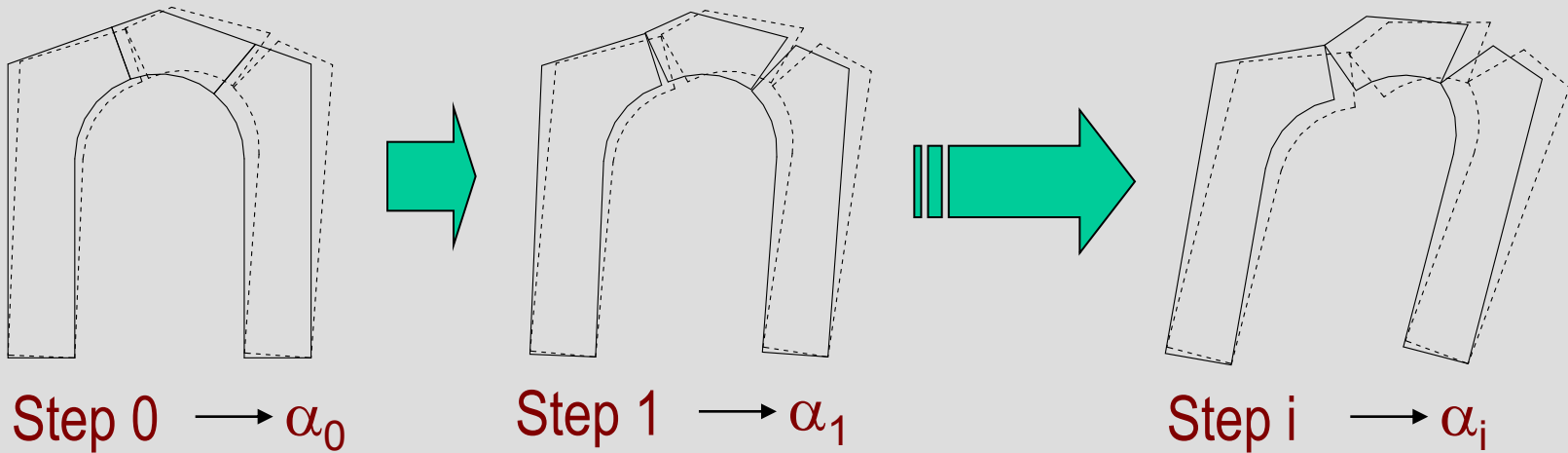






**TREMA Project – ENEA, DPC, University of Basilicata, ReLUIS**

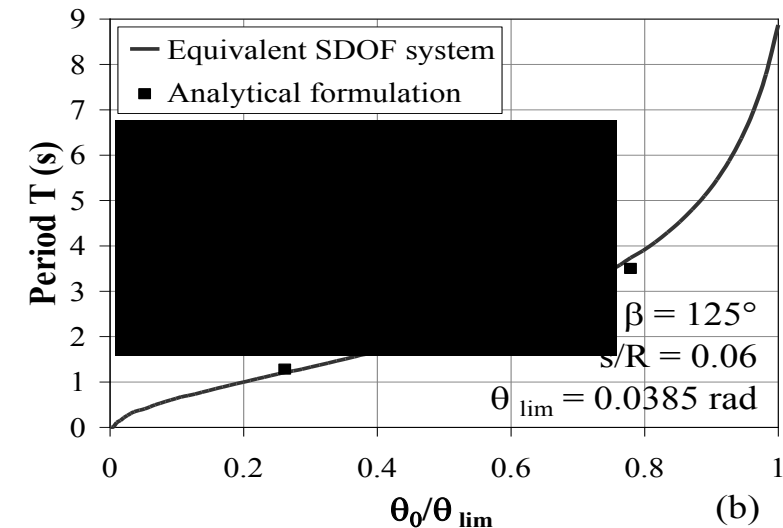
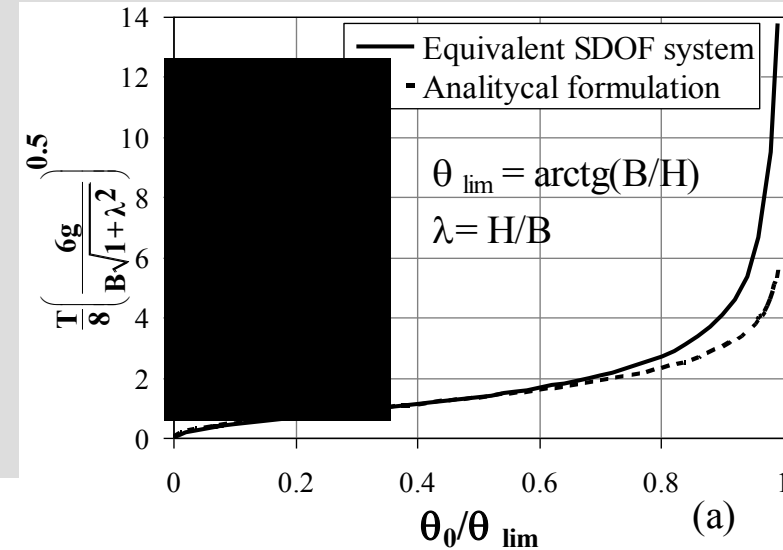
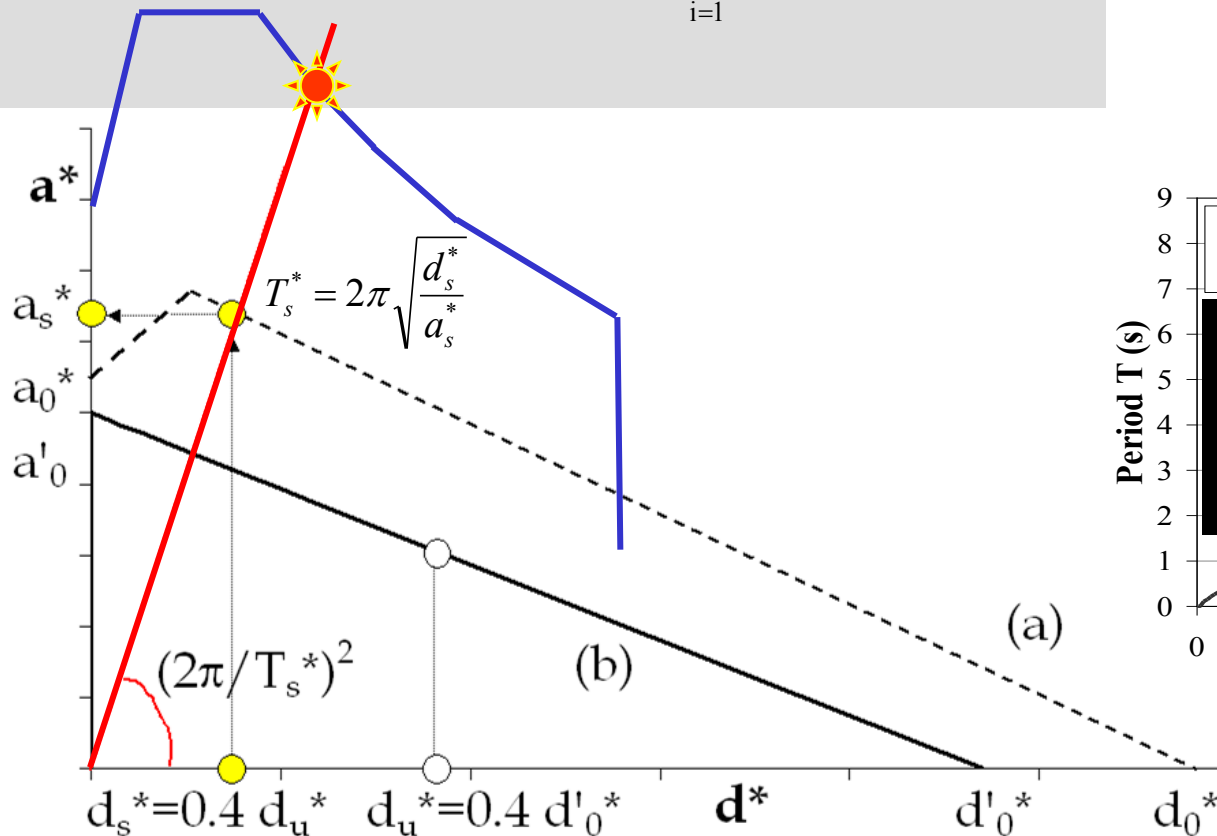
## Pushover curve by equilibrium limit analysis



**Two blocks (or walls) of the same slenderness but of different size have the same seismic horizontal multiplier but different displacement capacity. The bigger one is safer under earthquake action.**

## Conversion of pushover curve into a capacity spectrum

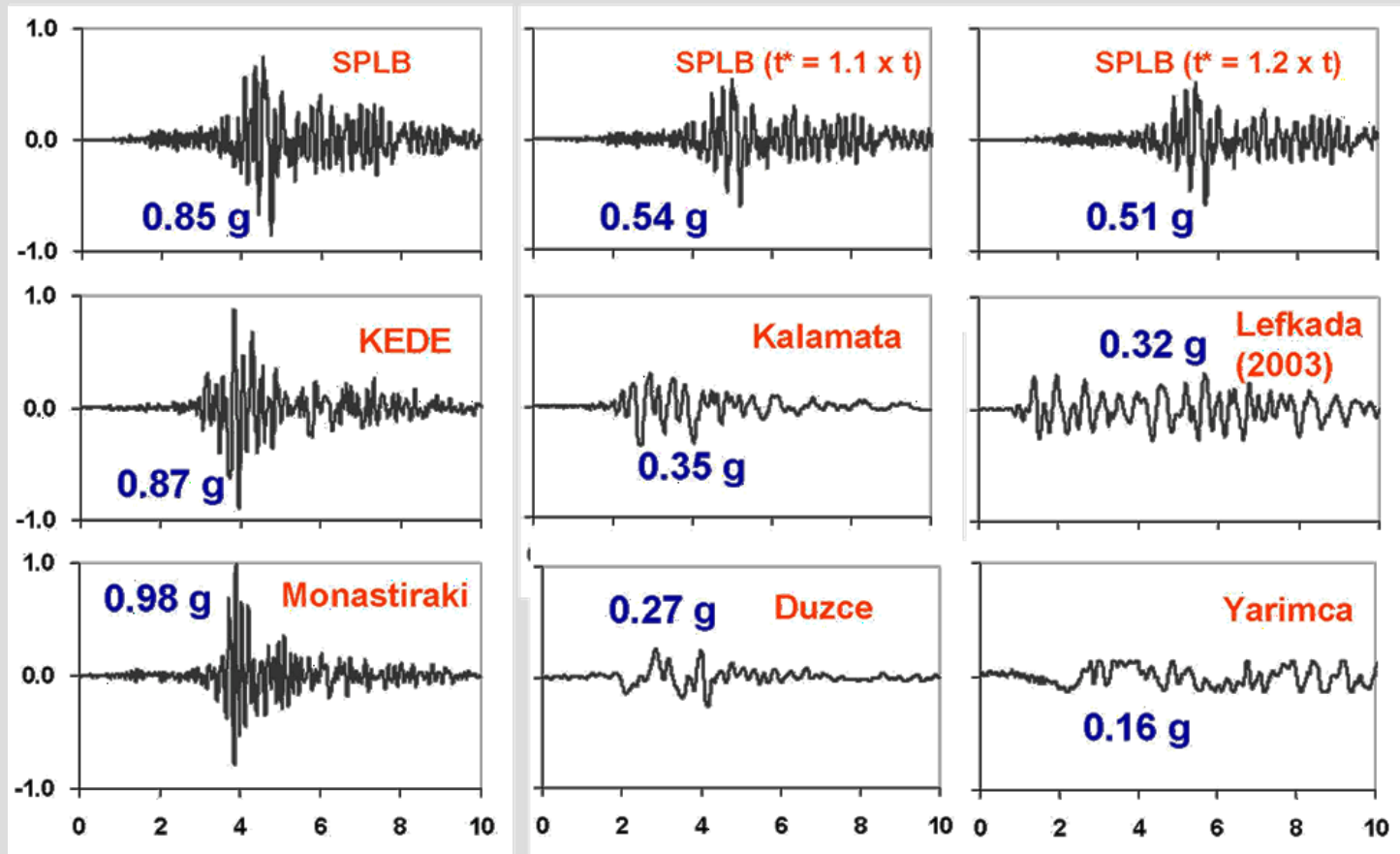
$$a^* = \frac{\alpha \sum_{i=1}^{n+m} P_i}{M^* FC} = \frac{\alpha g}{FC \cdot e^*} \quad d^* = d_k \frac{\sum_{i=1}^{n+m} P_i \delta_{x,i}^2}{\delta_{x,k} \sum_{i=1}^{n+m} P_i \delta_{x,i}}$$



Validation with reference solutions

# VALIDATION - Overturning of a block

## Non linear dynamic analysis of a rigid block (by Gazetas et al.)



$2b = 20 \text{ cm}$   
 $2h = 127 \text{ cm}$

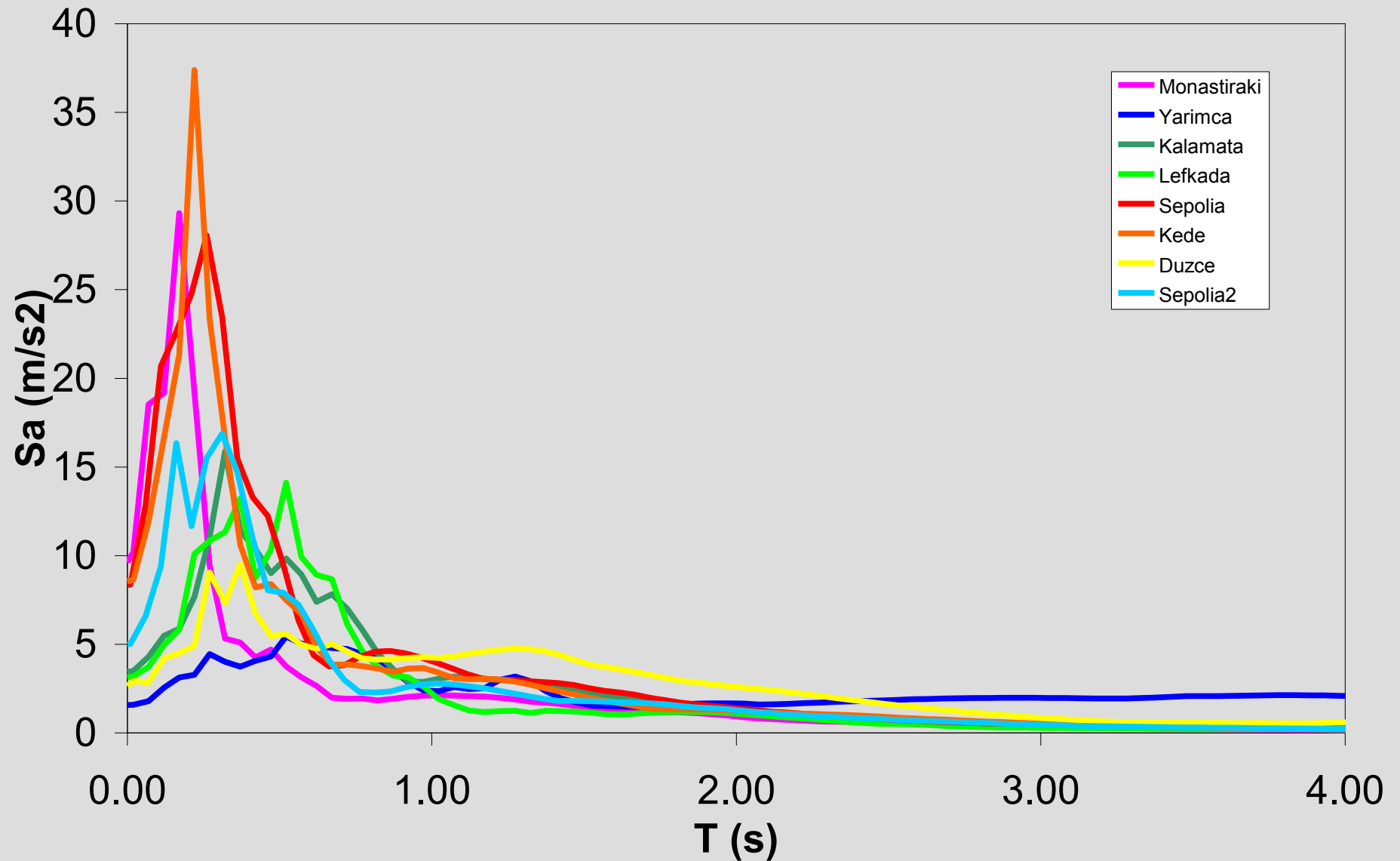
$\alpha = b/h = 0.16$

$$\delta = \ln \left( \frac{d_n}{d_{n+1}} \right) \quad \xi = \frac{\delta}{2\pi} = \frac{1}{2\pi} \ln \left( \frac{1}{c^2} \right)$$

Elastic response spectra (5% damping)

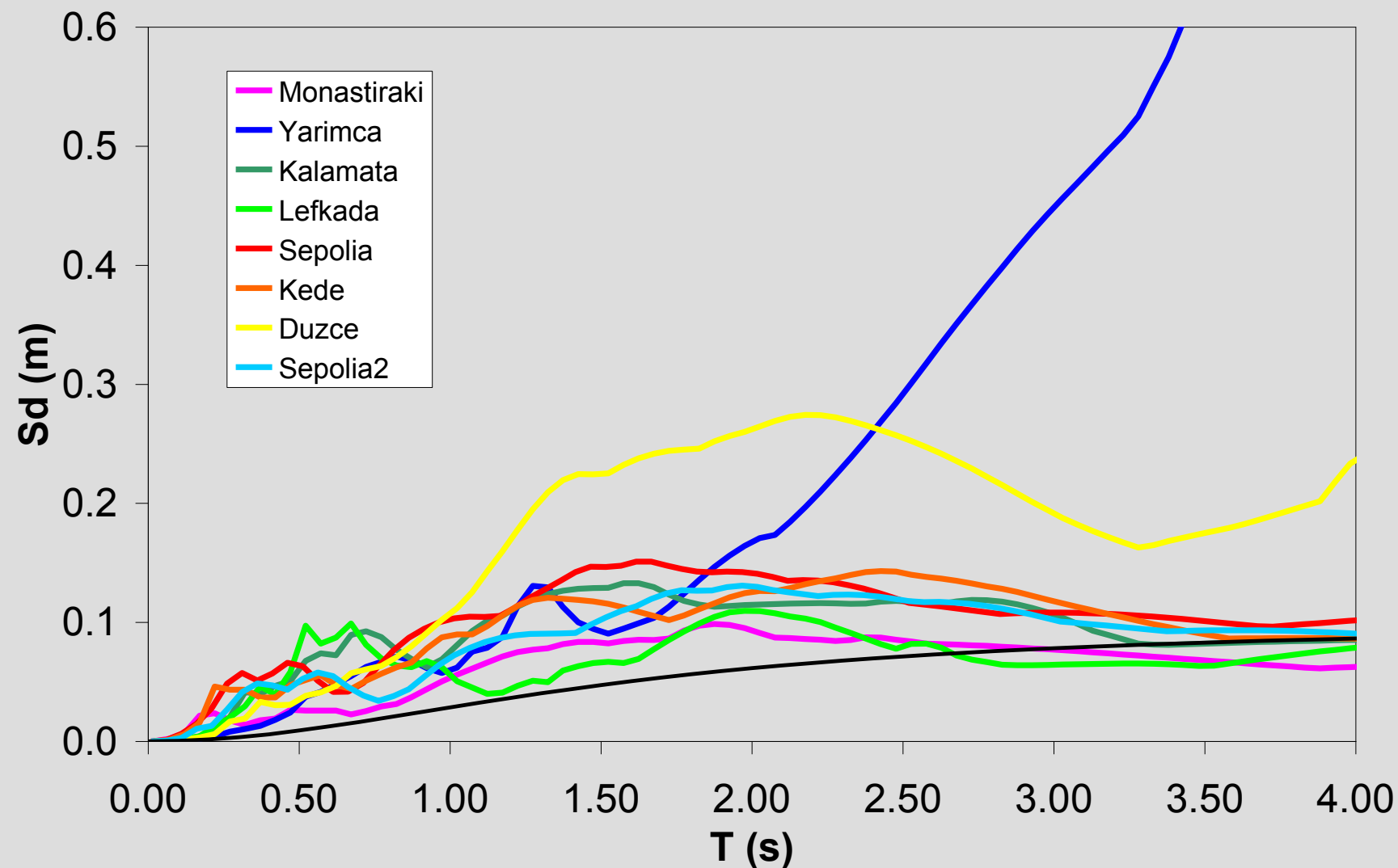
$c = 0.85 \quad \xi = 5.2\%$

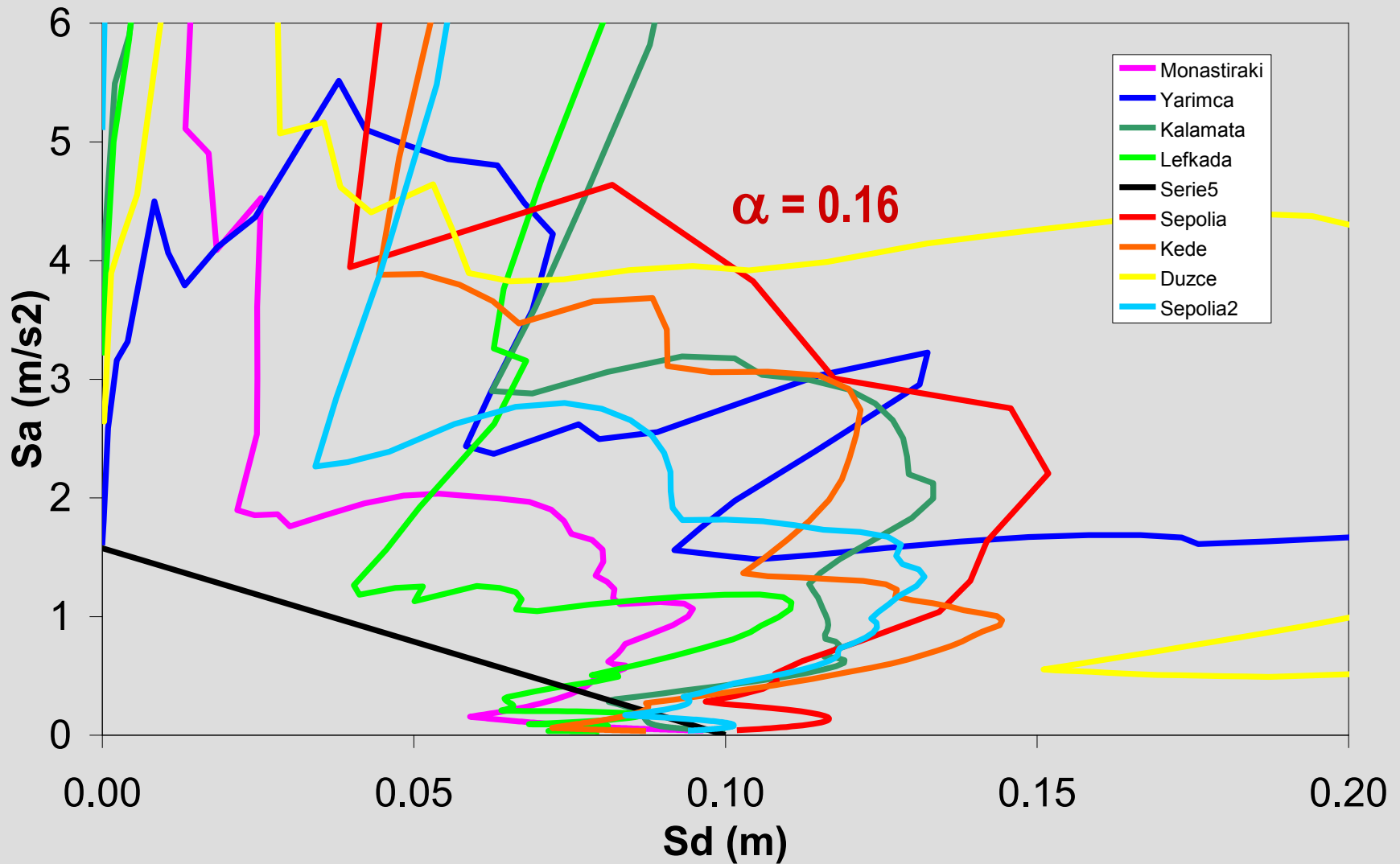
# Acceleration response spectra





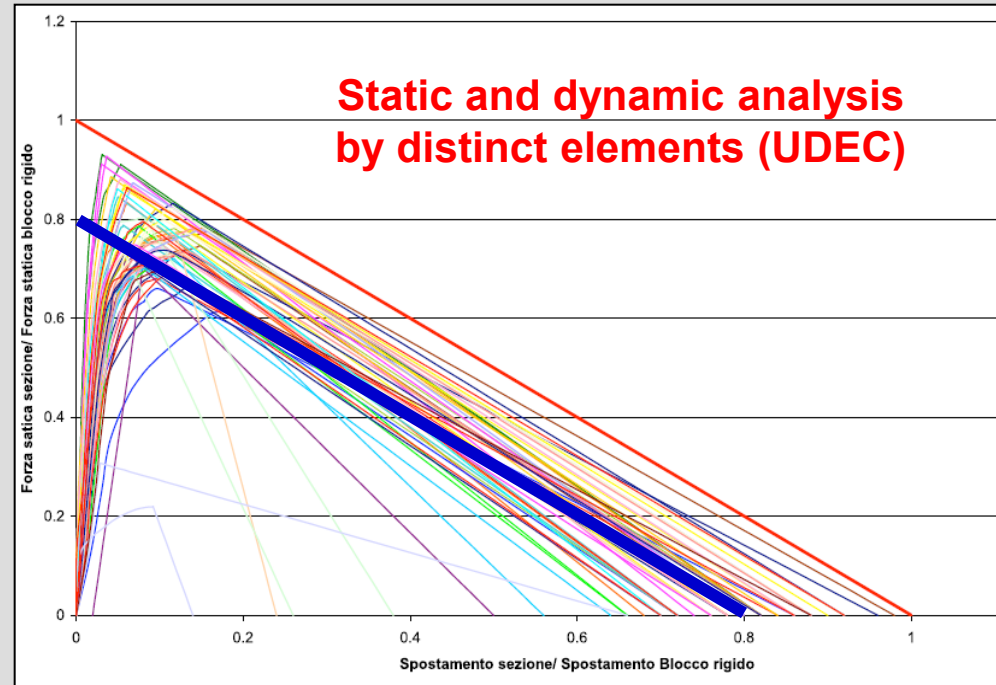
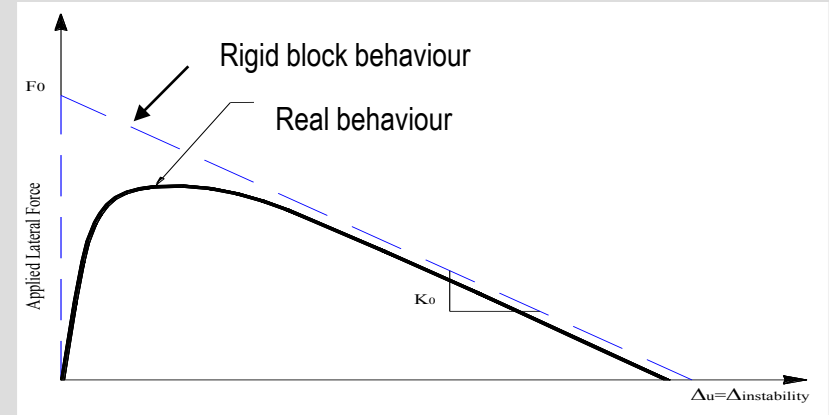
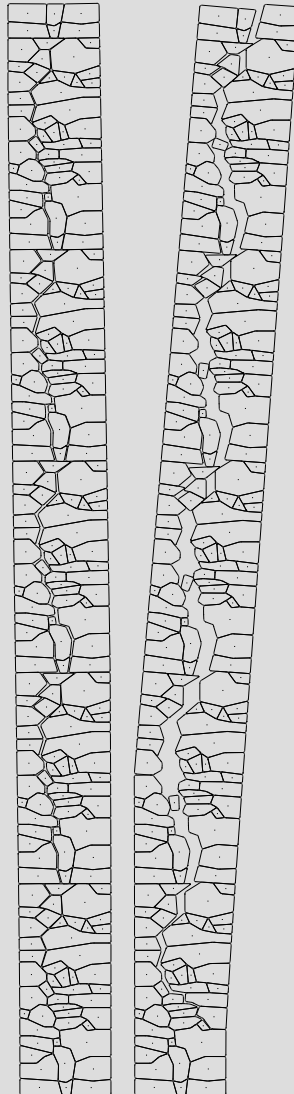
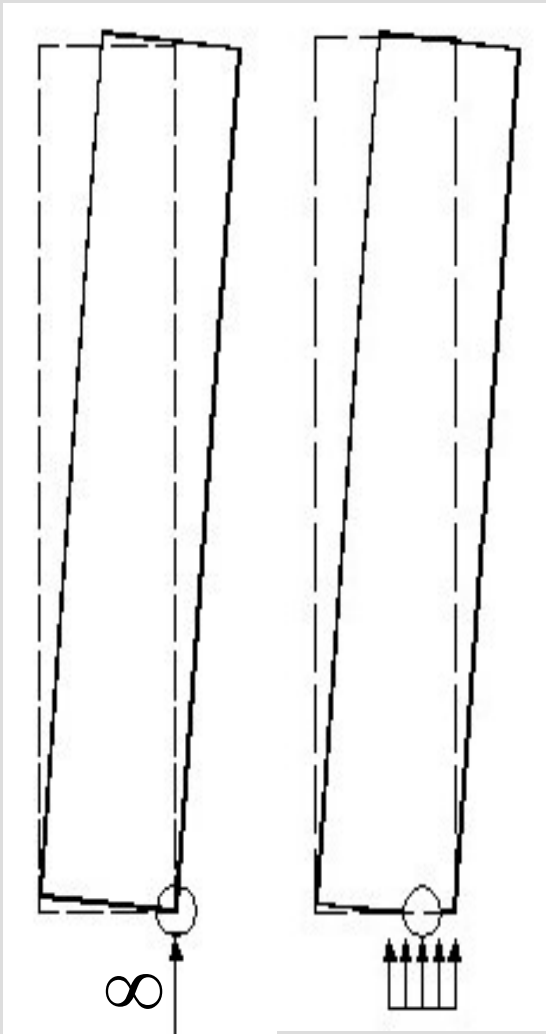
# Displacement response spectra



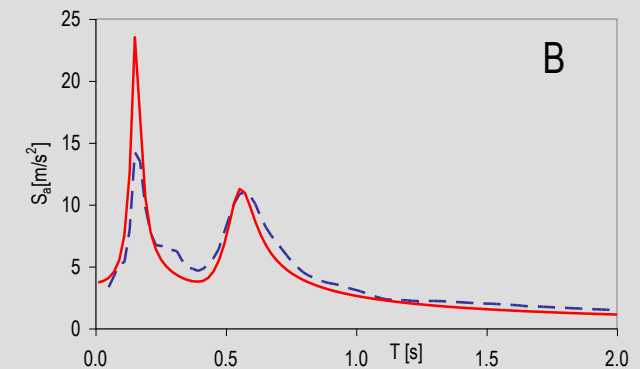
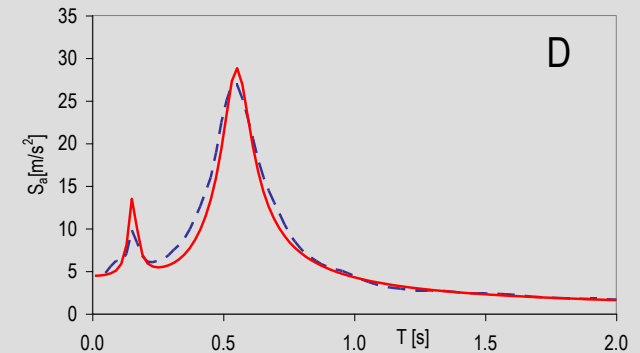
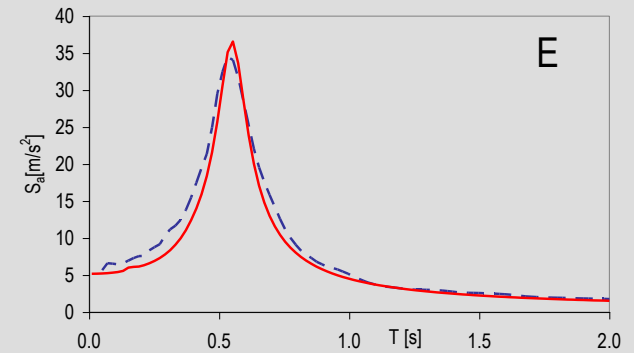
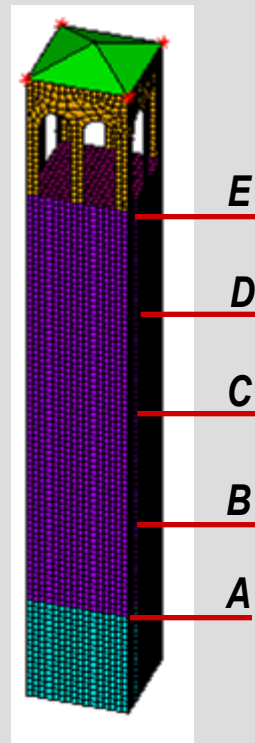
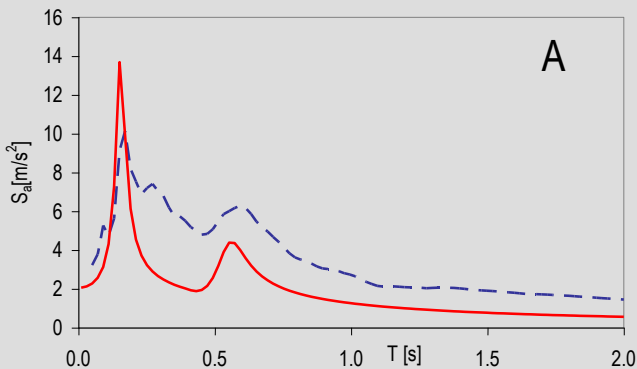
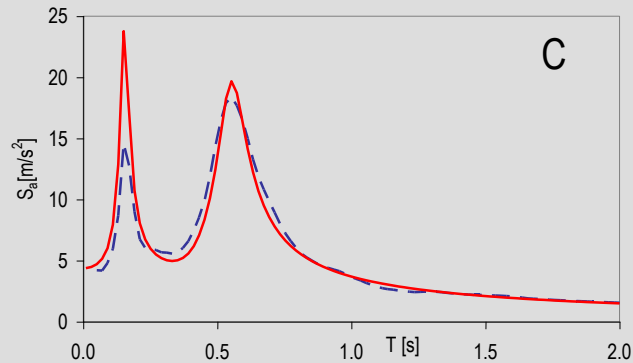


**All response spectra (in acceleration-displacement form) intersect the capacity curve for displacements values which are close to the ultimate displacement of the block. In the case of Yarimca earthquake, the acceleration is that producing the activation of rocking.**

## INFLUENCE OF THE QUALITY OF MASONRY



$$\Delta(T) = \sum_{r=1}^n \begin{cases} \frac{T^2}{T_r^2} \frac{\Delta_{h=0}(T_r) |\gamma_r \psi_r(z)|}{\sqrt{\left[1 - \left(\frac{T}{T_r}\right)^2\right]^2 + \frac{0.02}{\eta_D^2(\xi_s)} \left(\frac{T}{T_r}\right)}} & T \leq T_r \\ \frac{T^2}{T_r^2} \frac{\Delta_{h=0}(T_r) |\gamma_r \psi_r(z)|}{\sqrt{\left[1 - \left(\frac{T}{T_r}\right)^2\right]^2 + 0.02 \left(\frac{T}{T_r}\right)}} \cdot \eta_D(\xi_s) & T > T_r \end{cases}$$



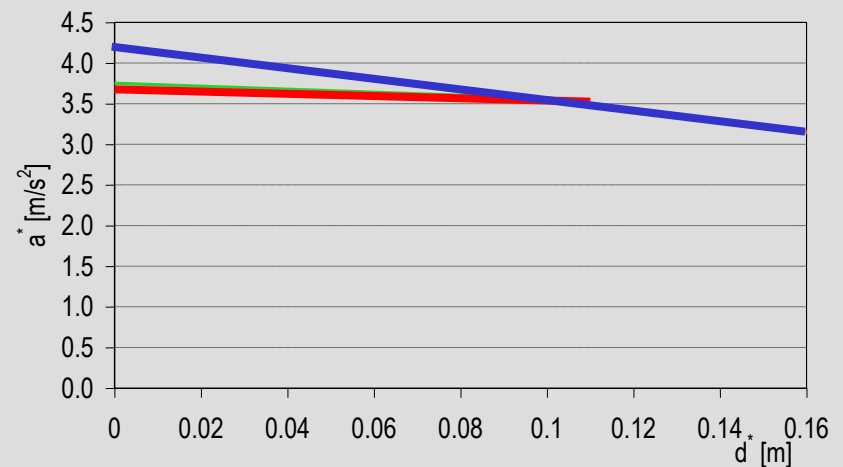
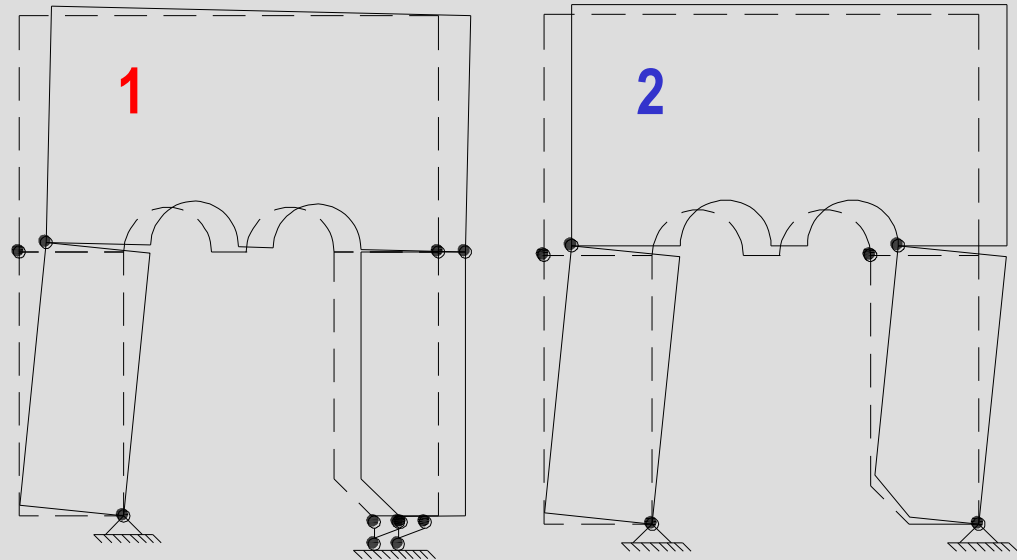
--- Numerical response spectra

— Simplified response spectra



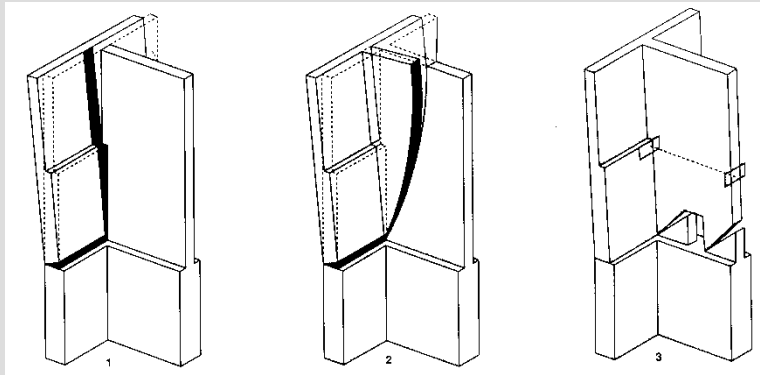


**Spilimbergo bell tower**  
**Friuli earthquake, 1976**

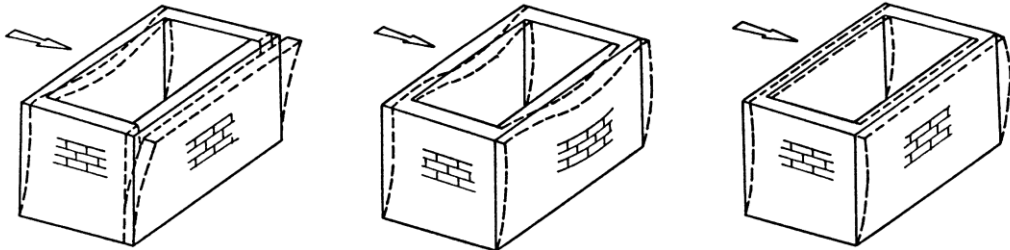


# SEISMIC BEHAVIOUR OF MASONRY BUILDINGS

The occurrence of out-of-plane mechanisms may be prevented by improving wall-wall and floor-wall connections (insertion of tie-rods, stiffening of floors, ..)

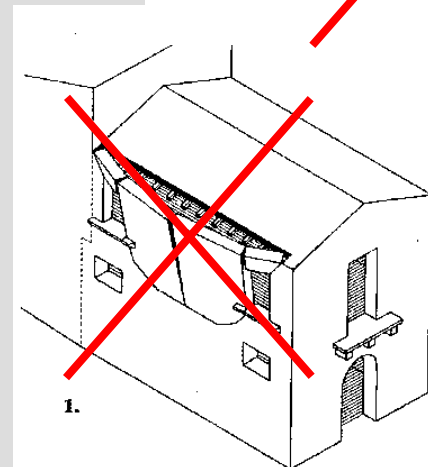
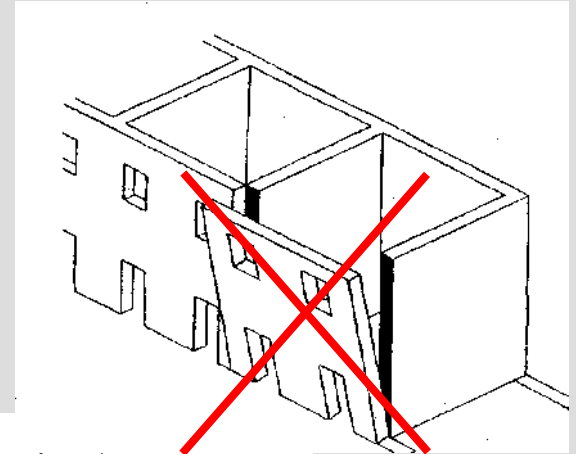


Effect of increasing quality of walls interlocking and insertion of tie-rods



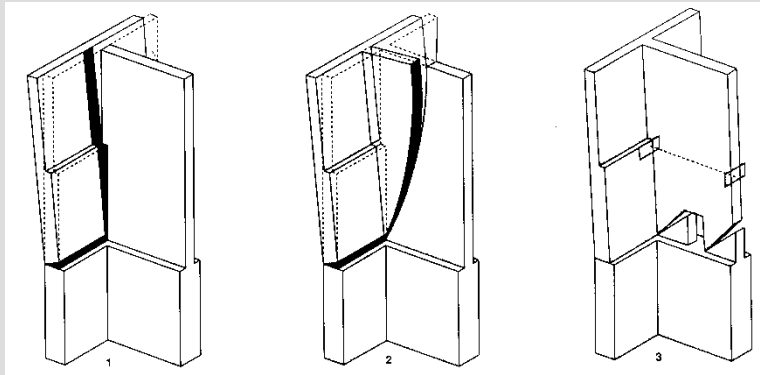
Effect of increasing quality of wall-floor connection and floor stiffening

## Examples of out-of-plane mechanisms

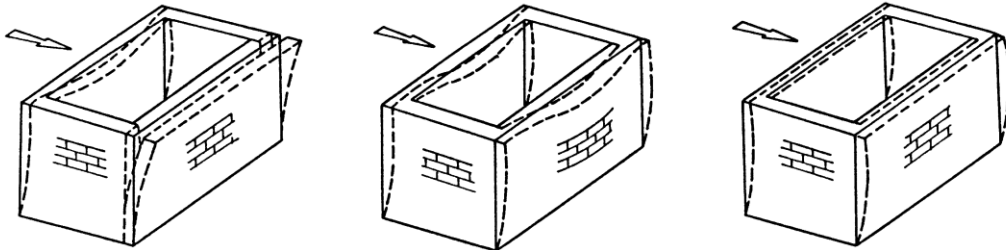


# SEISMIC BEHAVIOUR OF MASONRY BUILDINGS

The occurrence of out-of-plane mechanisms may be prevented by improving wall-wall and floor-wall connections (insertion of tie-rods, stiffening of floors, ..)

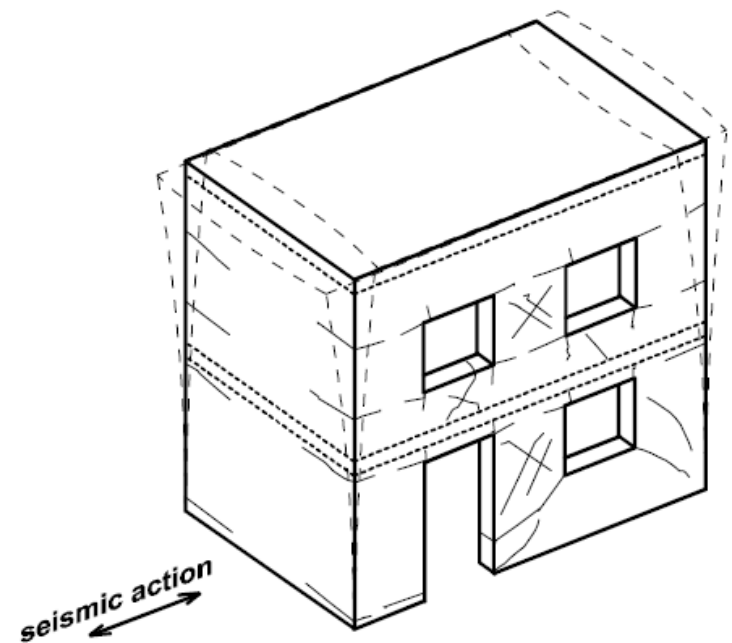


Effect of increasing quality of walls  
interlocking and insertion of tie-rods



Effect of increasing quality of wall-floor  
connection and floor stiffening

In-plane mechanisms:  
Global behaviour of the building



from Magenes 2007 (Proc. of 1<sup>th</sup> ECEES)



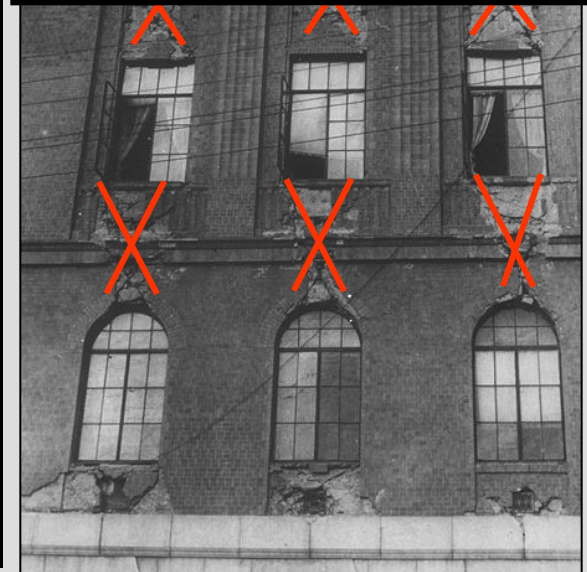
# STRUCTURAL ELEMENTS IN MASONRY WALLS



**PIERS**

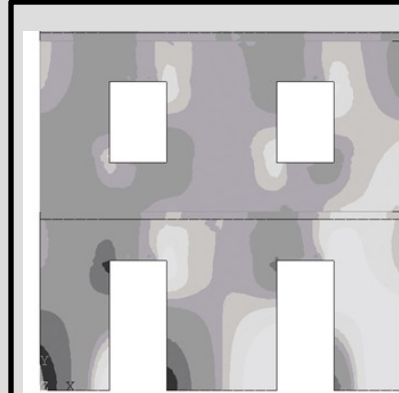
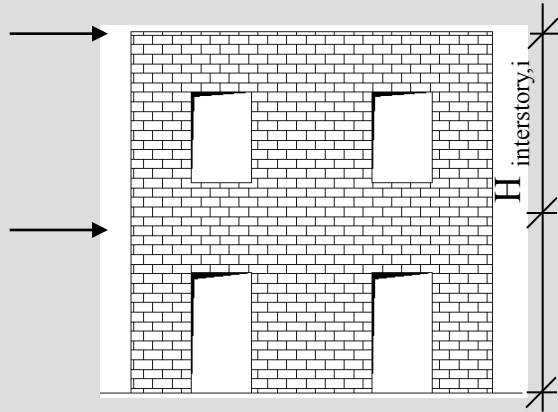


**SPANDRELS**





# MODELLING STRATEGIES



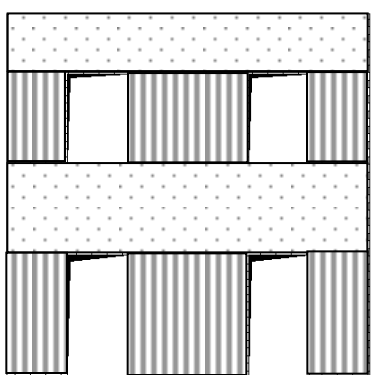
## DISCRETIZATION OF THE WALL BY FINITE ELEMENTS

Lofti and Shing 1991, Gambarotta and Lagomarsino 1997, Lourenço et al. 1997, Lourenço and Rots 1997, Luciano and Sacco 1997, Zhuge et al. 1998, Pietruszczak and Ushaksaraei 2003, Massart 2003, Schlegel 2004, Calderini and Lagomarsino 2008

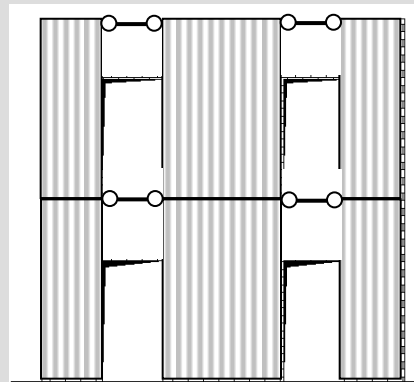
## SIMPLIFIED MODELS

(as proposed in FEMA 356 – FEMA 306 – POR Method)

### STRONG SPANDREL – WEAK PIER

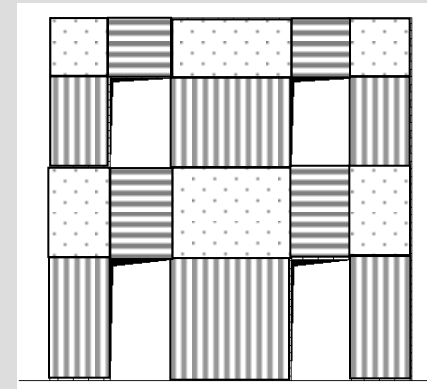


### WEAK SPANDREL – STRONG PIER

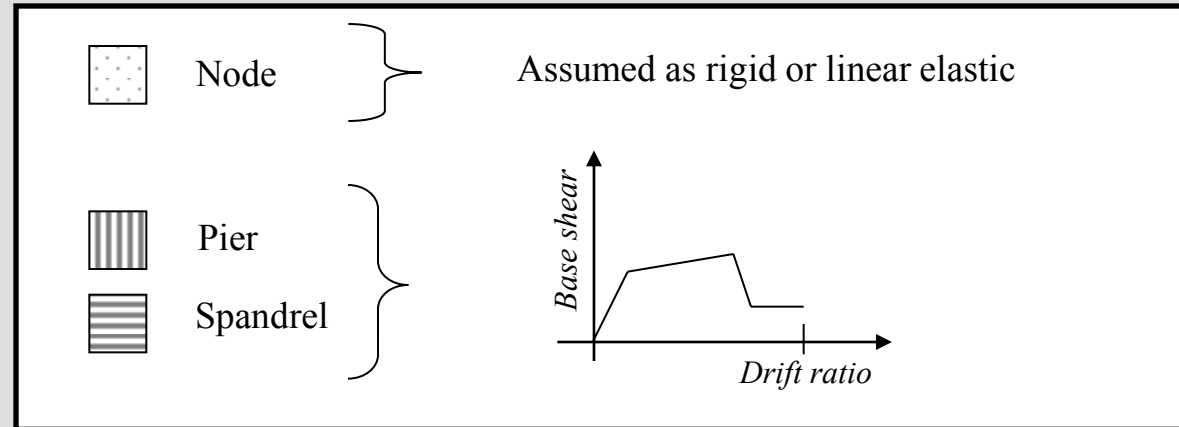
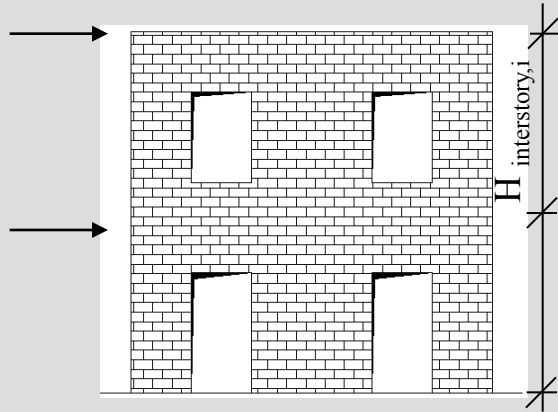


## EQUIVALENT FRAME MODEL

(Tomažević and Weiss 1990, D'Asdia and Viskovic 1995, Brencich and Lagomarsino 1998, Magenes and Della Fontana 1998, Galasco et al. 2004)



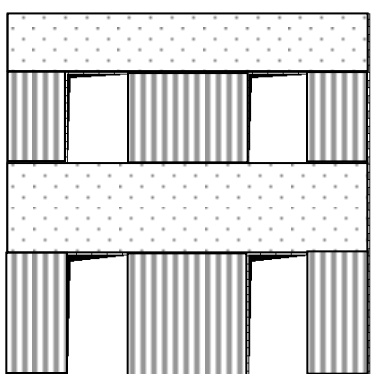
# MODELLING STRATEGIES



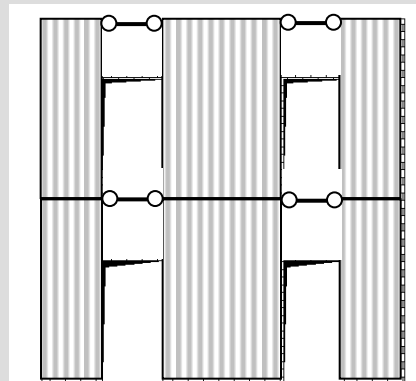
## SIMPLIFIED MODELS

(as proposed in FEMA 356 – FEMA 306 – POR Method)

### STRONG SPANDREL – WEAK PIER

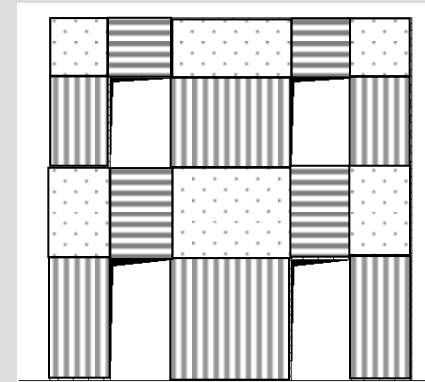


### WEAK SPANDREL – STRONG PIER

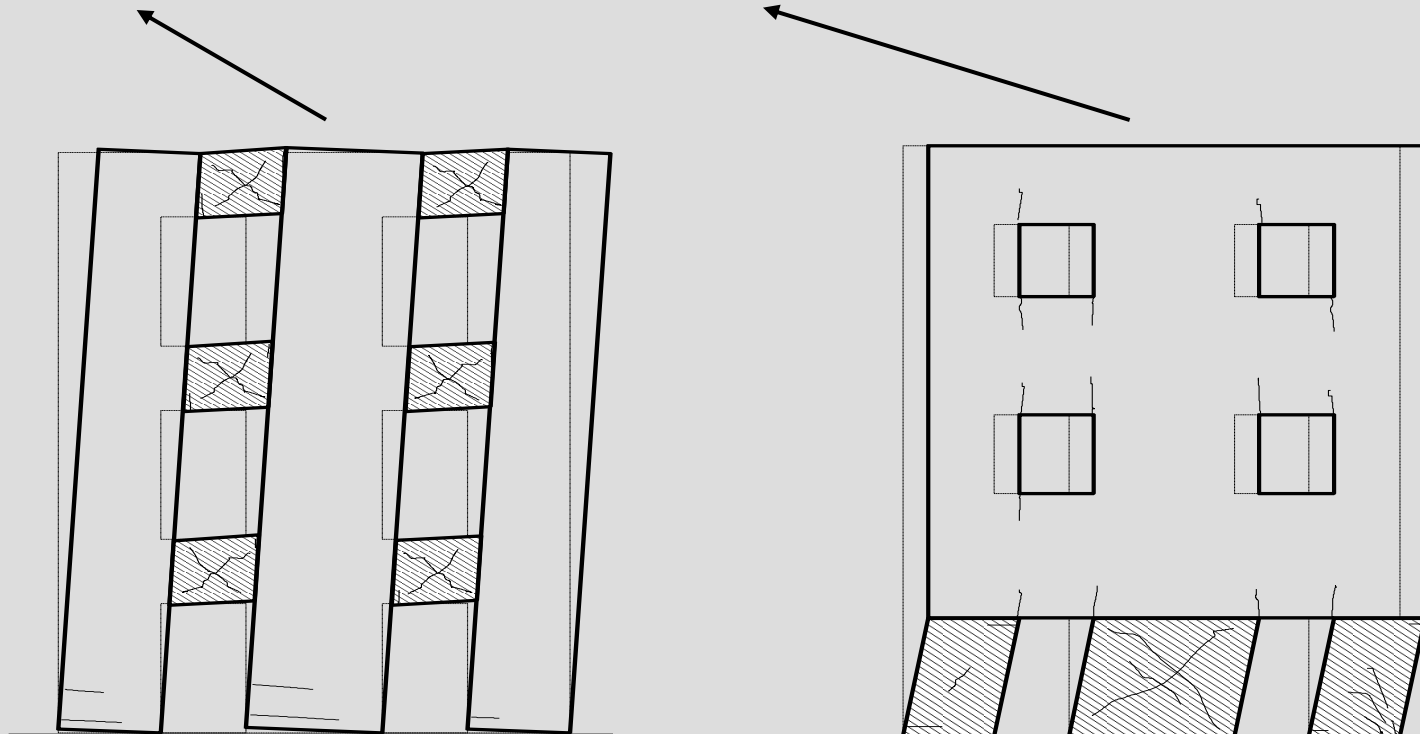
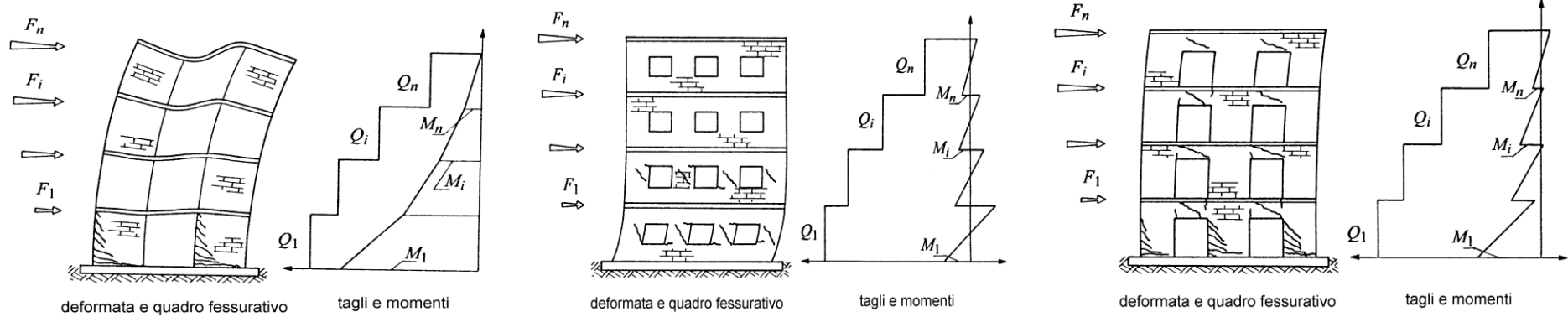


## EQUIVALENT FRAME MODEL

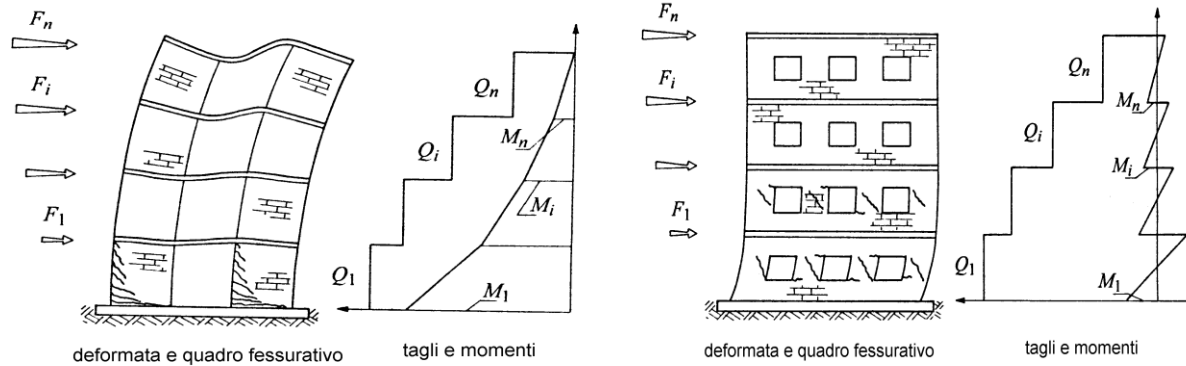
(Tomažević and Weiss 1990, D'Asdia and Viskovic 1995, Brencich and Lagomarsino 1998, Magenes and Della Fontana 1998, Galasco et al. 2004)



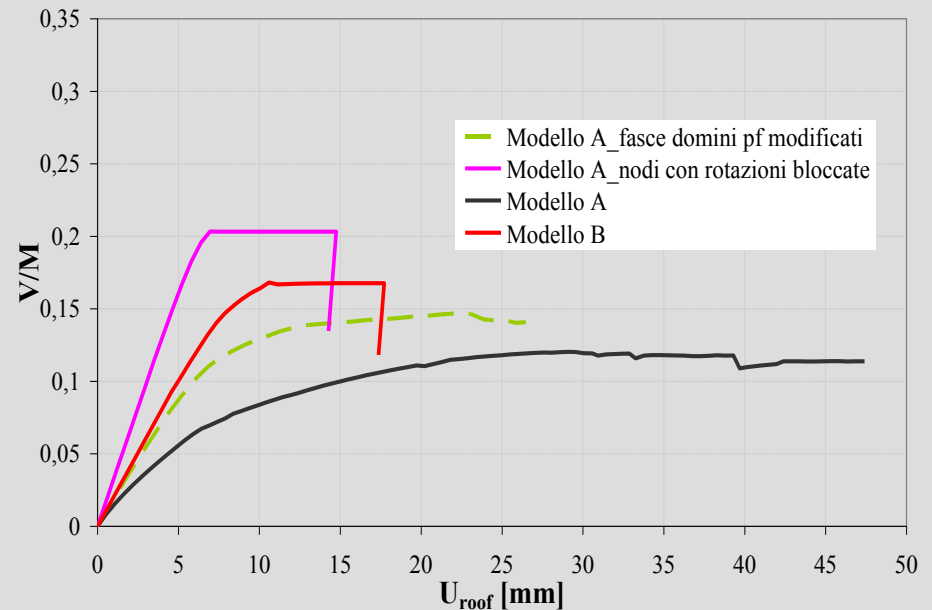
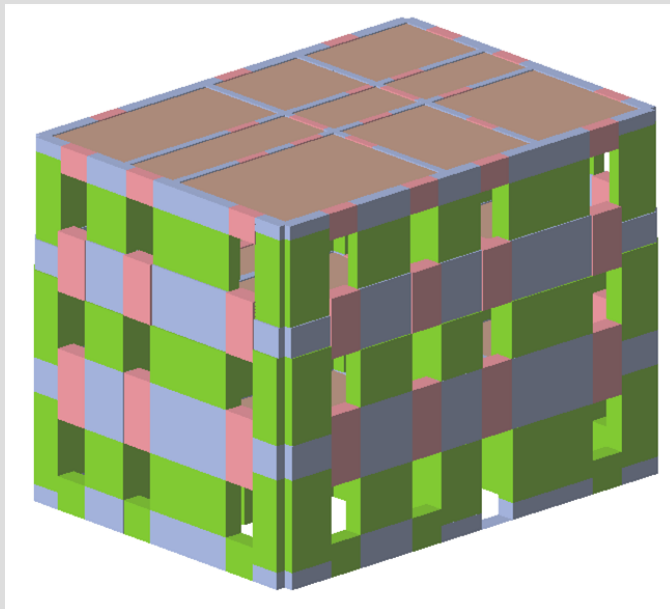
# NON LINEAR PUSHOVER ANALYSIS



# NON LINEAR PUSHOVER ANALYSIS



**TREMURI Program** (ask to [tremuri@gmail.com](mailto:tremuri@gmail.com) – commercial release: [www.stadata.com](http://www.stadata.com))  
3D modelling of masonry buildings by the equivalent frame model.

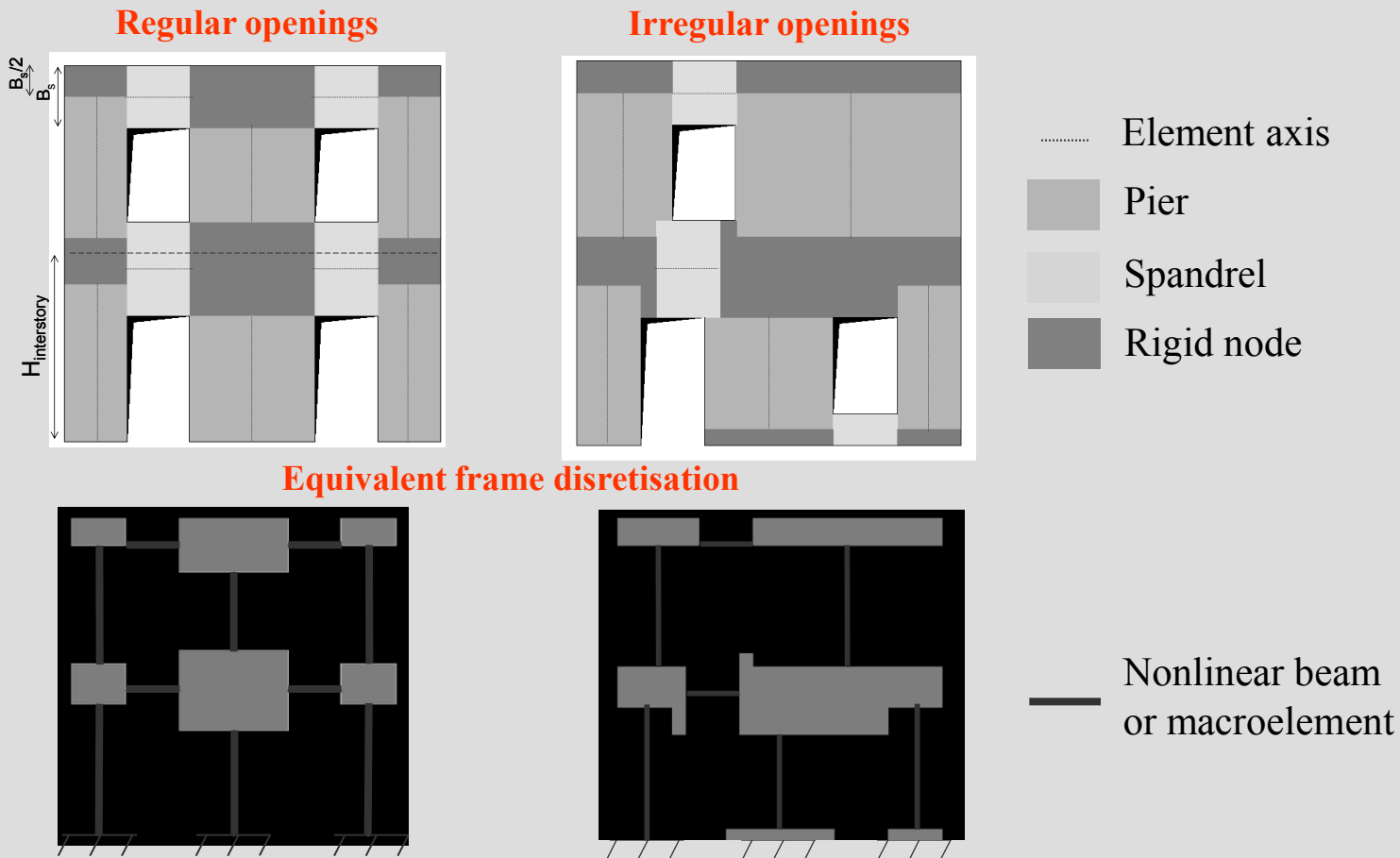




# DISCRETISATION OF THE WALL IN AN EQUIVALENT FRAME MODEL

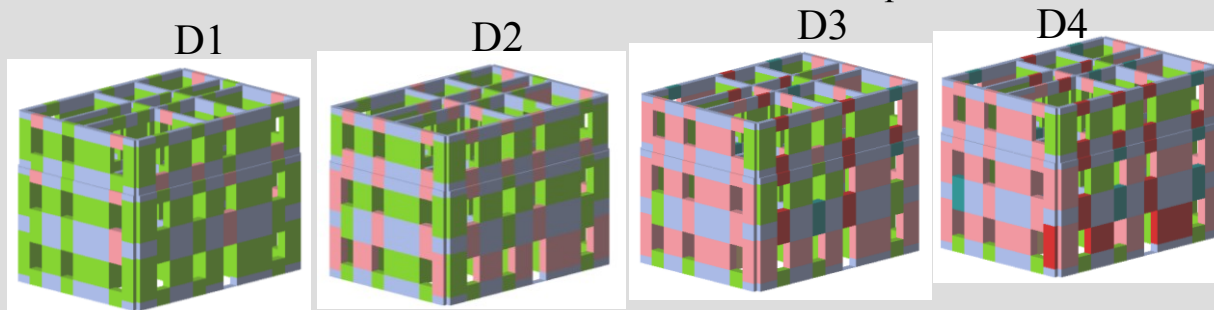
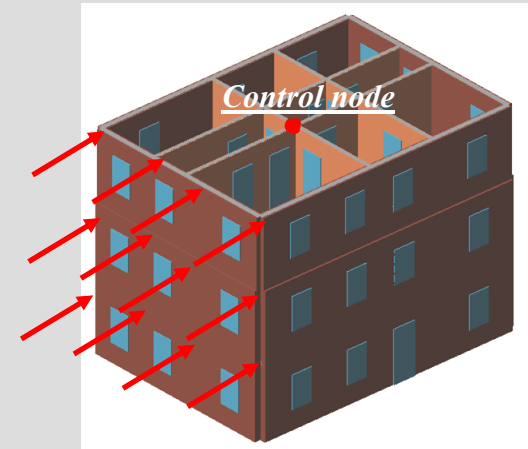
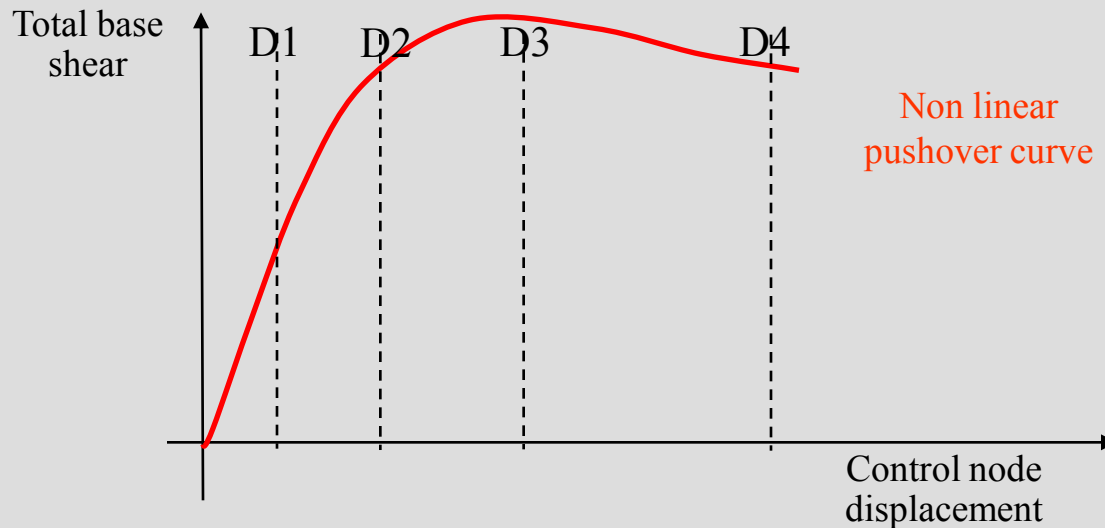
## Identification of the geometry of piers, spandrels and rigid nodes

- ✓ Conventional criteria are assumed in the literature, validated by damage observation after earthquakes and by experimental campaigns (e.g. Benedetti et al., 1998; Calvi and Magenes, 1994; Yi et al., 2006).
- ✓ These criteria are based on: empirical rules based on opening distribution; conventional stresses diffusion; pattern of existing cracks (in case of existing buildings)



# SEISMIC ANALYSIS METHODS AND VERIFICATION CRITERIA

## ■ NON LINEAR STATIC ANALYSIS



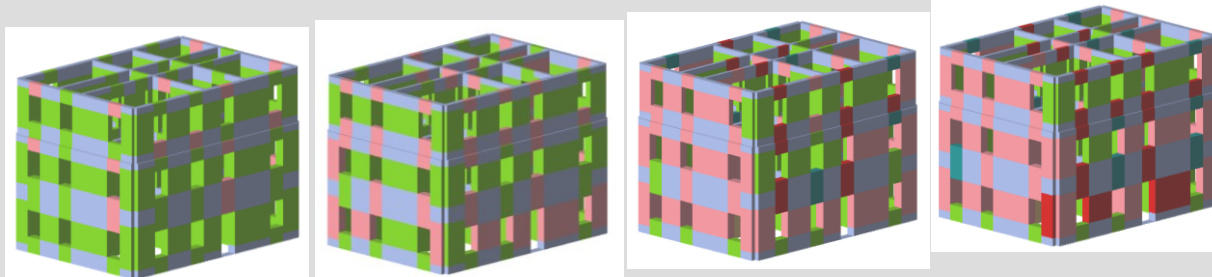
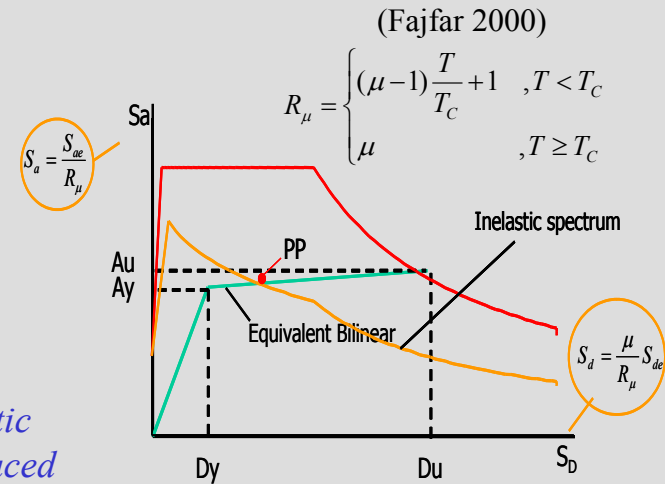
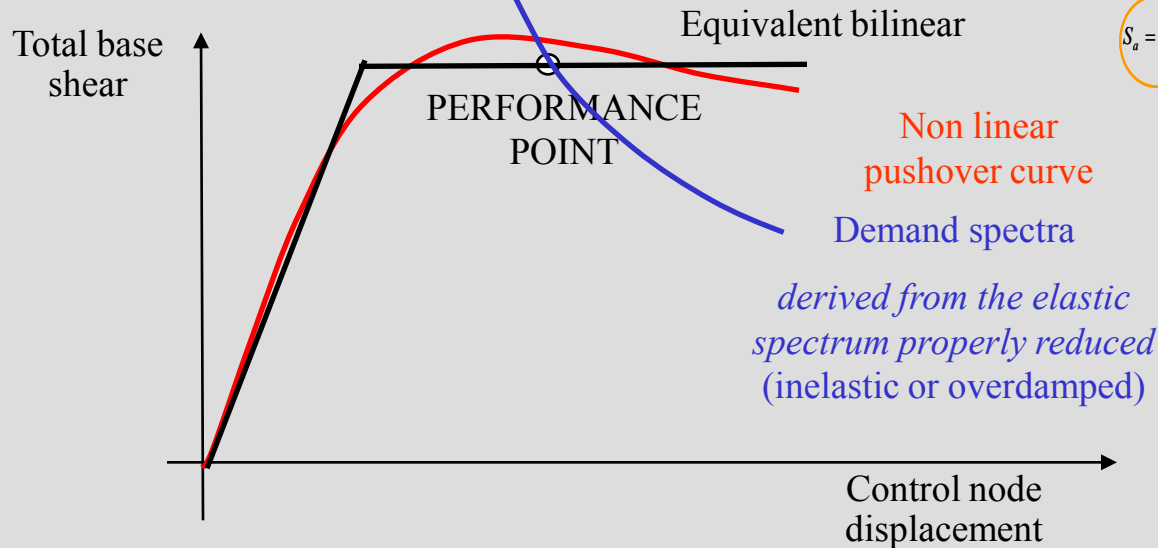
- Panel in elastic phase
- Damage state of panel
- Panel at collapse

Progressing of non linear response and the damage state of building

Usually just from the beginning of incremental analysis a non linear response occurs (with damage concentration in spandrels)

# SEISMIC ANALYSIS METHODS AND VERIFICATION CRITERIA

## ■ NON LINEAR STATIC ANALYSIS

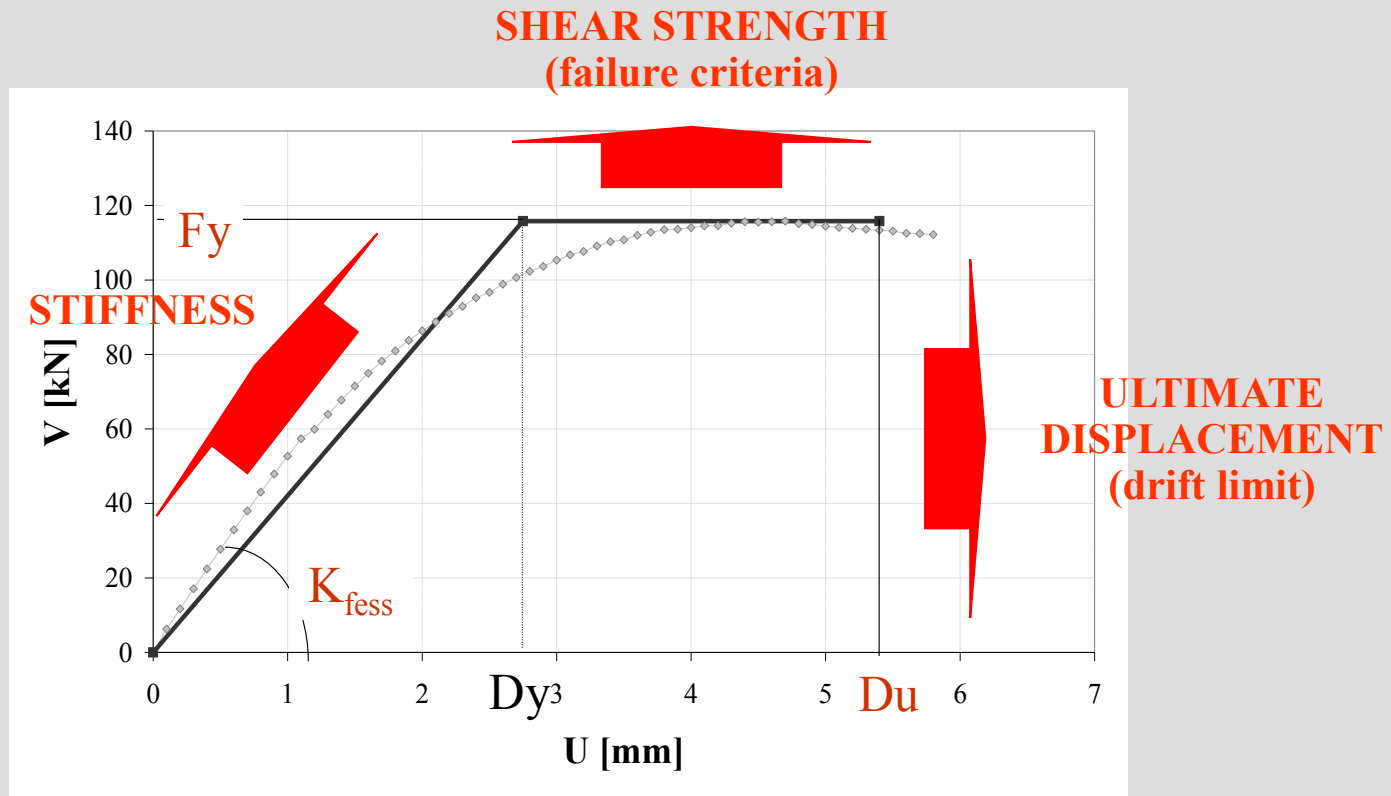


Progressing of non linear response and the damage state of building

Usually just from the beginning of incremental analysis a non linear response occurs (with damage concentration in spandrels)

# FORCE – DISPLACEMENT RELATION IN SHEAR

- Laboratory tests on masonry panels (cyclic raking tests) are well simulated by TREMURI macroelement. The force-displacement curve in shear presents a curvilinear trend, with an ultimate displacement (drift limit) depending on softening or brittle failure.
- Different failure modes can occur: **Rocking** and **Crushing** (flexural behaviour); **Sliding** and **Diagonal Cracking** (shear behaviour).
- The curve may be approximated by a bilinear curve, defined by three parameters.





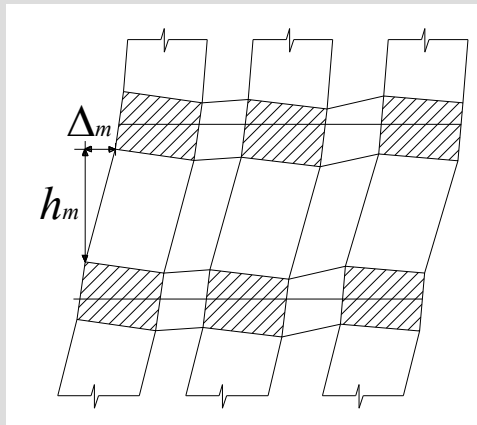
# 3MURI – NON LINEAR BEAM

## ■ Stiffness properties

A secant stiffness may be defined, but this is an approximation, as it is not possible to know in advance the actual stiffness degradation in each element.

Eurocode 8 and the new Italian code propose to adopt for the panel a reduced initial elastic stiffness of the beam; usually, unless specific information are available, a reduction of 50% is proposed.

## ■ Ductility control in terms of drift limits



Drift limits defined as a function of the failure mode occurred

$$\delta_m^{DL} = \frac{\Delta_m}{h_m} = \delta_u \begin{cases} 0.004 & \text{Shear} \\ 0.006-0.008 & \text{Rocking} \end{cases}$$



Shear failure



Rocking failure

# 3MURI – NON LINEAR BEAM – FAILURE CRITERIA FOR PIERS

## ■ Shear strength for masonry piers

Failure criteria for masonry piers are based on the approximate evaluation of the local (or mean) stress state induced by the applied forces on predefined points (or sections) of the panel, to be compared with proper limit strength domain for the constituent material (and the panel itself)

## ■ FLEXURAL BEHAVIOUR

Failure modes: *Rocking* and/or *Crushing*

$$M_u = \frac{Nl}{0.425 f_m} \left( 1 - \frac{N}{lt} \right)$$

## ■ SHEAR BEHAVIOUR – PRINCIPAL STRESS MODELS

Failure modes: *Diagonal Cracking*

(Turnsek and Cacovic Theory, 1971)

$$T_u = lt \frac{f_t}{b} \sqrt{1 + \frac{N}{f_t lt}}$$

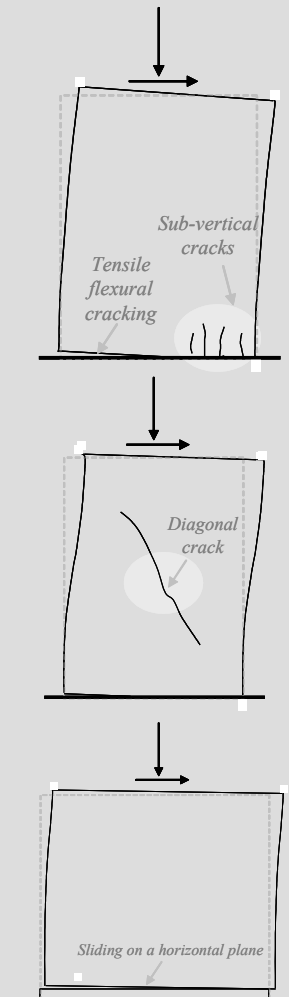
$b = f$  (slenderness of the panel)

## ■ SHEAR BEHAVIOUR – COULOMB TYPE MODELS

Failure modes: *Bed Joint Sliding* – *Diagonal Cracking through Joints*

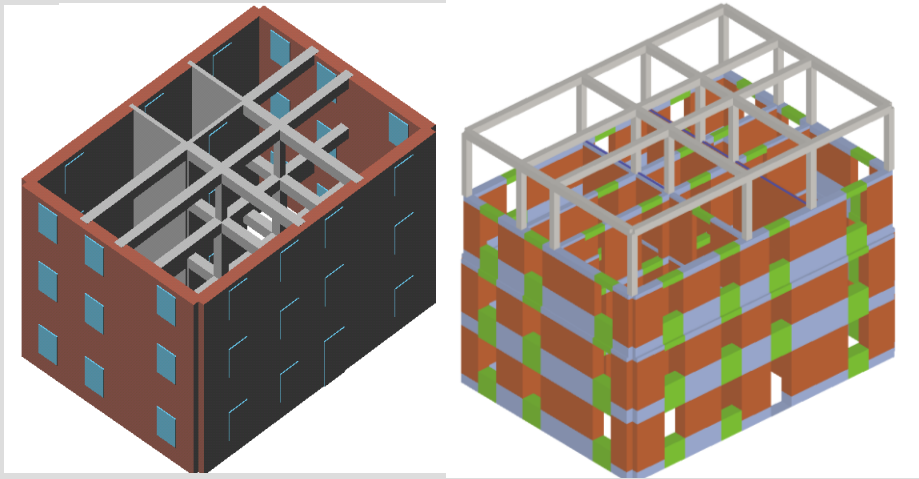
$$T_u = l'tc + \mu N$$

$$T_u = \frac{lt}{b} (\tilde{c} + \tilde{\mu} N)$$

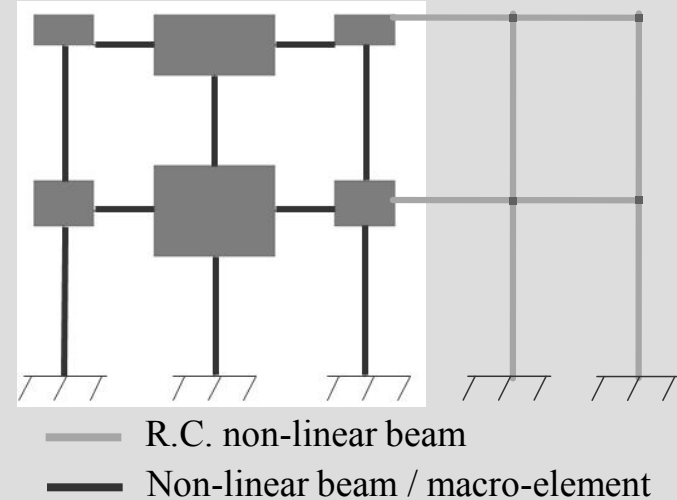


# 3MURI – REINFORCED CONCRETE BEAM ELEMENTS

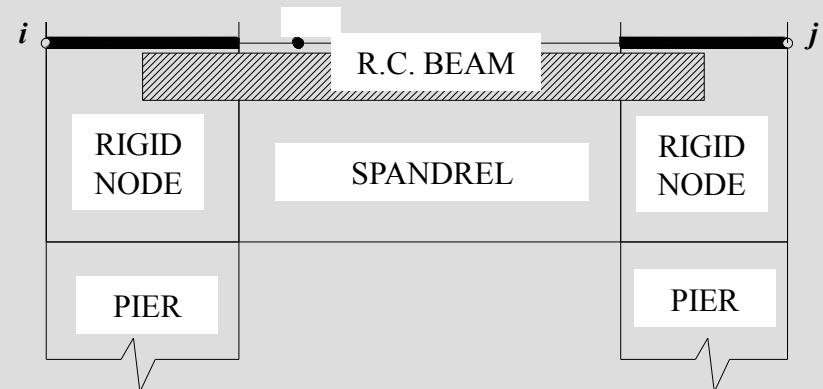
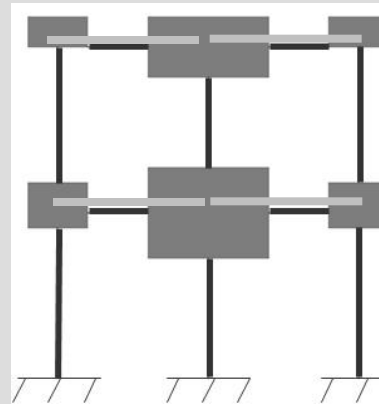
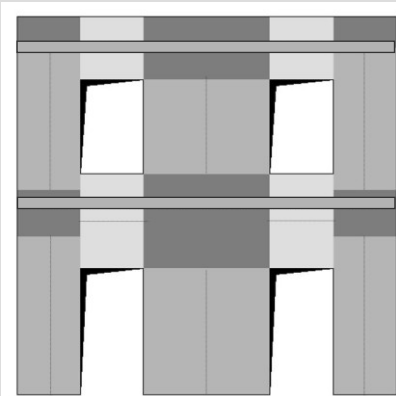
- ✓ Examples A: buildings with external masonry walls and internal r.c. beams, raising-up of masonry building with new r.c. storey, enlargement with a r.c. portion



Equivalent frame idealisation

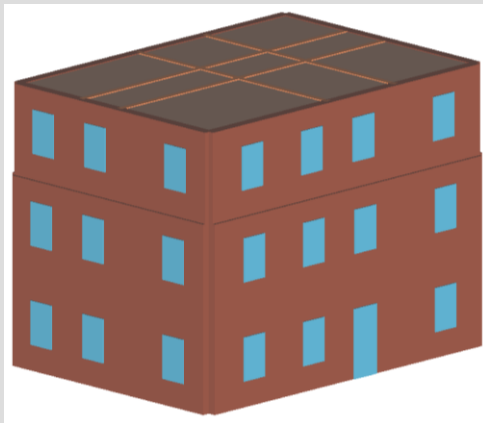


- ✓ Examples B: presence of r.c. beam coupled to spandrels

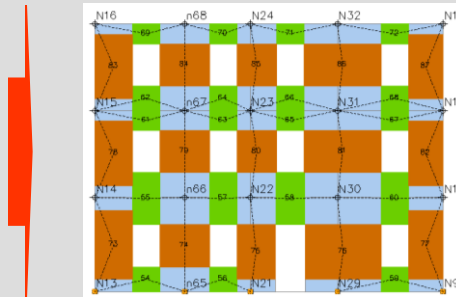
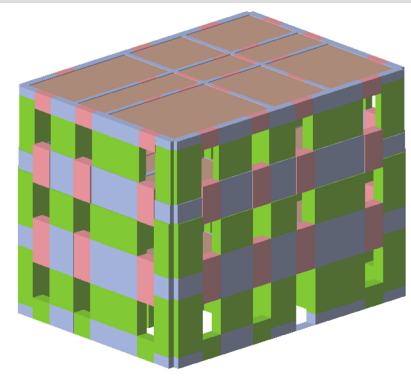


# 3-D EQUIVALENT FRAME MODEL

- ✓ 3-D equivalent frame is made of masonry walls, elastic floors, reinforced concrete elements
- ✓ out-of-plane stiffness and strength of masonry walls are neglected
- ✓ floors are planar elements with only in-plane stiffness, for sharing seismic action on walls



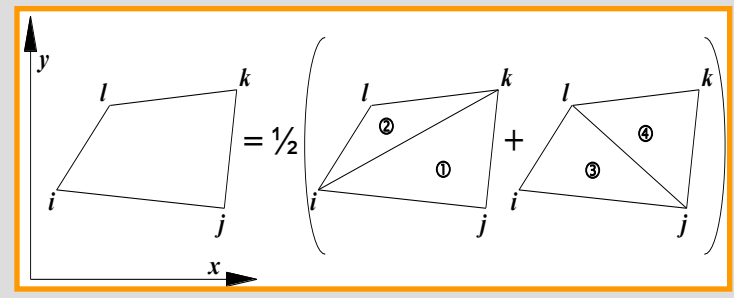
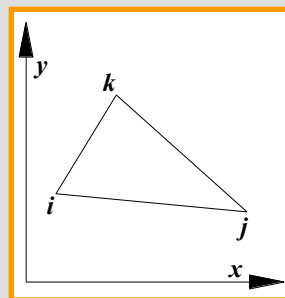
Modelling of floors



Equivalent frame idealisation of each structural walls

Assembling of 2D walls

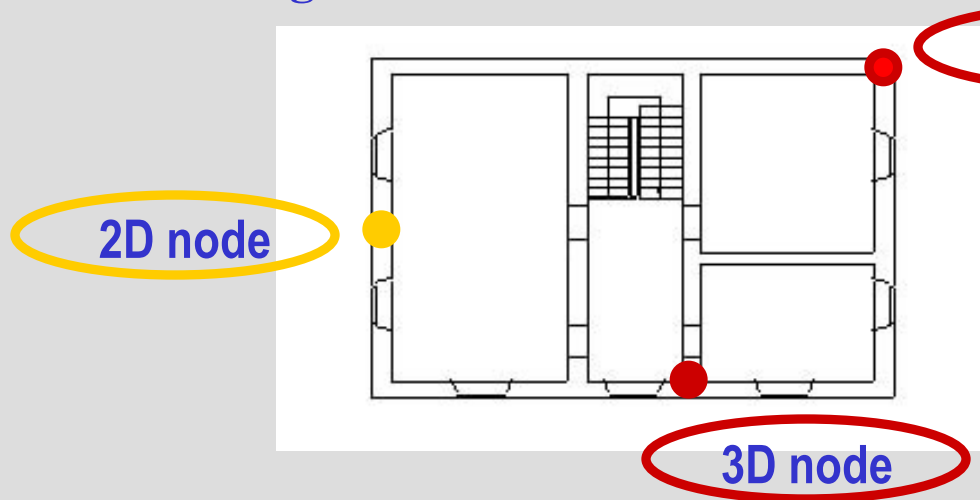
The floor are orthotropic membrane finite elements, with 3 or 4 nodes, defined by two independent axial stiffness and the shear stiffness





# 3-D EQUIVALENT FRAME MODEL

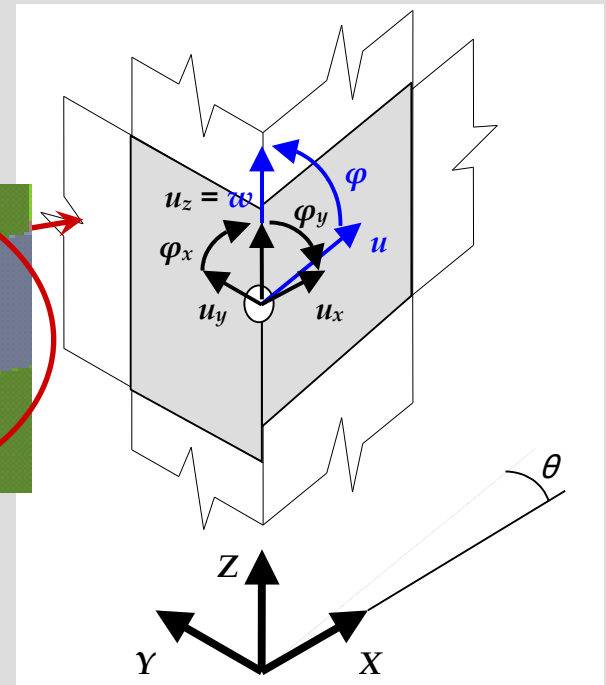
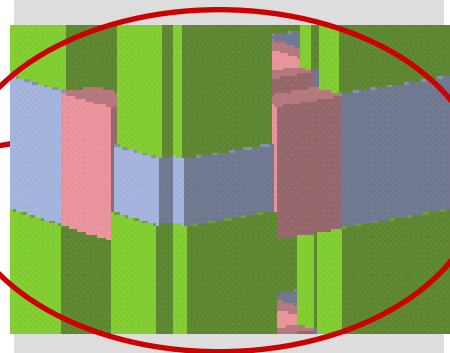
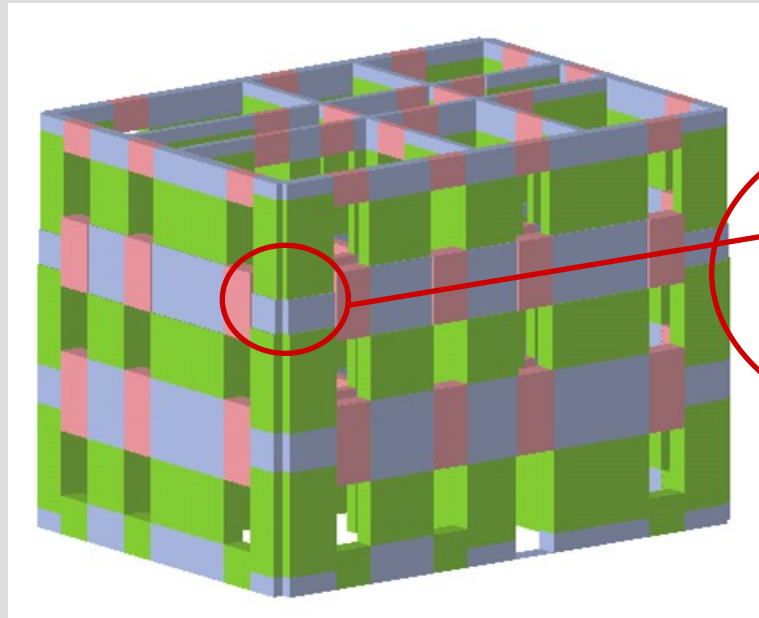
## Assembling 2D walls



3D node

➤ 3D nodes: 5 d.o.f → they come out from two 2D nodes

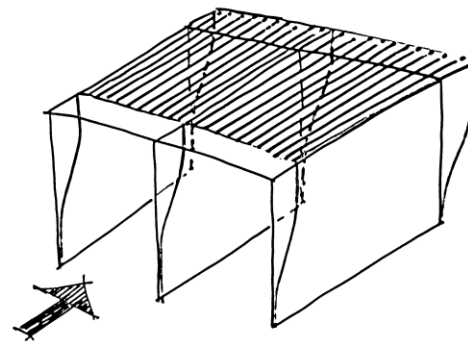
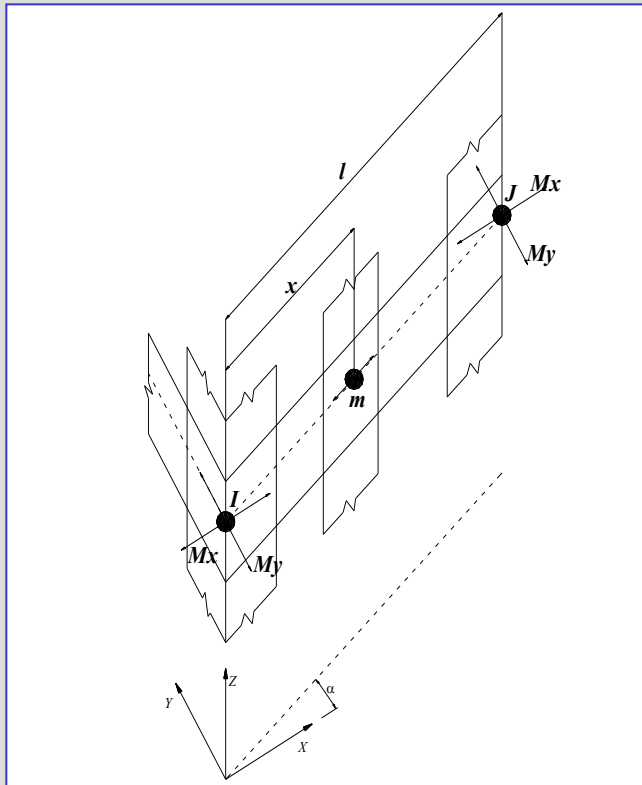
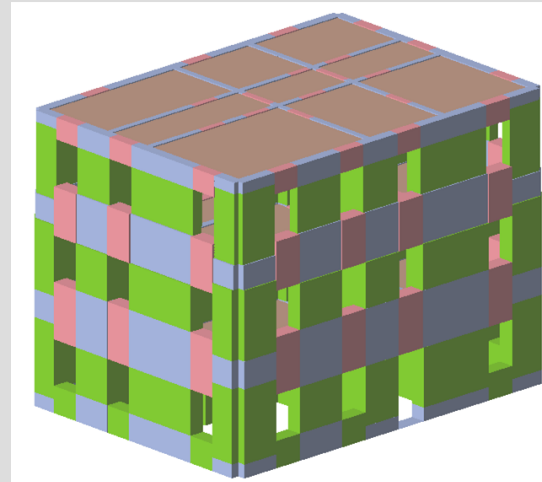
➤ 2D nodes: 3 d.o.f. in the wall plane



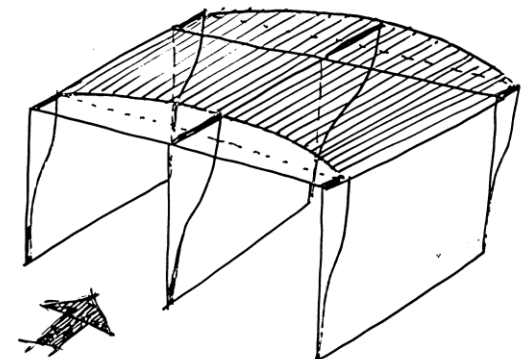
# 3-D EQUIVALENT FRAME MODEL

## 2D nodes: Sharing out of the nodal mass in the out-of-plane direction

$$M_x^I = M_x^I + m(1 - |\cos \alpha|) \frac{l - x}{l}$$
$$M_y^I = M_y^I + m(1 - |\sin \alpha|) \frac{l - x}{l}$$



RIGID FLOOR



FLEXIBLE FLOOR

# 3-D EQUIVALENT FRAME MODEL – FLOOR STIFFNESS

## TIMBER FLOORS

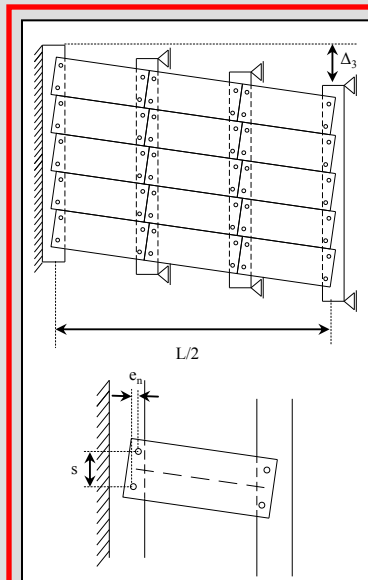
### FEMA Guidelines

Default expected values for the in-plane stiffness of different kinds of diaphragm related to existing, enhanced or new configurations

### New Zealand guidelines

Provide formulae for the evaluation of the diaphragm stiffness depending, for each floor type, on the properties of each component.

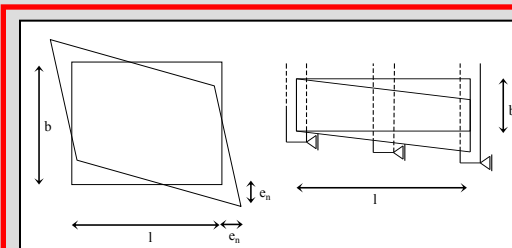
Diaphragm type	$G_d$ [kN/mm]
Single straight sheathing	0.35
Double straight sheathing	
Chorded	2.67
Un-chorded	1.24
Wood structural panel overlay on straight sheathing	
Un-blocked, un-chorded	0.87
Un-blocked, chorded	1.58
Blocked, un-chorded	1.24
Blocked, chorded	3.20



### Single straight Sheathing

$$G_d = \frac{s^2 \cdot k_{nail}}{2 \cdot l \cdot b}$$

( only the contribution of nails is considered)



### Panels sheathing

$$G_d = \left( \text{Panel contribution} + \text{Nails contribution} \right)^{-1}$$

Panel  
contribution

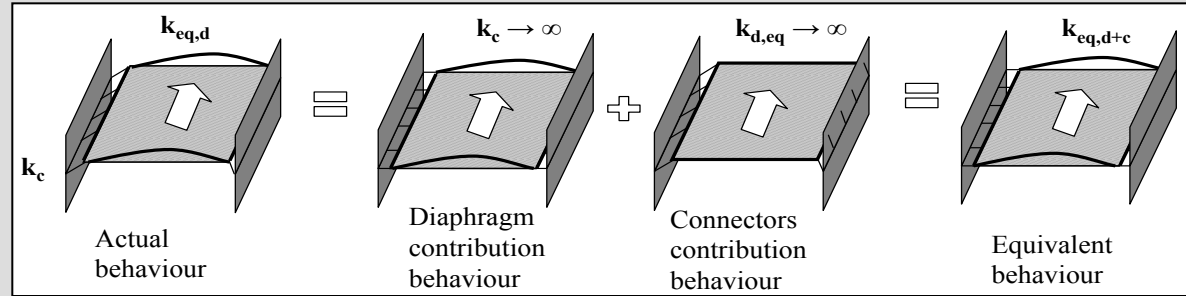
Nails  
contribution

# 3-D EQUIVALENT FRAME MODEL – FLOOR STIFFNESS

## TIMBER FLOORS

**Brignola 2009 (PhD Thesis)**

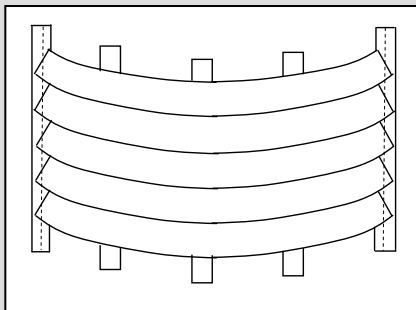
Proposal based on the results of an experimental campaign carried out at Canterbury University



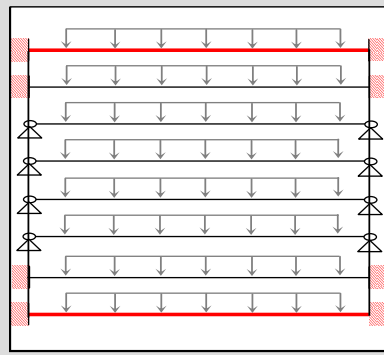
### Straight flooring boards

$$G_{d+c} = \left[ \left( \text{Wood beam contribution} + \text{Steel beam contribution} + \text{Chord contribution} \right)^{-1} + \text{Connector contribution}^{-1} \right]^{-1}$$

Wood beam contribution

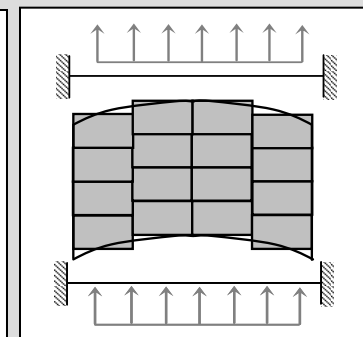
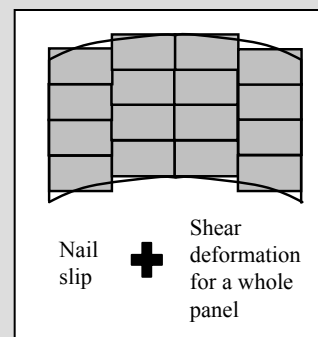


Chord and steel beam contribution



### Straight flooring boards and plywood panels overly

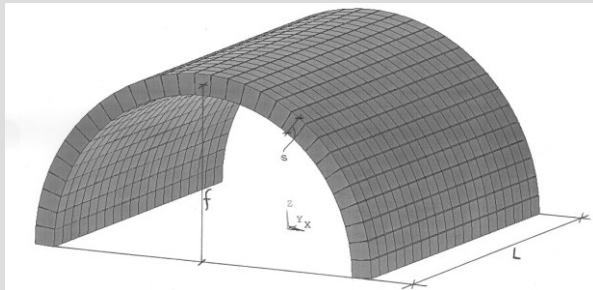
$$G_{d+c} = \left[ \left( \text{Panel contribution} + \text{Nails contribution} + \text{Chord contribution} \right)^{-1} + \text{Connector contribution}^{-1} \right]^{-1}$$



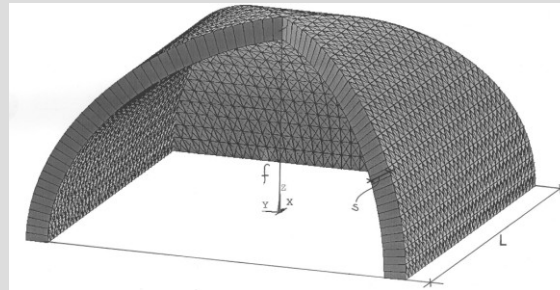
# 3-D EQUIVALENT FRAME MODEL – FLOOR STIFFNESS

## MASONRY VAULTS

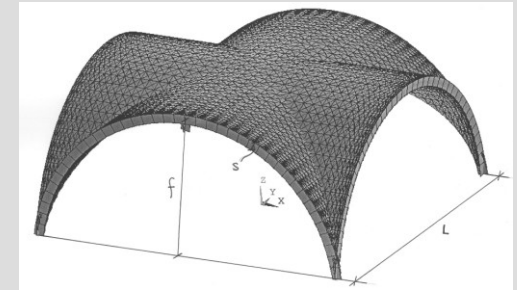
Linear and non linear parametric FEM simulations (Cattari et al. 2008, Proc. of 6<sup>th</sup> SAHC)



Barrel vault

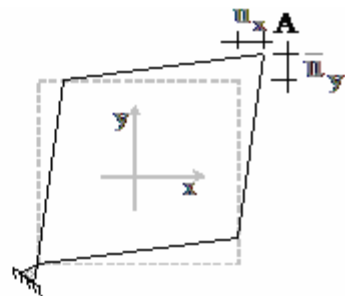
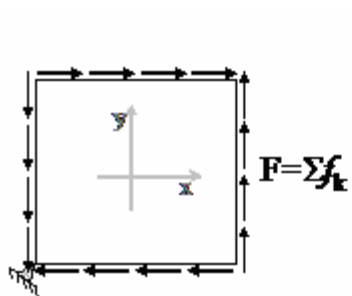
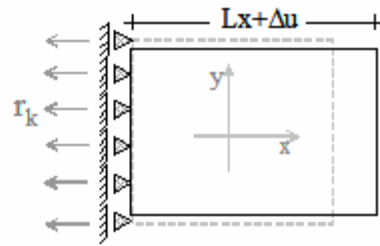
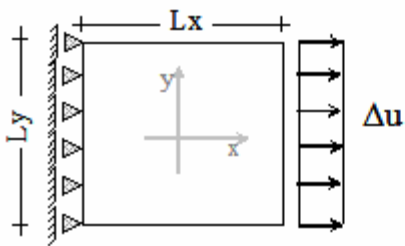


Cloister vault



Cross vault

Boundary configuration and loads



## LINEAR NUMERICAL ANALYSES

Shear stiffness  $G_v/G$

Analytical expressions aimed to take into account the shape effect and the boundary conditions as a function of the vault types

$$\frac{G_v}{G} = \left( b_1 \frac{s}{L} + b_2 \right) \left( \frac{f}{L} \right) + b_3 \frac{s}{L} + b_4$$

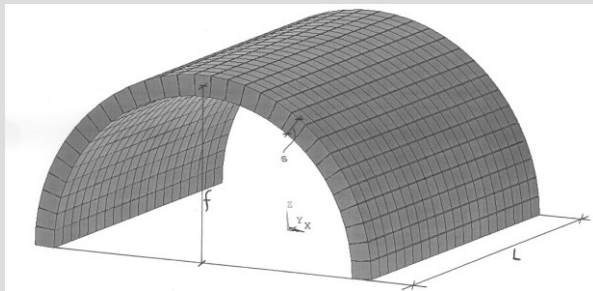
	Vault typology		
	Barrel	Cloister	Cross
$b_1$	1.6433	-0.1633	-1.12
$b_2$	-1.8191	-1.3051	-4.1766
$b_3$	0.1133	1.9733	8.9033
$b_4$	1.1189	1.0339	0.7273
$b_5$	-	-	-34.323
$b_6$	-	-	5.6202



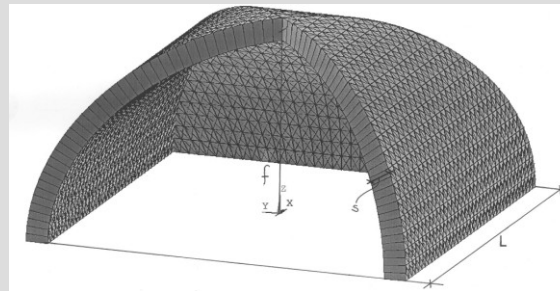
# 3-D EQUIVALENT FRAME MODEL – FLOOR STIFFNESS

## MASONRY VAULTS

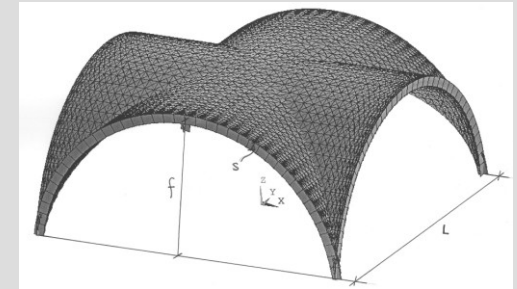
Linear and non linear parametric FEM simulations (Cattari et al. 2008, Proc. of 6<sup>th</sup> SAHC)



Barrel vault

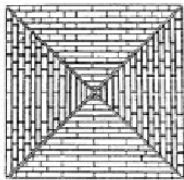


Cloister vault

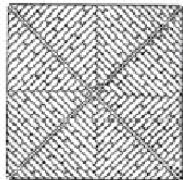


Cross vault

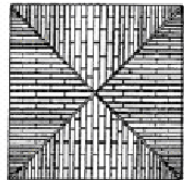
Parametrical analyses for different texture patterns



Tessitura A

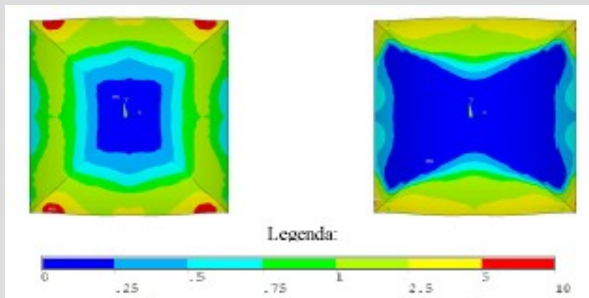


Tessitura B



Tessitura C

Cloister vaults – damage pattern texture pattern A – shear response

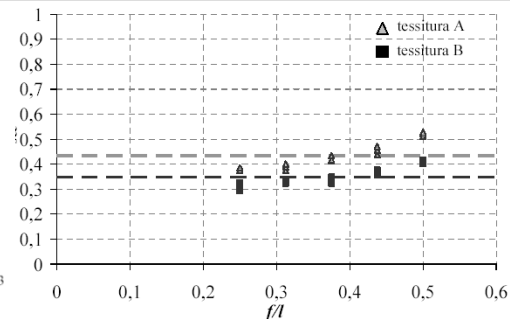
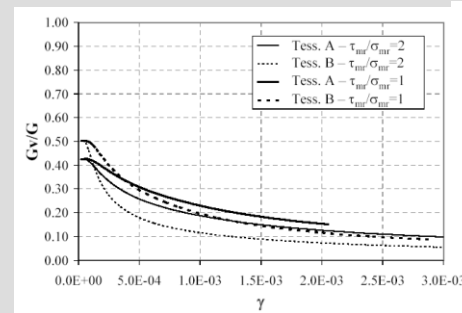


## NON LINEAR NUMERICAL ANALYSES

Effects valid in linear range

$$G_{eq} = \frac{G}{2}$$

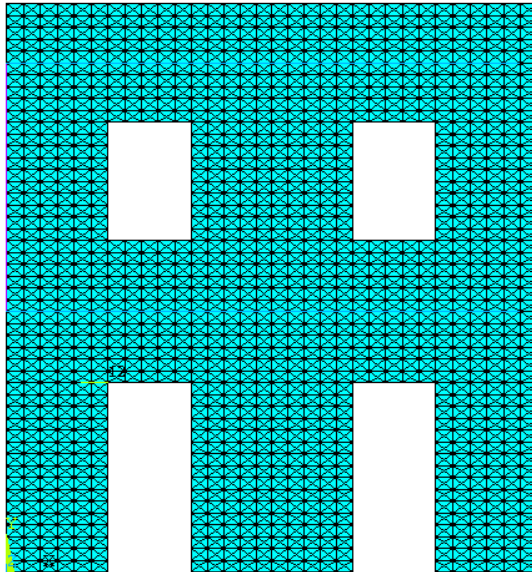
Effect of stiffness degradation



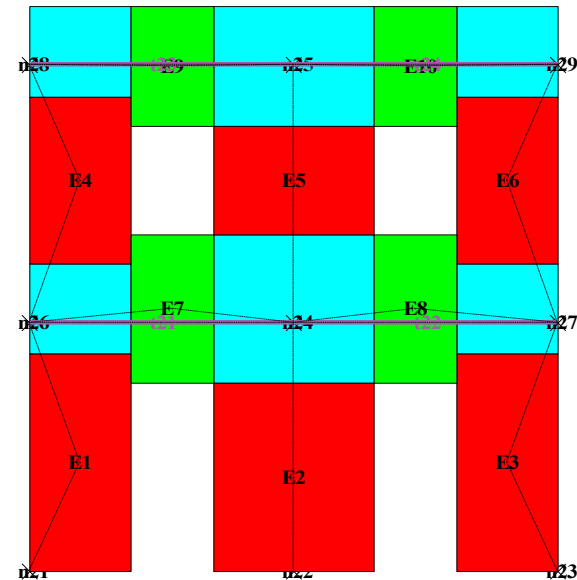
# EQUIVALENT FRAME MODEL: VALIDATION AND EXAMPLES OF APPLICATION

Modelling scale

Finite Element Model



Equivalent Frame Model



Constitutive law

Constitutive law for masonry formulated by Calderini and Lagomarsino

Non-linear beam model - Elasto-plastic constitutive law with secant stiffness degradation. The resistance criteria adopted are: for the *Rocking*, that proposed in the Italian Code ; for the *Diagonal Cracking*, the criterion proposed by Mann and Müller

# EQUIVALENT FRAME MODEL: VALIDATION AND EXAMPLES OF APPLICATION

## FINITE ELEMENT MODEL

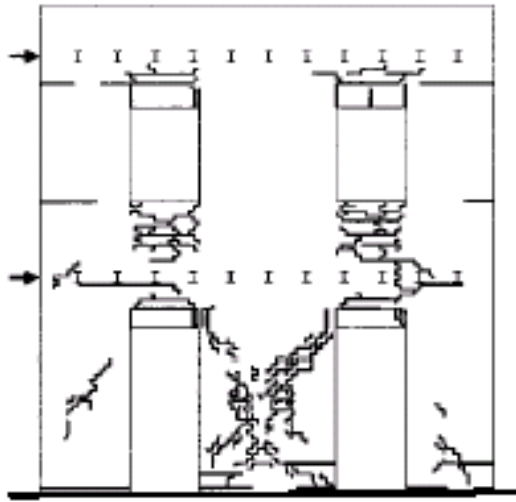
## EQUIVALENT FRAME MODEL

Mechanical parameters	<i>Elastic compliance parameters</i> Young modulus: 1400 MPa Shear modulus: 480 MPa	<i>Elastic compliance parameters</i> Young modulus: 700 MPa Shear modulus: 240 MPa
	<i>Inelastic compliance parameters</i> Ratio elastic/inelastic shear strain at failure in mortar joints: 4 Ratio elastic/inelastic normal strain of masonry in compression at failure: 2	
	<i>Strength parameters</i> Mortar joints Cohesion: 0.23 MPa Friction coefficient: 0.58 Tensile strength: 0.04 MPa Softening coefficient: 0.4	<i>Strength parameters</i> Mortar joints Cohesion: 0.23 MPa Friction coefficient: 0.58
	Blocks Tensile strength: 1.22 MPa Shear strength: 2.1 MPa Softening coefficient: 0.0	Blocks Tensile strength: 1.22 MPa
	Masonry Compressive strength: 6.2 MPa Block aspect ratio (width/height): 4	Masonry Compressive strength of masonry: 6.2 MPa Block aspect ratio (width/height): 4

# EQUIVALENT FRAME MODEL: VALIDATION AND EXAMPLES OF APPLICATION

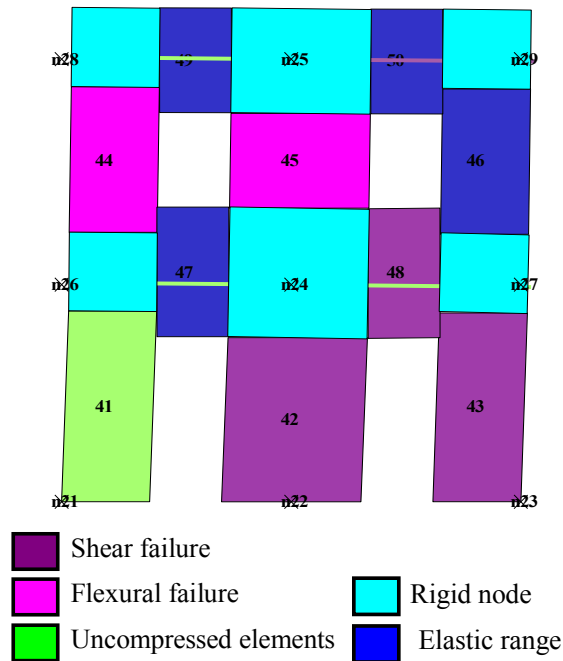
## DAMAGE STATE AT COLLAPSE

PROTOTYPE

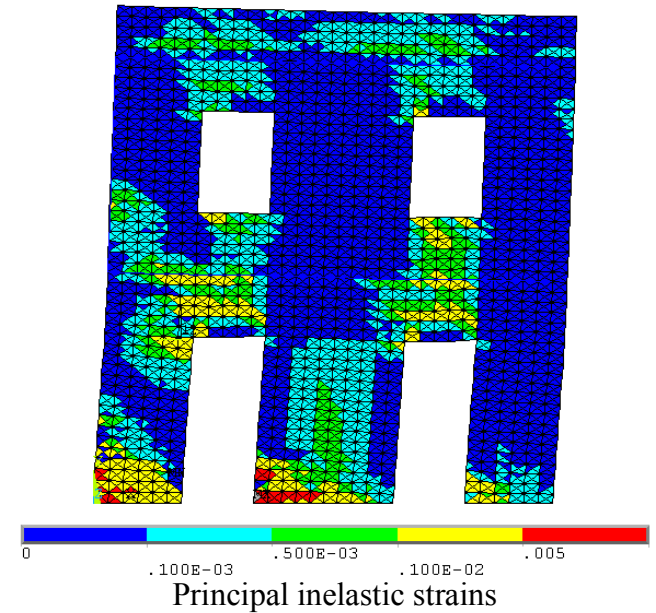


$dx = 15 \text{ mm}$

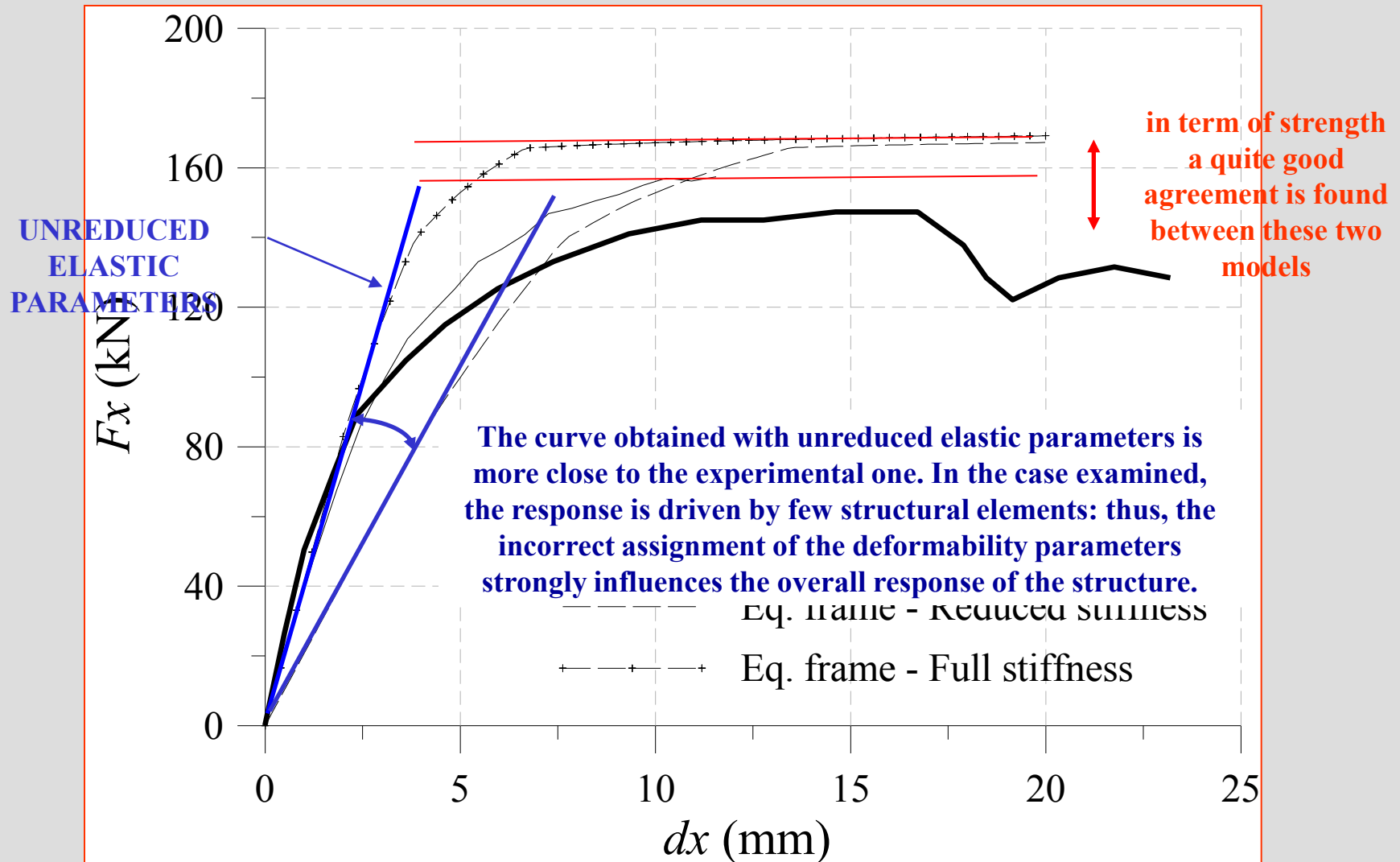
EQUIVALENT FRAME



FEM

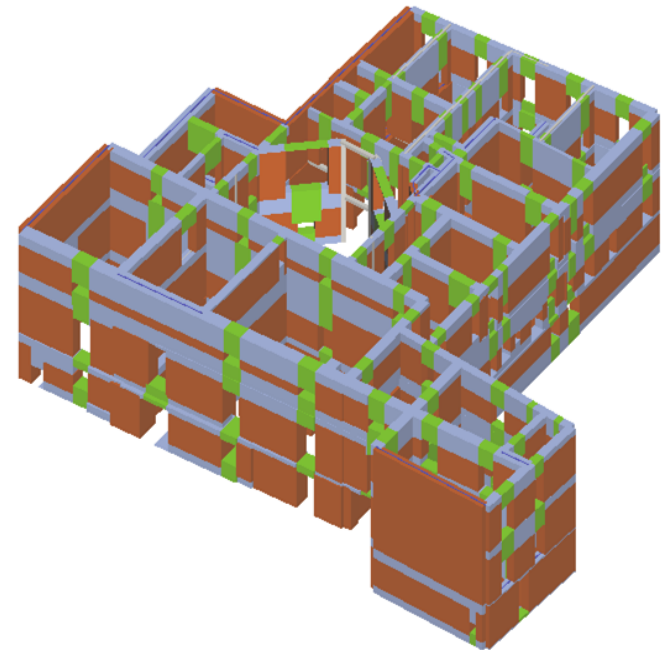
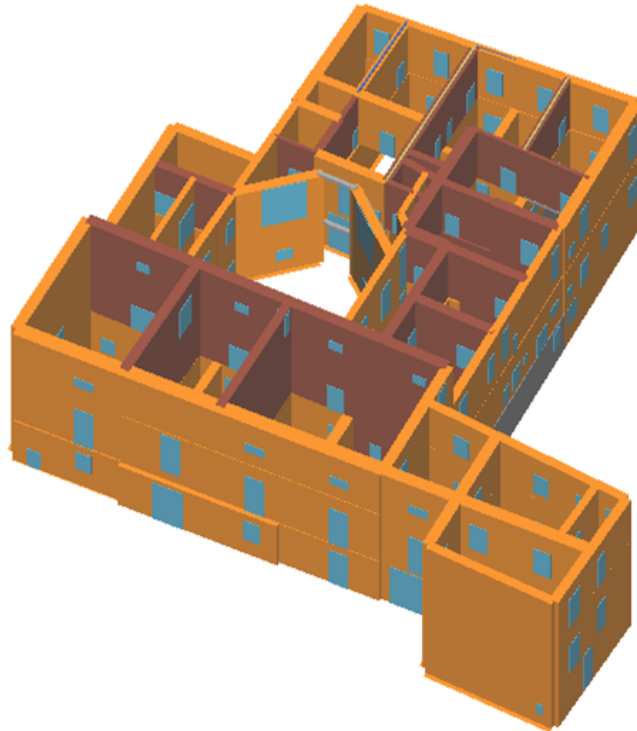


# EQUIVALENT FRAME MODEL: VALIDATION AND EXAMPLES OF APPLICATION

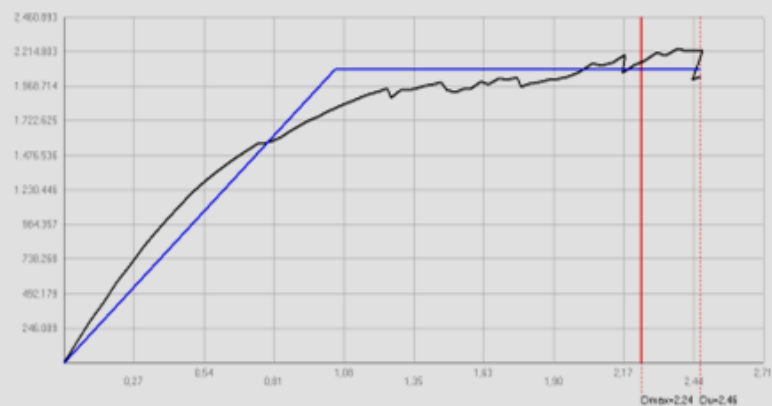




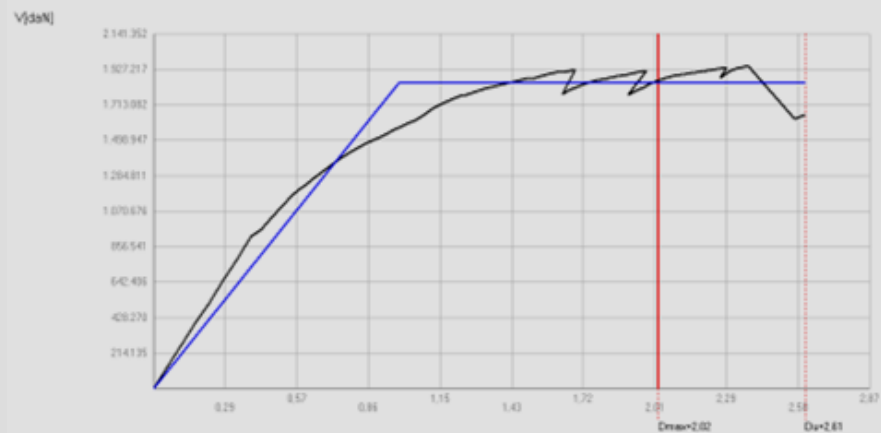
# ARDINGHELLI PALACE, L'AQUILA



NT 08: Verifica SLU soddisfatta - Verifica SLD soddisfatta



NT 08: Verifica SLU soddisfatta - Verifica SLD soddisfatta



#### Muratura

- Integro
- Plastico per taglio
- Rottura per taglio
- Plastico presso flessione
- Rottura presso flessione
- Rottura per compressione
- Rottura per trazione
- Rottura in fase elastica

